

# Energy system modeling

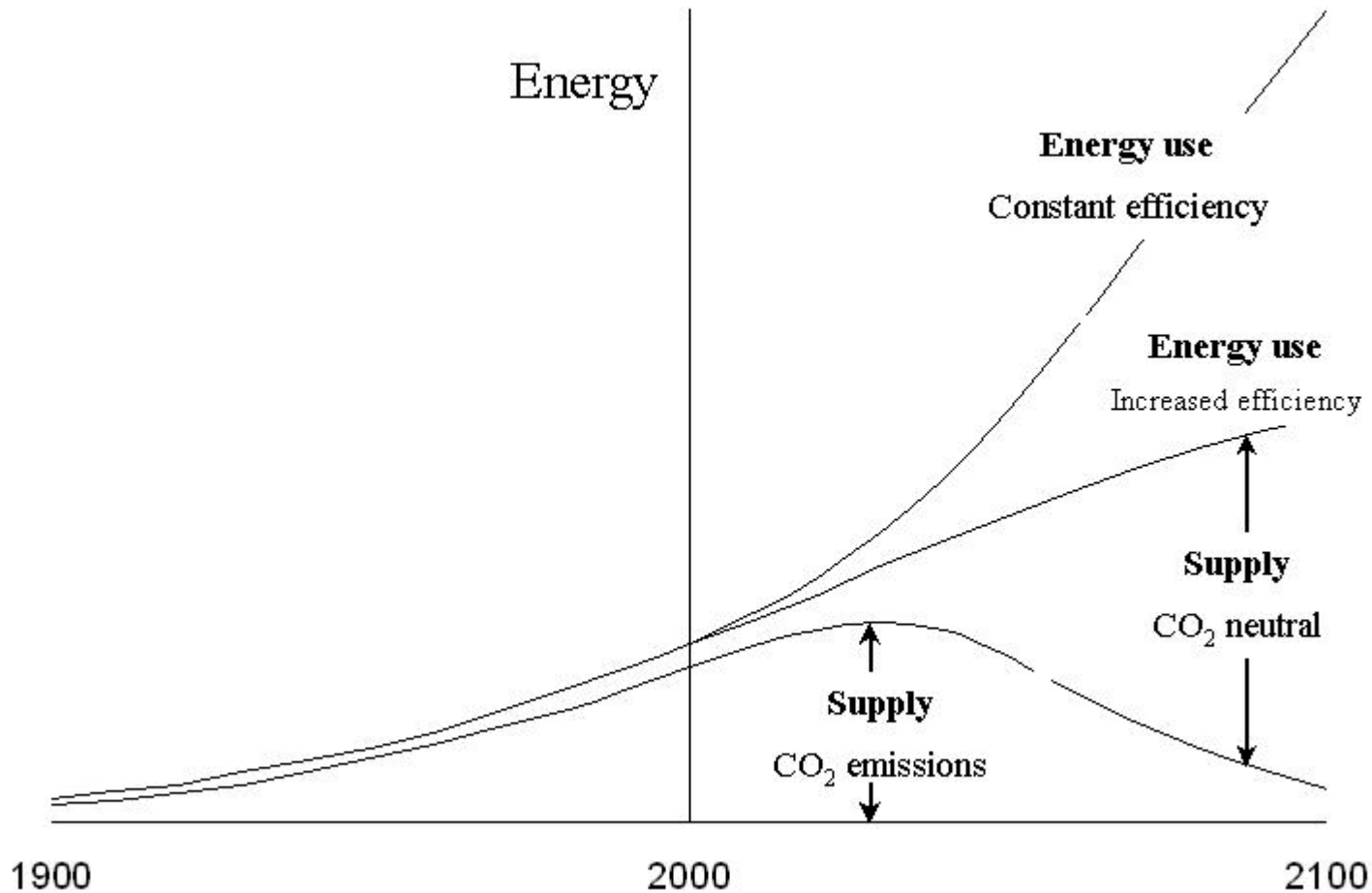
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# Outline

- Structure of energy system models
- Background on energy technologies
- Results and analysis

# Strategies to reduce carbon dioxide emissions



# Research questions

- Which energy technologies are the cheapest to use?
- What is the cost of reducing the emissions?
- Which interrelations are there in the energy system?
- Where is it most cost-effective to use biomass?
- What determines the future transport system?

# Objective to minimize cost

$$A(t) = \sum_f S(f, t)p(f) + \sum_{x, y} I(x, y, t)k(x, y)$$

- $A(t)$  Annual cost of the energy system
- $S(f, t)$  Energy supply
- $p(f)$  Fuel cost
- $I(x, y, t)$  Investments made
- $k(x, y)$  Capital costs for energy conversion

# Discounting

- Do you prefer the get 1000 USD today or in 10 years?
- We are richer in the future
- We get interest at the bank
- Uncertainty about the future

# Objective function

$$\min C = \sum_{t=1}^T \frac{A(t)}{(1+r)^{t-1}}$$

- $C$ , total cost,  $A(t)$  annual cost,  $t$  time
- Discount rate,  $r$ , 5 %

# Main constraints

- Emission constraints

$$U(t) = \sum_f S(f, t) \beta(f)$$

- Supply must be equal demand

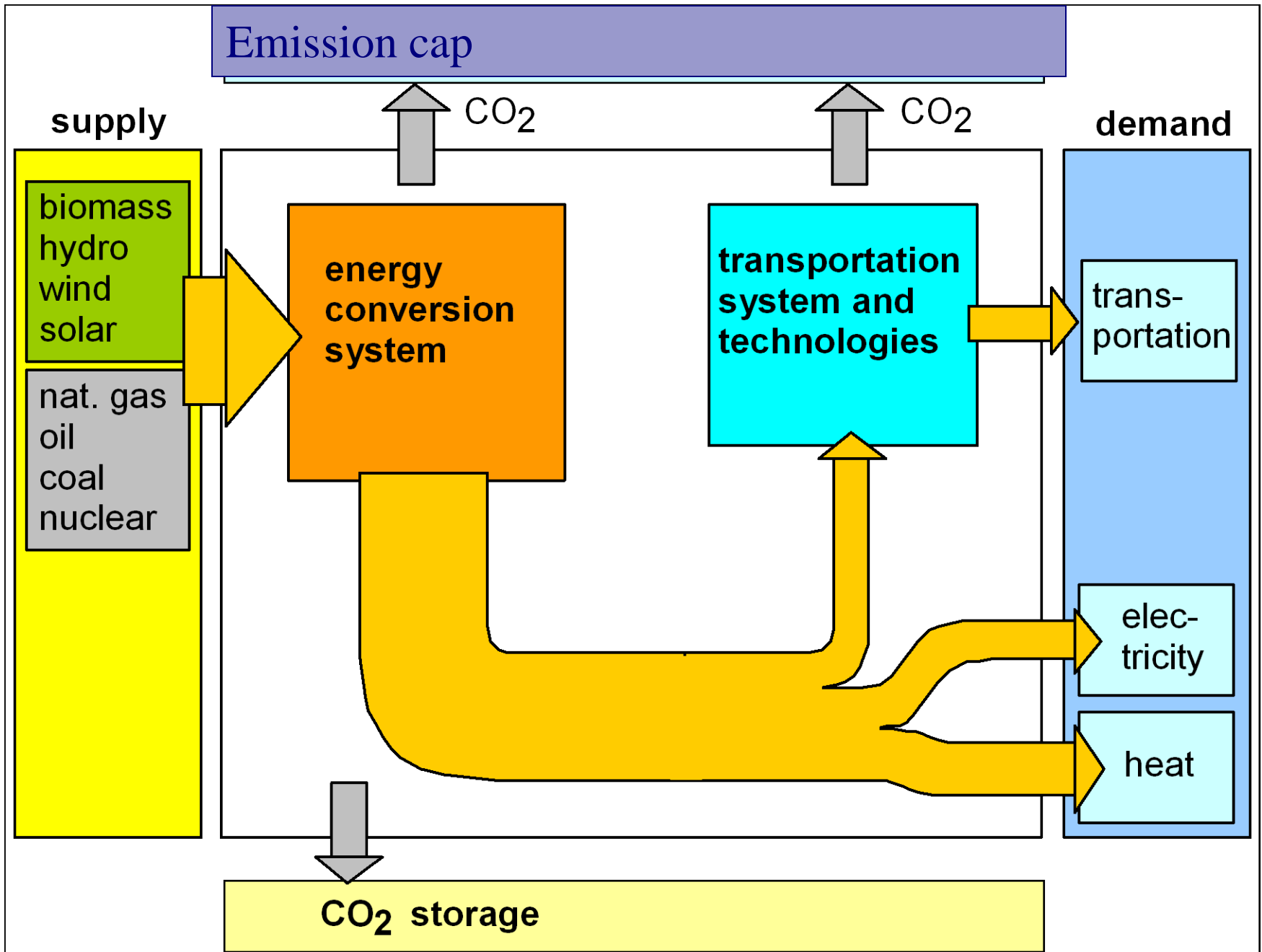
$$D(t, y) + e(y, t) = \sum_x E(x, y, t) \eta(x, y)$$

