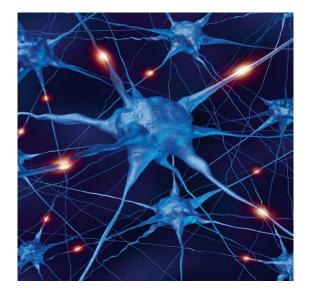
#### **Understanding Big data & Big systems**

Holger Rootzén, Mathematical Sciences



We all know that it is happening – but it still is hard to fathom how fast it will revolutionize our world:

Library of congress contains more than 96 miljon books and 100 terabyte



 $(100x10^{12})$  data. In 2013 a miljon times more will be created, and in 2023 100 times more – and it will be only a mouseclick away

The internet has more than 3 billion users; the worlds telphone networks connect 6 billion mobile phones; physics experiments become bigger and bigger; systems for making astronomical measurements are fantastically sophisticated and complicated.

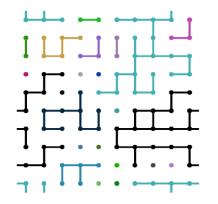
Natural systems – as we see them in larger and larger resolution – exhibit more and more details and complexity

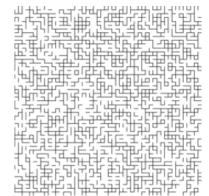


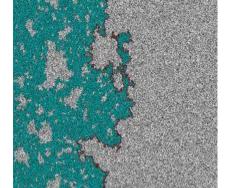
# more abstraction more generality

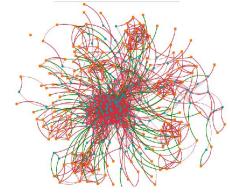
## more mathematics

## percolation



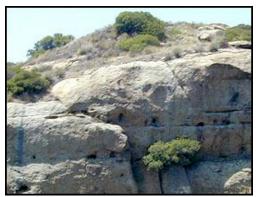






#### Simple local rules lead to complicated system behavior System behavior informs about local rules

#### Helps understanding of



water flow through porous rocks



through gels

## Big data and Big systems affects the lives of all of us (and of our children)



#### past

#### future

see advertizements in newspapers, TV, billboards

on web, choosen just for you



cost of insurance

accident rates of "your group" + your own accidents this + your internet trail: Facebook, Instagram, Twitter, blogs, ....

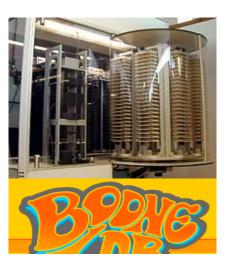


get credit

credit behaviour of "your group" + your own credit history this + your internet trail: Facebook, Instagram, Twitter, blogs, ....

Nothing is ever forgotten

good or bad??







### Some things we do:

*understand 27 millon p-values* from a study of interaction between pairs of genes in yeast, coming from 27 million experiments in 4 replications

*understand how huge datasets* from weather satellites, buoys, weather stations, and sensor systems can improve safety and efficiencey of marine transports

understand traffic accidents from a naturalistic driving study where 2000 cars equipped with web cams, radars, gps-s, sensors are driven in normal traffic for 3 years by drivers like you and me, and all data is saved

### Traffic accidents

- 1.3 miljon deaths/year worldwide, 20-50 million severely injured
- Large economic losses
- Less than 1 death/day in Sweden now. Down from 3 deaths/day a few decades ago – at a time with much less traffic
- First simple measures: seatbelts, helmets, follow traffic rules, drunk driving laws, ..., then more sophisticated ones: rebuild roads, better tires, improve driver education, airbags, ..., then next level of sophistication: more driver training and retraining, ABS, ESP, ..., and ??

Naturalistic driving studies: cars with drivers like you and me are instrumented with video cameras, radar, GPS, sensors for steering wheel movement, gas- and brake pedal movement,



...

Generates extremely large data sets – and give completely new opportunities for preventing traffic accidents

Accidents are extreme events – same methods as those for financial risks and for natural catastrophes (later in talk!) can be used

## New and exciting area for statistics

Selection bias/errors Risk estimation

Active safety systems for next generation cars. Important for competition with other car makers and for safety (?)

Driver training, traffic laws, ...

## Visual behavior/censoring

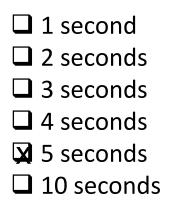
How much do you look off road while driving?

lacksquare 5% of the time

10% of the time

- 🛛 15% of the time
- 20% of the time

There is a 1 in 1000 chance that the lengths of an off road glances is longer than

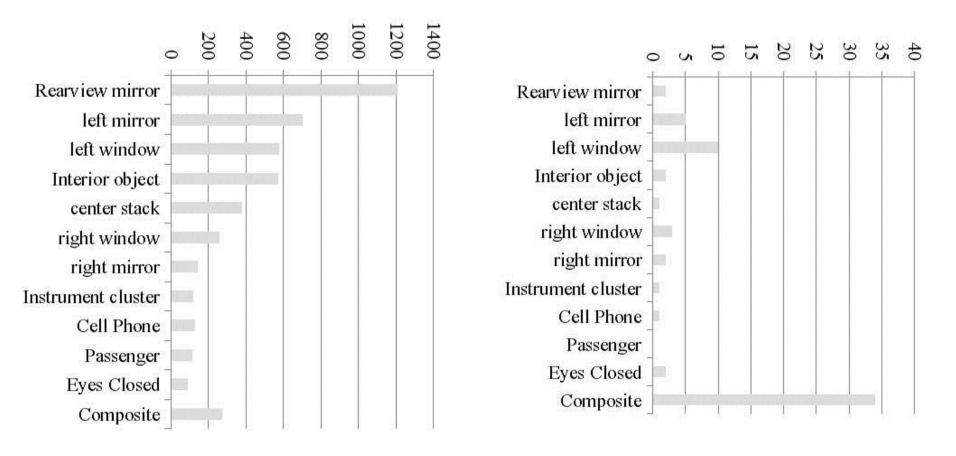


Is glance behavior different in different circumstances?

Not well understood

## Glance behavior in the 100-car study

Raw data: 19,616 annotated 6-second intervals from 100-car study: 4582 with 1 or more off road glances



Glances shorter than 3 seconds

#### Glances longer than 3 seconds

#### My research this week:

How should one use window censored observations of 0-1 processes to find the tail behaviour of the distributions of lengths of 0intervals (= off road glances)?

#### **One conclusion**

different kinds of nearcrashes and crashes; naturalistics driving studies; vehicles; drivers, all lead to different kinds of

- Selection bias
- Crash proximity measures
- Driver behavior and "covariates"

#### All require separate careful analysis

No omnibus answer to "is there selection bias in choice of near-crashes or the estimation of driver characteristics"

## The next step: SHRP 2

- 2000 cars
- 3 years
- Much better instrumentation (?)
- Started a year ago

## Some more things we do

## Catastrophes

#### Not now

Normal statistics: uses typical values, helps make life longer, feed the world

#### Now

- Extreme value statistics: only uses extreme observations, helps avoid floods, bridges collapsing, increase safety of cars, ships, airplanes, understanding of climate
- The wonderful and useful generality of mathematics and statistics



September 15, 2008 New York August 29, 2005 New Orleans

All the time everywhere 1,3 milj dead/year

### **Nassim Taleb: Black swans**

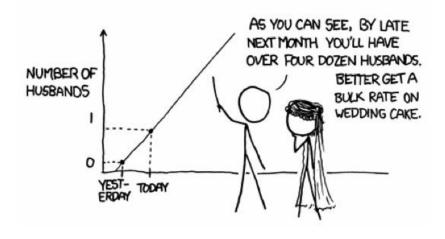


Cygnus atratus

- Rare: Have not occured before
- Extreme consequences
- Unpredicatable before, easy to predict after they have happened
- Shape history

Taleb (approximately): History is shaped by black swans – so not worth your while to try to manage risks

### Taming grey swans with statistics



Not (good) statistics

Statistics: to find stable patterns which have happened many times, and which one believes (sometimes because of lack of better knowledge) will continue to repeat themselves

### Stable patterns $\rightarrow$ statistical distributions

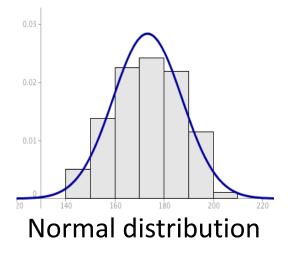
ightarrow shapes of possible distributions