$$e(\text{elec}, t) = \sum_y E(\text{elec}, y, t)$$

- Fossil resource constraints

$$\sum_t S(f, t) \Delta t \leq R(f)$$





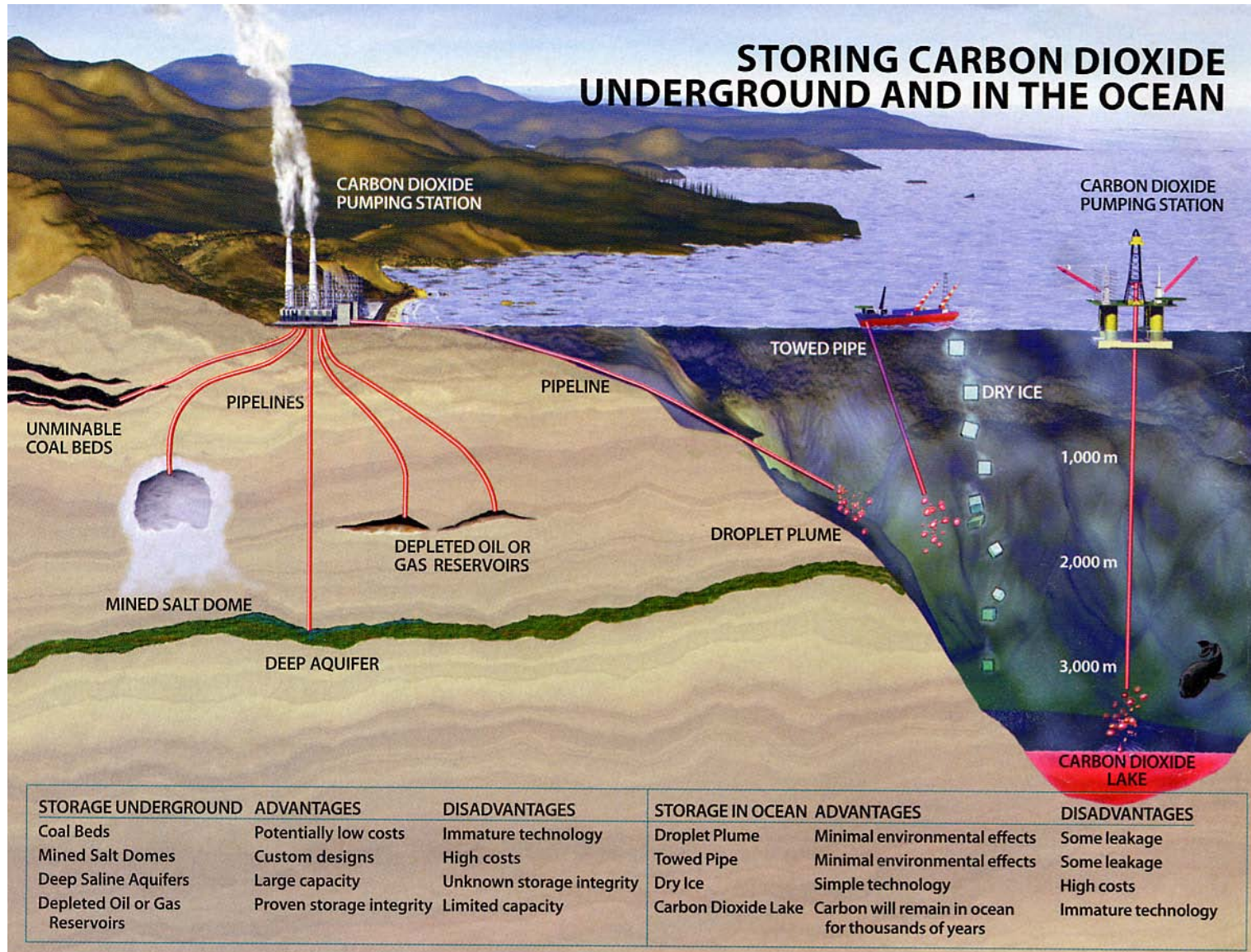
Human energy use – 410 EJ/yr

Biological production – 1 800 EJ/yr

Wind, waves, thermal energy in  
oceans

Solar radiation –  
5 440 000 EJ/yr

# Carbon capture and storage (CCS)



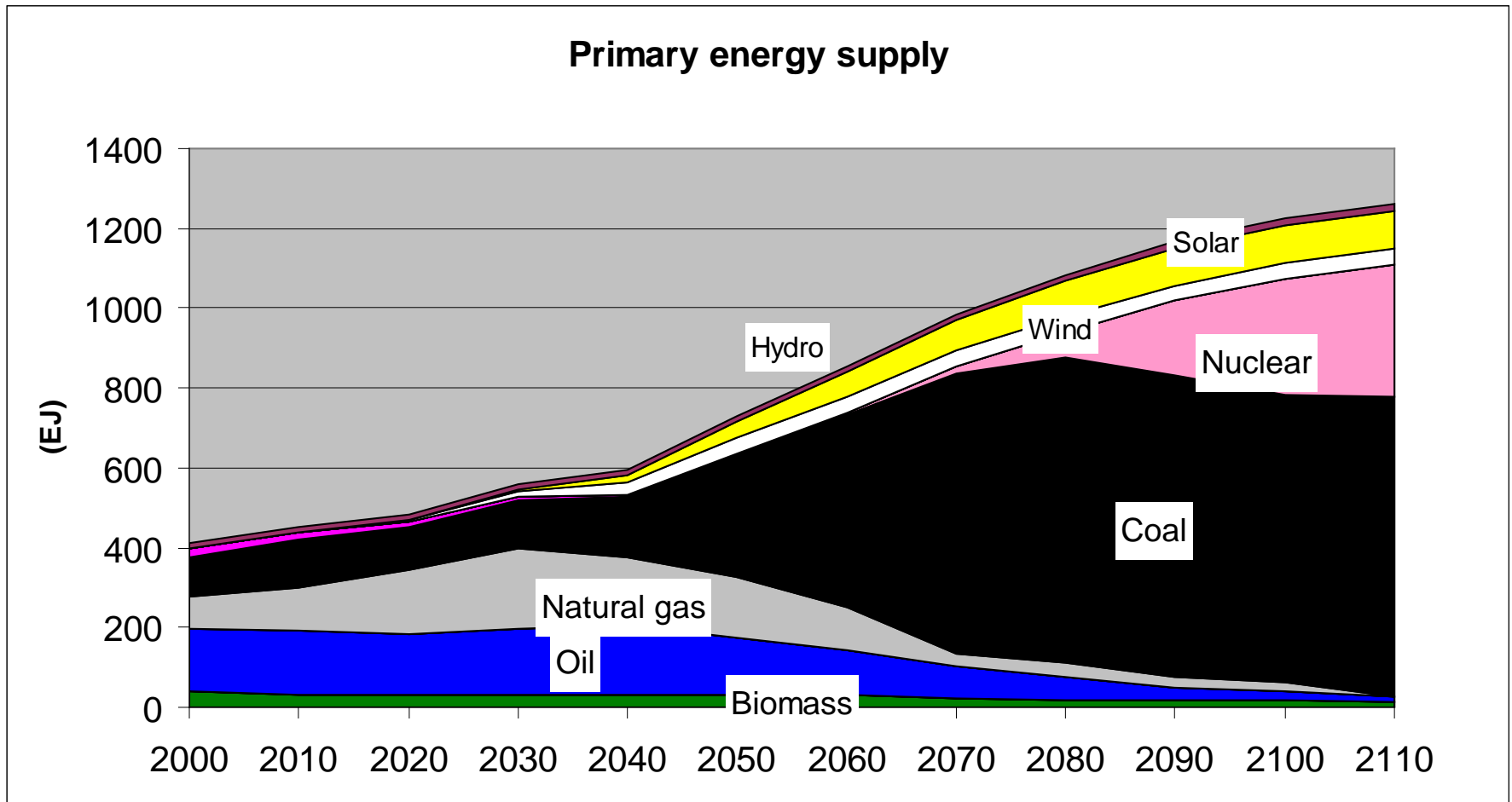
# Energy carrier

- Hydrogen H<sub>2</sub>