## Statistics

**Matematics** 

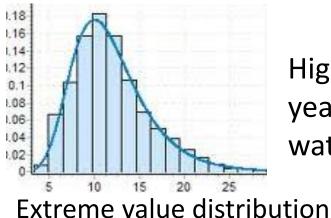
 $\rightarrow$  choice of specific distribution (with uncertainty)

Distribution → quantifies risk



Error in the measured distance = sum of many small measurement errors





Highest water level during year = maximum of daily water levels

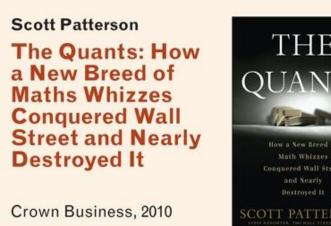


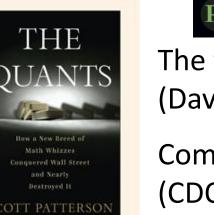
#### Statistics can tame swans if

- One has realized they exist
- One has enough data
- There are sufficiently stable patterns in data and the patterns continue to repeat themselves in the future

**Then** statistics can help judging: "How big is the risk?" -- and what types of catastrophes are most likely (how to handle the risk then depends on the situation)

*If not* then statistics cannot help





 $Pr[\mathbf{T}_{A} < 1, \mathbf{T}_{B} < 1] = \boldsymbol{\varphi}_{2}(\boldsymbol{\varphi}^{\text{-1}}(\mathbf{F}_{A}(1)), \boldsymbol{\varphi}^{\text{-1}}(\mathbf{F}_{B}(1)), \boldsymbol{\gamma})$ 

The formula that broke Wall street (David Li's formula)

Complicated credit insurance contracts (CDO-s) were valued by Li's formula Contributed to starting financial crisis

- **Opinion 1**: Matematics contributed to starting the financial crisis. Ergo forbid financial mathematics!
- Opinion 2: Matematics contributed to starting the financial crisis. Ergo develop better financial mathematics!

The world has chosen Opinion 2 and implements new mathematics based regulation of banks and insurance companies (e.g. Basel III, Solvency 2)

What do you think?

#### Megastort skadestånd för Weavering-blåsning Dagens industri 2011-09-02 08:23 Weavering Capital Founder charged with fraud The Guardian 2012-12-14

"Weavering Capital-härvan: Magnus Petersons, den svenske grundarens, styvfar och bror döms att solidariskt betala ett skadestånd på 700 miljoner kronor. "Det är fruktansvärt mycket pengar", säger brodern Stefan Peterson. Men det är inte Stefan Petersons inblandning i Weaverings svenska del som nu straffar sig.

Det var i mars 2009 som skandalen kring Weavering Capital, och den svenske grundaren till det brittiska fondbolaget Magnus Peterson, briserade. … Trots den turbulens som följde efter Lehman Brothers-kraschen hösten 2008 såg Weaverings fond ut att klara sig oförskämt bra. Men fondens värde misstänks ha blåsts upp av internaffärer och med hjälp av ränteswappar. Det mesta var dock luft. Sammanlagt uppges Weavering ha förvaltat omkring 5 miljarder kronor, men en stor del av de pengarna misstänks vara försvunna. … I en domstol på Caymanöarna föll i fredags en dom mot Magnus Petersons 85-årige styvfar och bror. Den senare var chef för det svenska dotterbolaget Weavering Capital, ett av dotterbolagen till det brittiska bolaget."

"Hedge fund boss Magnus Petersen charged with six offences after three-and-a-half year investigation by Serious Fraud Office. ... " investigation first closed and then reopend.

## Court demands 10 years of accounts from Weavering Capital boss

Magnus Peterson – the \$600 million hedge fund leader facing a criminal prosecution for alleged fraud – has 10 weeks to provide a personal asset trail to forensic investigators at liquidators Duff & Phelps.



At an unrelated hearing at the High Court last week, the founder of Weavering Capital UK was instructed by deputy chancery master Roger Bartlett to provide a list of all transactions over £2,000 for him and his wife, Amanda, dating to 2003.

In a trial scheduled for October 2014, Peterson faces criminal charges of forgery, fraudulent trading and false accounting, brought by the Serious Fraud Office. He has not yet made a plea and has

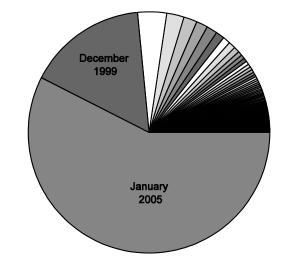
not issued any comment through a lawyer as he is representing himself.