  - Fossil fuels with CCS
  - Bioenergy (with CCS)
  - Solar energy
- Synthetic fuels CH<sub>2</sub>
  - Fossil fuels with CCS
  - Bioenergy (with CCS)
- Electricity
  - Fossil fuels with CCS
  - Nuclear power
  - Solar energy

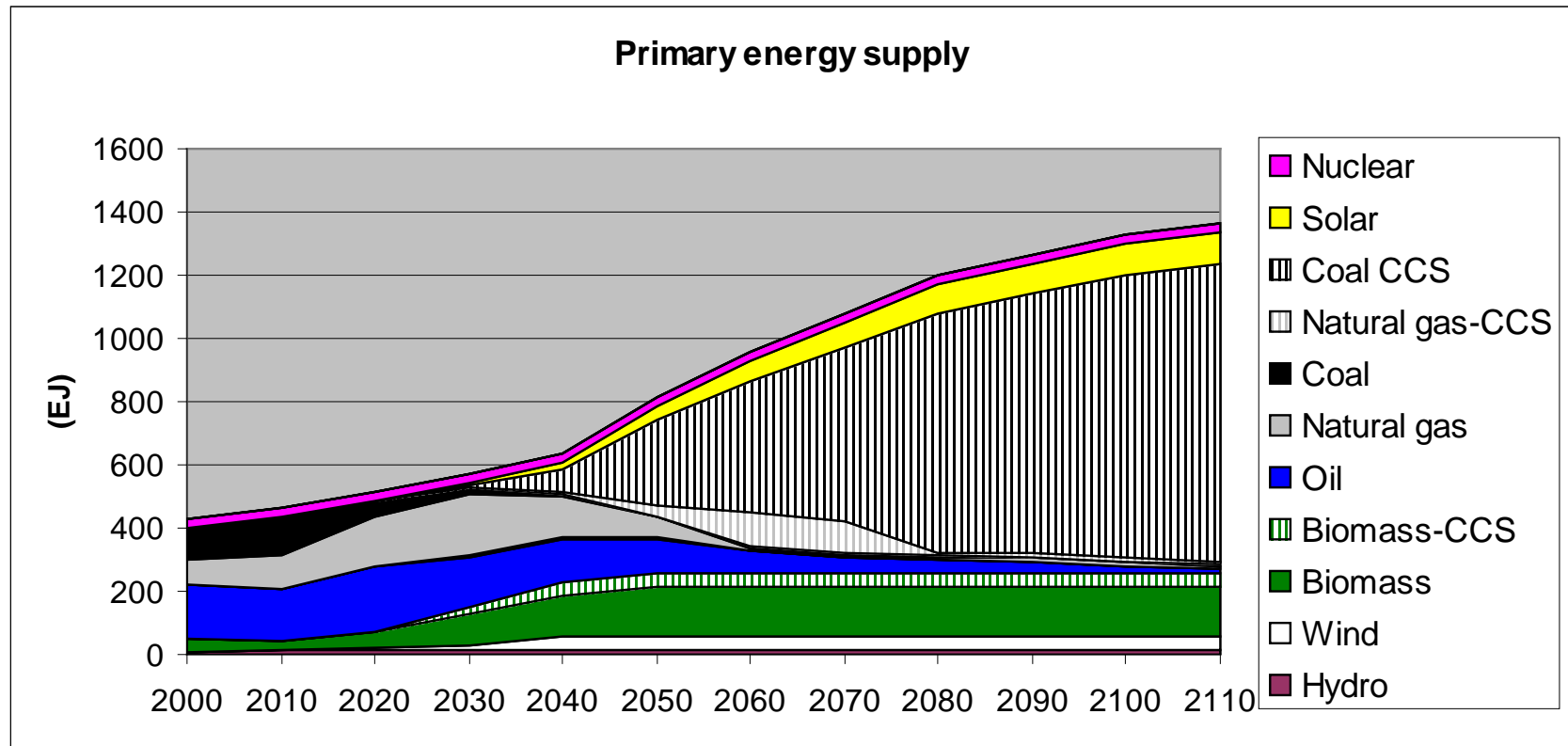
# Vehicles types

- Hybrid cars (HEV)
  - 35% more efficient for personal transport
- Plug-in hybrid (PHEV)
  - Charged from the grid
- Hydrogen fuel cells (FCV)
  - 70 % more efficient