Peterson was declared bankrupt in 2012 after the High Court handed down a \$450 million judgment against him and three other senior executives at Weavering Capital UK, which was the UK-based manager for the Cayman Islands Weavering Macro Fixed Income hedge fund.

The Petersons are due to leave the family home they share with their four children at the end of next month in order to settle debts from an earlier High Court case, Amanda Peterson said in court. This is unconnected with next year's fraud case.

#### Financial News, Nov. 26, 2013





Before GudrunAfter GudrunWindstorm Gudrun, January 2005

SEK 2,8 billion loss (LF) 55% of total loss 1982-2005

Analysis based on data 1982-1993: 1% chance biggest damage next 15-year period will be more than SEK 2,5 billion

#### ???

Analysis basered on data 1982-2005: 10% chance biggest damage next 15-year period will be more than SEK 7 billion (this time we didn't miss damage to forrest – but did we miss something else?)

Pandemics: the SARS Timeline Cristl Donnelly, Imperial College

(slides adapted from one of her presentations)

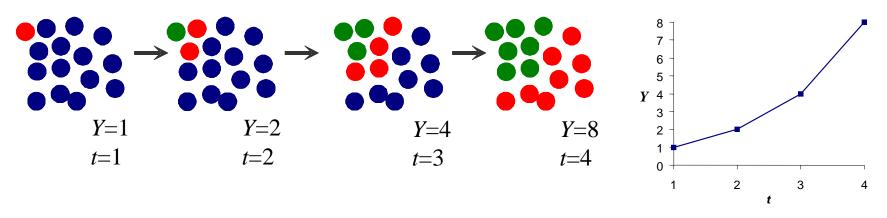
- 16 Nov 02 a case of atypical pneumonia, ۲ Guangdong.
- 26 Feb 03 cases of unusual pneumonia, Hanoi •
- Facemasks ripped off as HK dropped from SARS list
- 10 Mar 03 Dr Carlo Urbani reports an unusual outbreak of the illness he ۲ calls sudden acute respiratory syndrome (SARS) to WHO.
- 11 Mar 03 outbreak of mysterious respiratory disease in Hong Kong. ٠
- 12 Mar 03 WHO issues a global alert about SARS. ٠
- 15 Mar 03 WHO issues a heightened global health alert after cases in ۲ Singapore and Canada.

#### Act now $\rightarrow$ close down (parts of) countries, stop air travel

**Don't act** → **cause millions of deaths** ("only" 775 for SARS)



- Pandemics spread through contact between individuals
- 'Chain reaction' gives (initial) exponential growth

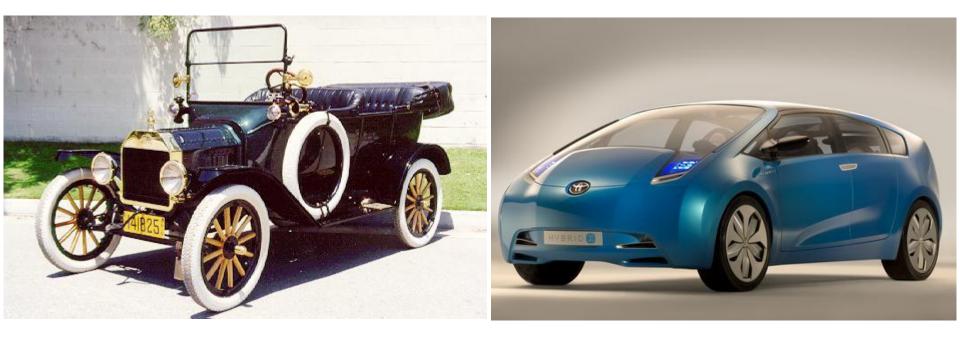


*R* = reproduction number = # of secondary infections caused by one primary case at the start of an epidemic.