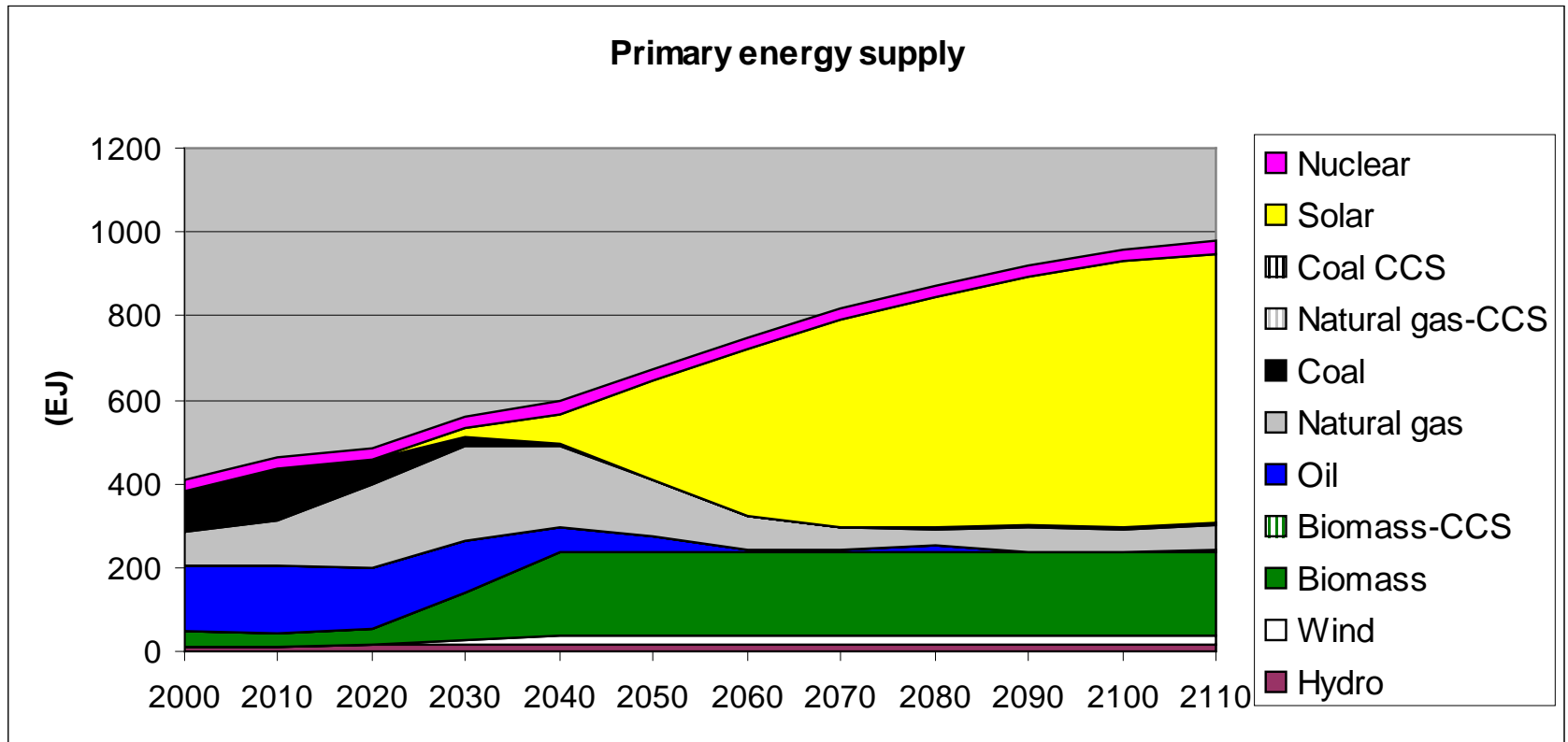
# Global baseline scenario



# 400 ppm, limited nuclear, CCS allowed



# 400 ppm, no nuclear and no CCS



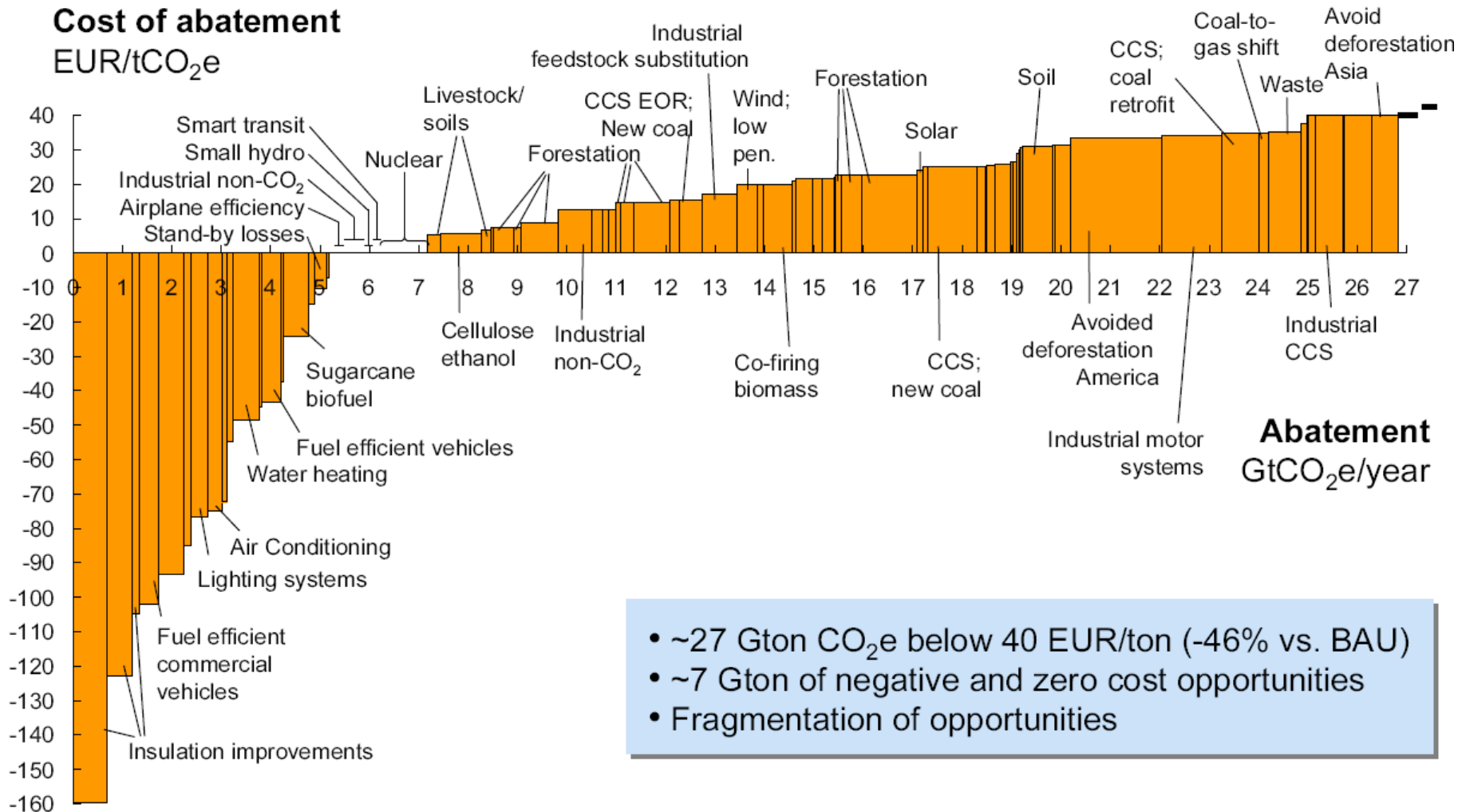


Stabilization is possible at limited costs – markets can supply

2030

Cost of abatement

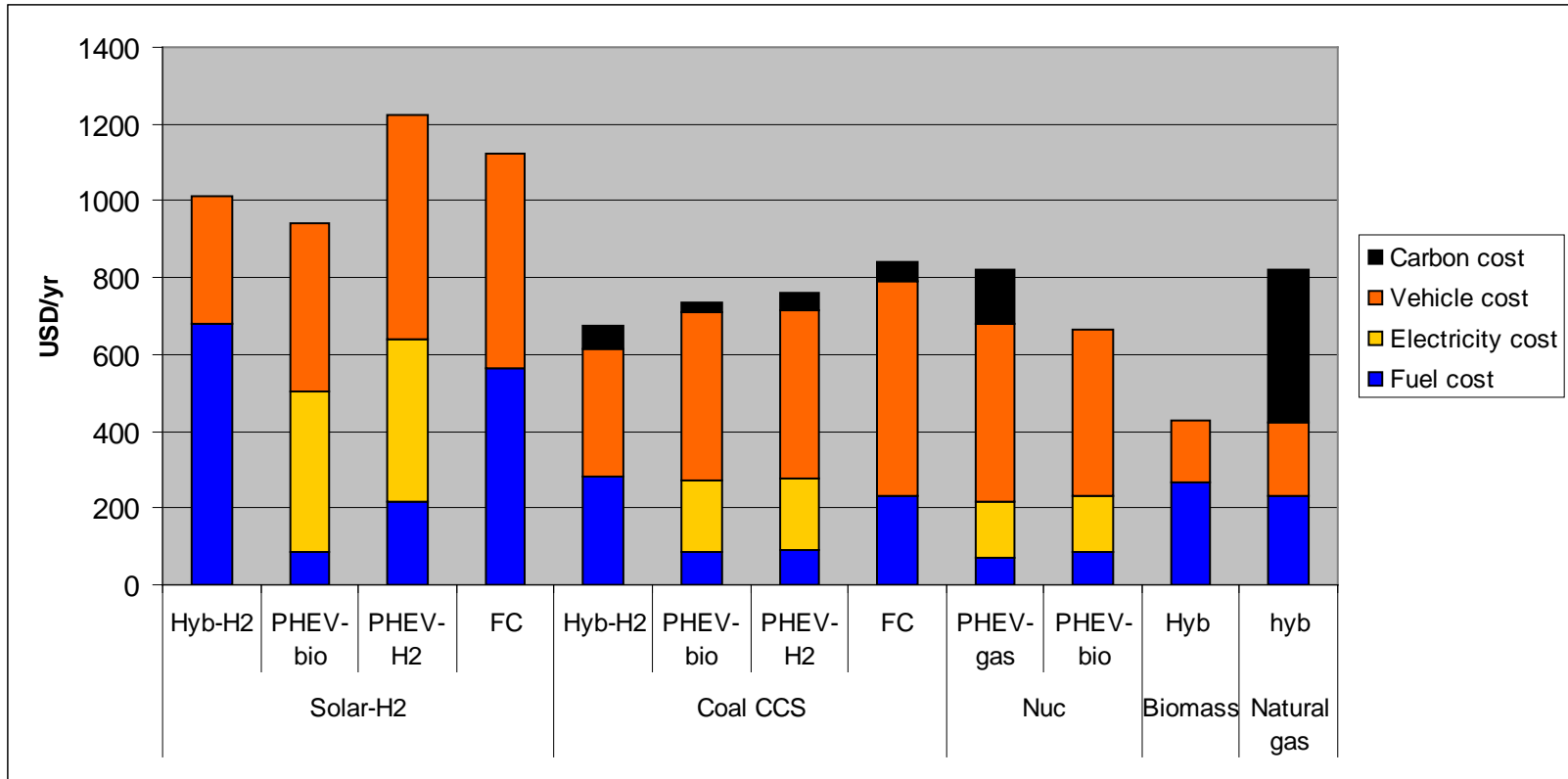
EUR/tCO<sub>2</sub>e



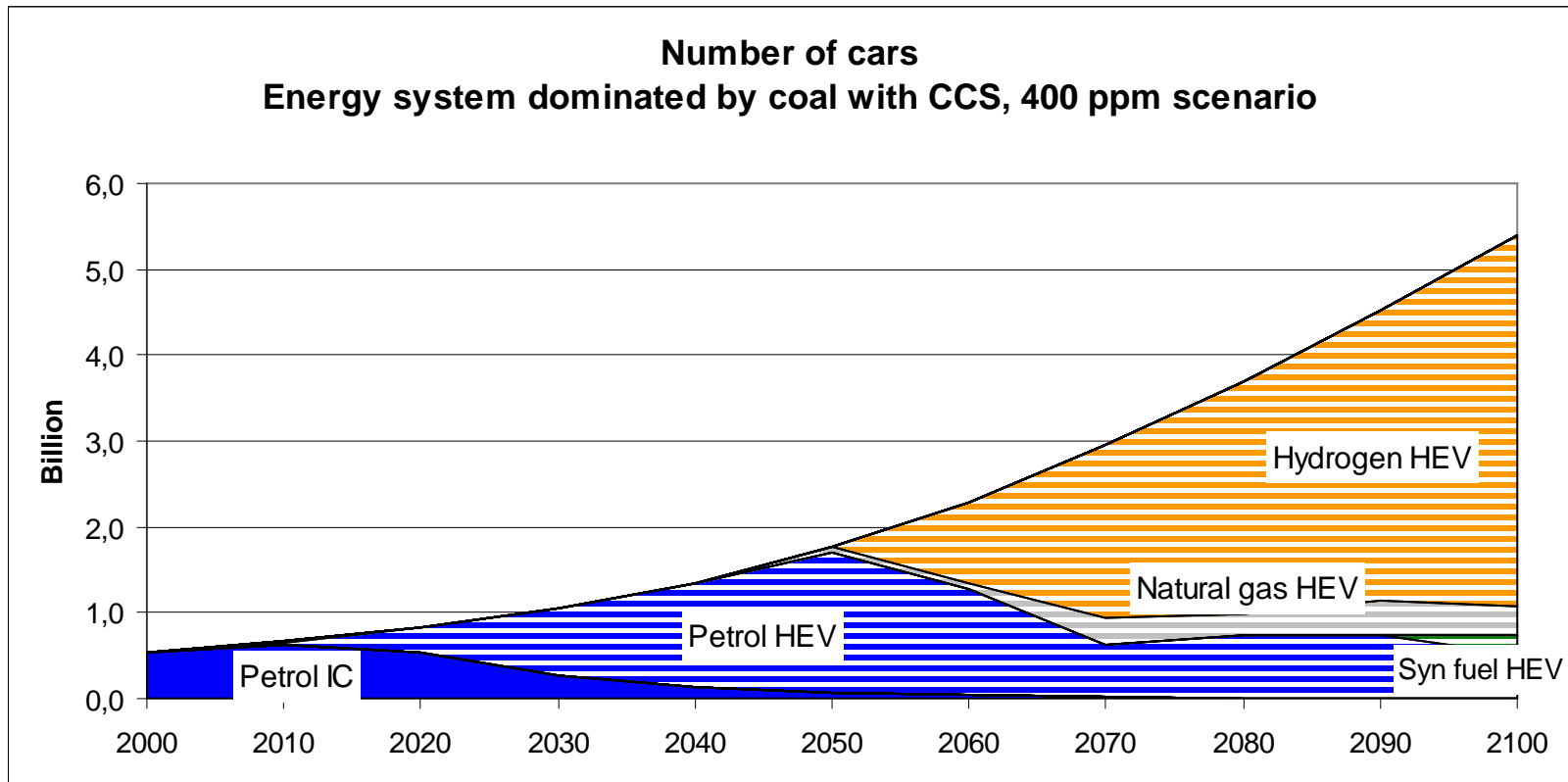
**Abatement**  
GtCO<sub>2</sub>e/year

- ~27 Gton CO<sub>2</sub>e below 40 EUR/ton (-46% vs. BAU)
- ~7 Gton of negative and zero cost opportunities
- Fragmentation of opportunities