#### is R big, in particular >1?

**The key is international coordination:** better decision systems, better reporting, better (and faster!) data processing, better understanding – and better communication with the public

## Total Quality Management Continuous Improvement (Also for the finance sector?)



Ford, model T, 1908

Toyota Prius, concept

### **FMEA – Failure Modes and Effects Analysis**

Systematic approach to identifying and diminishing risks

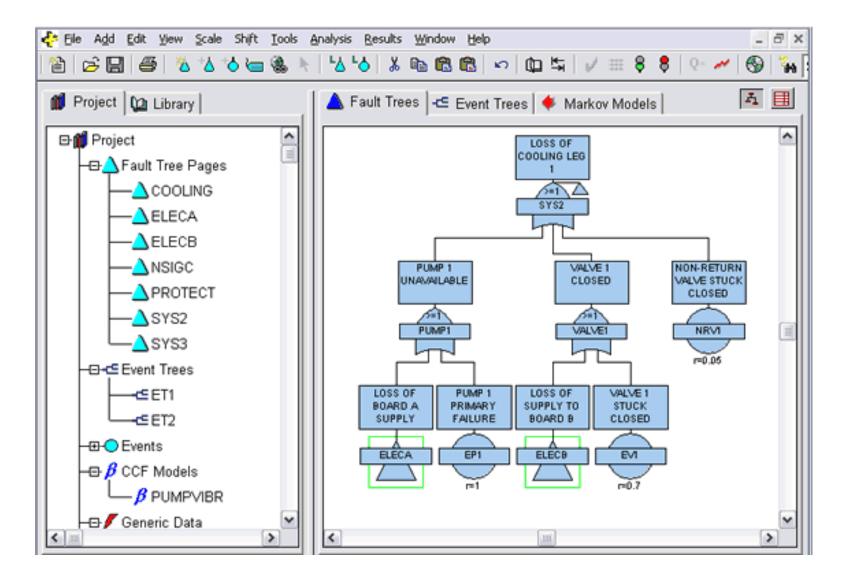
Subcomponent/ Subsystem	Component ID	Component Fail Rate	Failure Mode	Alpha	Failure Effects		Failure	Mitigation	Severity	Maintenance
					Local	End	Detection Method	-	Class	Action
Hoist Motor and Gearbox	MFPH- Hoist Motor 3 HP & Gearbox	5.5E-06	Motor fails to start/run	1.00	Cannot raise or lower Tube Plug by motor	Shutdown for repairs ~24 hours	Status light indicator	Use of handwheel for manual application	III	Replace
	BFPH - Tube Plug Hoist Brake	1.15E-05	Fails	1.00	Potential for tube plug drop (see note)	Shutdown for repairs ~24 hours. If tube plug drops then shutdown n > 1 week.	None	None	III (II if plug drops	Replace
	PHOL - Tube Plug Hoist Brake Overload Switch EB33056-16	4.12E-06	Fails Open	.98	Motor will not run	Shutdown for repairs ~8 hours	Status light indicator	Manual handwind	IV	Replace

working group with broad and diverse background – leader – data – training – plan work – brainstorm – take notes – everyone responsible – systematic judgment of likelihoods; consequences; countermeasures – someone responsible for implementing results

#### Systematic < Creative

Seriously and well thought through for many different kinds of FMEA-s

## FTA – Fault Tree Analysis PSA – Probabilistic Safety analysis



#### **Used for**

• Estimating probabilities



• Identification of important risks

#### FMEA: Bottom up, simple systems

#### FTA: Top down, redundant system

#### **Tools for continuous improvement**

## (but unstructured thinking about risks is also needed)

#### A Single Number Can't Hedge Against Economic Catastrophes

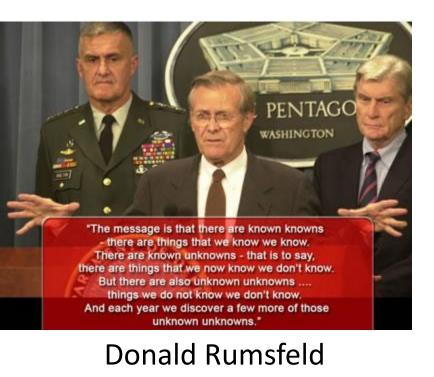
Mathematics and statistics have transformed day-to-day trading in the world's financial markets. This has led to new ways to reduce (or "hedge") risks, which provide an important service to society, but also a temptation to very big gambles, with a potential for extreme losses. This paper discusses some of the ways statistics and mathematics can be used to understand and protect against very large, "catastrophic" financial risks. We argue that means don't mean anything for catastrophic risk, that separate large financial risks often are better handled by separate companies, and that the mathematical aspects of risk can't be summarized into one number. We also believe that there is a large potential for improved risk management in financial institutions, where extreme value theory, a speciality of the present authors, may be a useful tool. Improvements, however, will not come for free, but require long and hard work, where mathematics is only one part of the total effort.