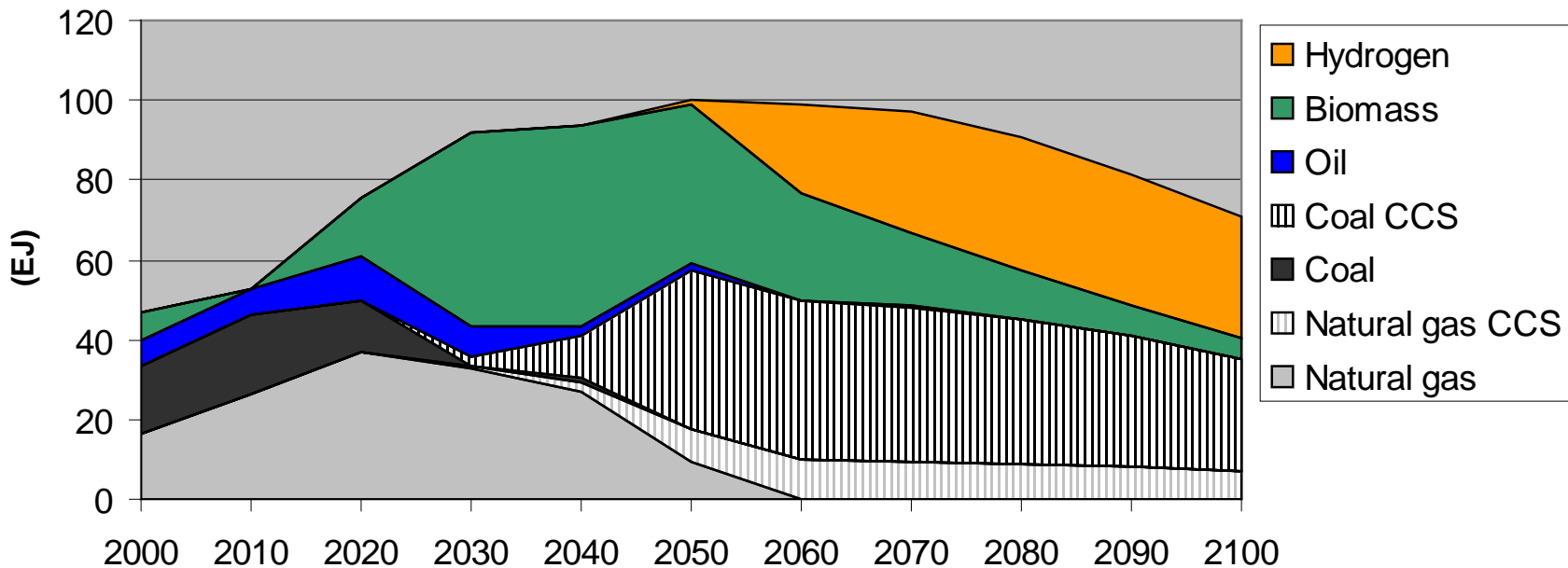
# Vehicle costs, carbon price 1000 USD/ ton C



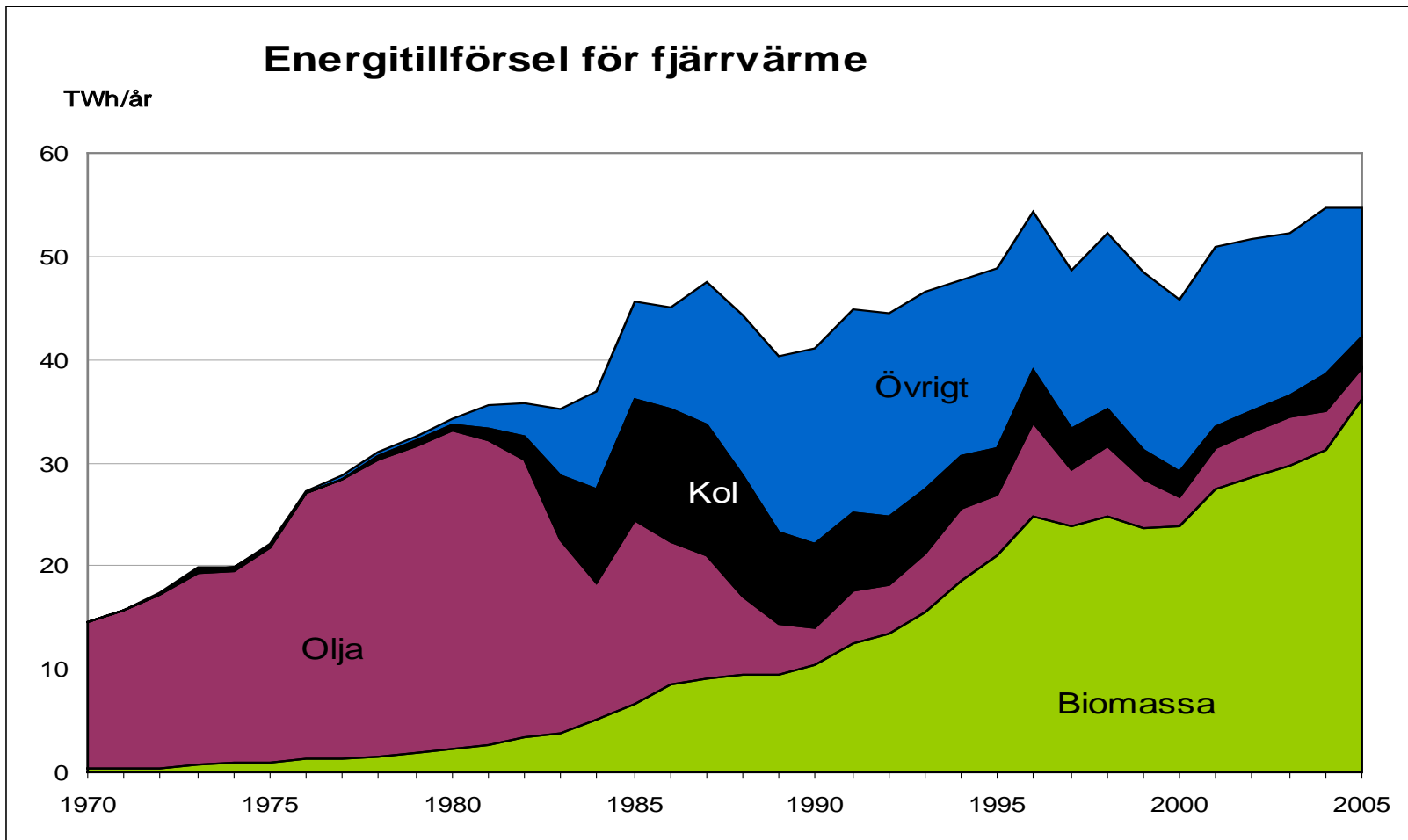
# 400 ppm scenario, limited nuclear CCS allowed



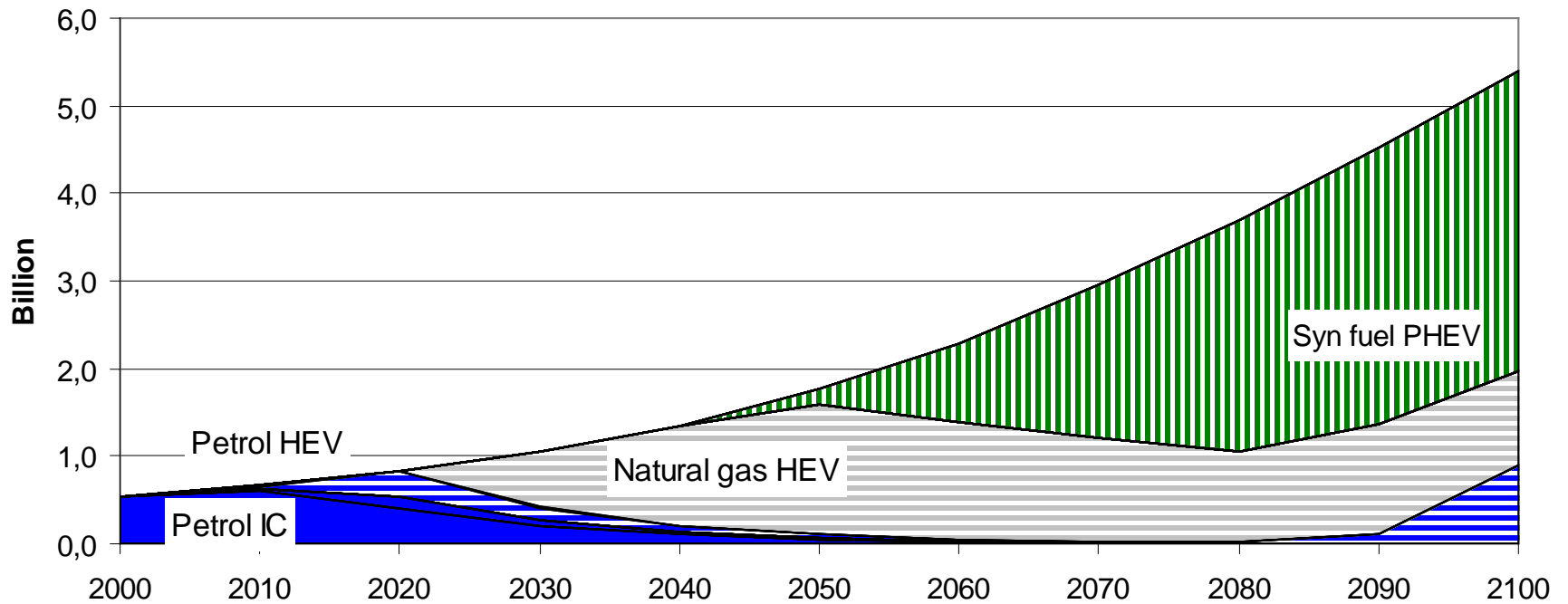
Industrial process heat



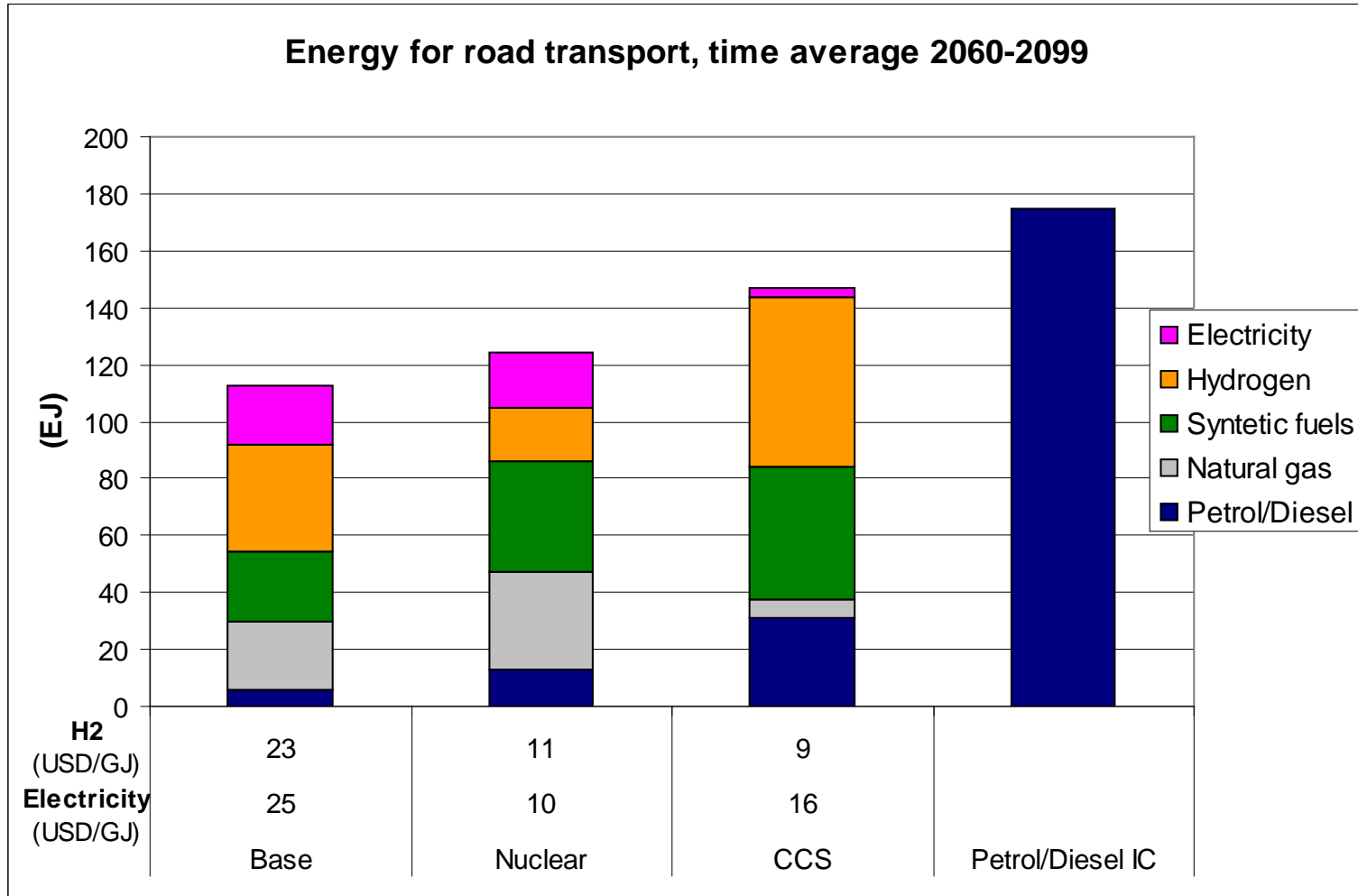
# District heating in Sweden



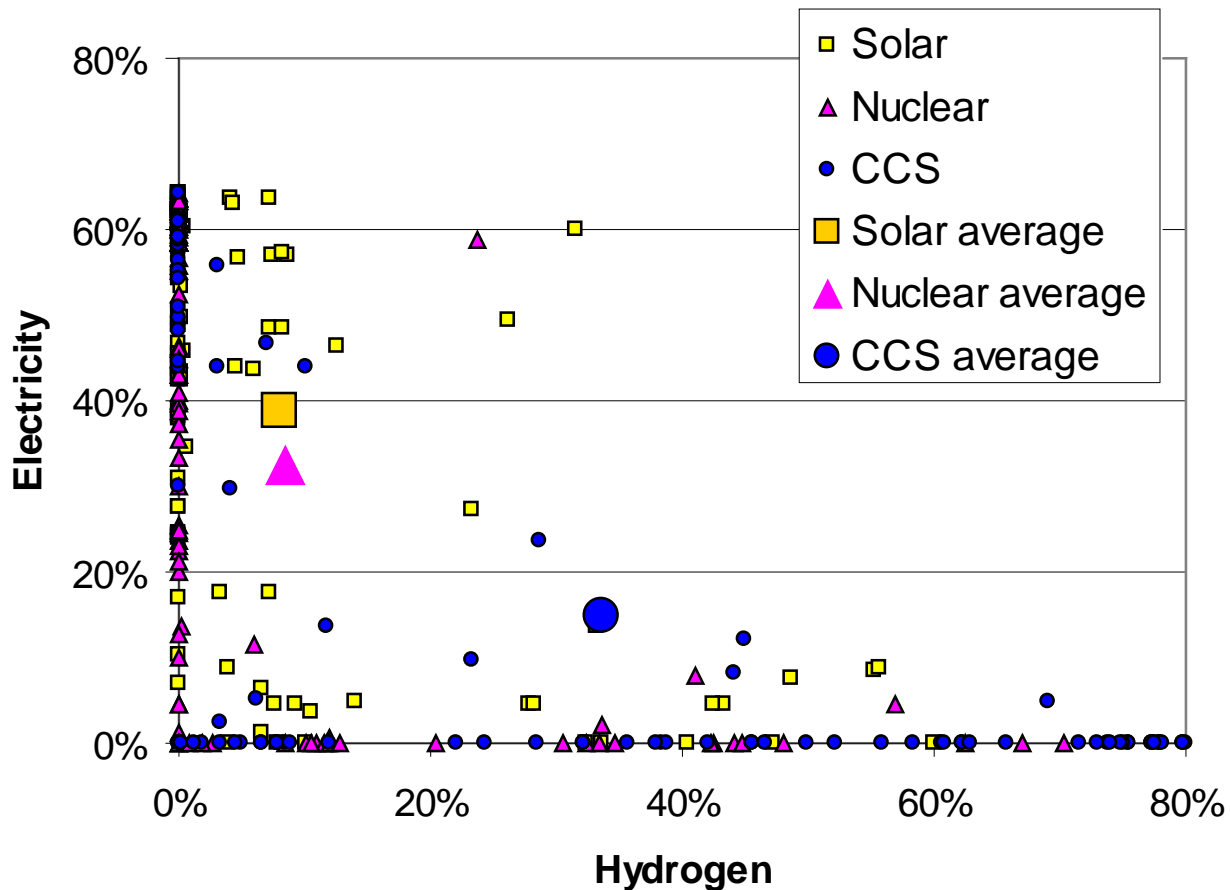
**Number of cars**  
**Energy system dominated by thermal solar energy, 400 ppm scenario**



# What determines which cars that are cost-effective?



### Monte Carlo analysis of vehicle costs





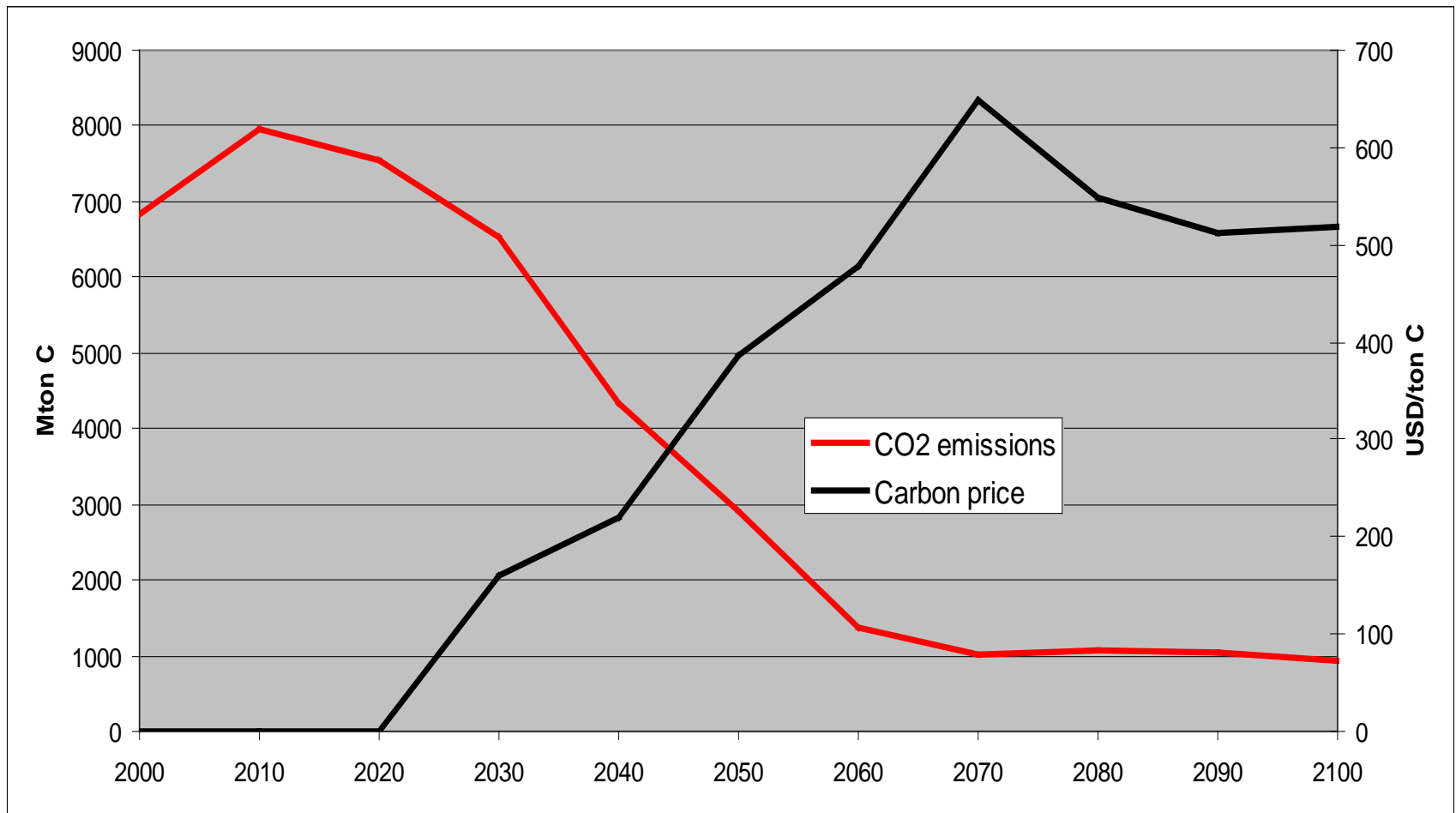
# Marginal abatement cost

- Shadow price of emissions
- Inflate with discount rate

$$M(t) = m(t)(1 + r)^{t-1}$$

- $M(t)$  carbon tax in net present value
- $m(t)$  shadow price generated in the model

# Carbon emissions and carbon price



# What does this model do?

- Predict (what will happen in the future)
- Prescribe (how ought the future look like)
- Describe (how does the energy system work)

# Summary

- Energy system models can
  - Give guidance on how we ought to develop the energy system
  - Give better understanding of good use of scarce resources
  - Give estimates of the cost of stabilizing the carbon emissions