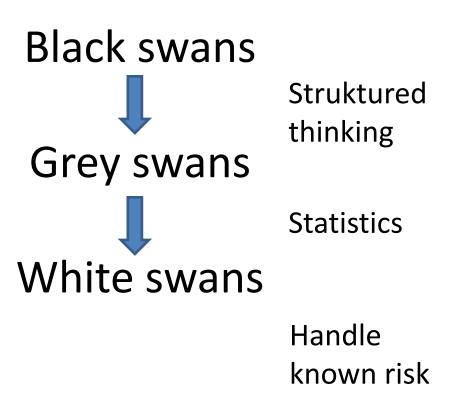


Figure 1. Long-term sickness? Reprinted from the *Economist* (3), with permission of the artist, D. Simmonds.

#### My own point of view

All risks must be handled as well as can be done – and if you don't handle the small risks, then the big risks become uniteresting! If possible, risk handling should be quantitative, otherwise qualitative (and, don't spend so much effort on "known unkowns" that you forget "unknown unknowns")





## Many small changes together lead to dramatic results



Rome10.000 years ago

Rom now

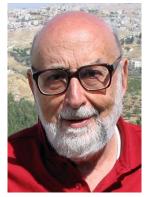
Mankind's total transformation of our earth has occured in very many small steps

#### **Nobel prize in Physics 2013**





#### Peter Higgs



# Which is most Important?



## CERN: thousands of researchers

Francois Englert

## **Climate change**

## slow down, stop mitigate

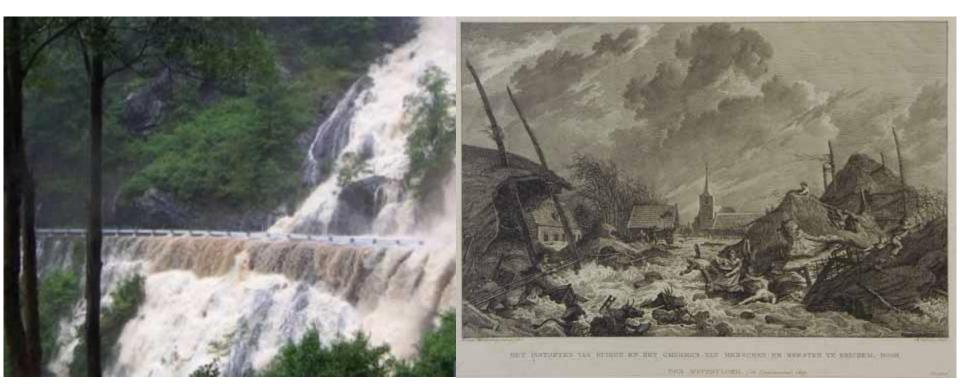
### **Extreme climate**

Make dyke 1.5 m higher

 $\rightarrow$  costs billions of Euros, popular protests

Keep dyke as is

 $\rightarrow$  (perhaps) thousands of deaths





Riktlinjer för bestämning av dimensionerande flöden för dammanläggningar

Nyutgåva 2007



"Dammanläggningar som dimensioneras enligt flödesdimensioneringsklass II ska vid dämningsgränsen kunna framsläppa ett tillrinnande flöde med en återkomsttid av minst 100 år."

Climate change: the standard method above doesn't work any more, one has to specify

- Design life period (e.g. 2015-2115)
- Risk (e.g. 5% probability of a flood during this period)

#### → Design life level

*First* convince engineering and political community that this has to be done, *then* the rest is climate modelling and (extreme value) statistics

(*But* science and statistics is only one part, one has to develop new and much more flexible and adaptive approaches to design)

Design Life	Prob.	Design Life Level	Return Level	EWT	EWT
			(2015 climate)		(trend stopped)
2015-2064	0.05	11.5	10.9	251	788
2015-2064	0.01	15.2	14.4	431	3839
2065-2114	0.05	12.6	10.9	262	1008
2065-2114	0.01	16.6	14.4	453	5002

Return levels are for T = 975 and T = 4975, respectively. EWT is expected waiting time

# Estimation of the distribution of maximal inclusion sizes in clean steels, from measurements on planar sections

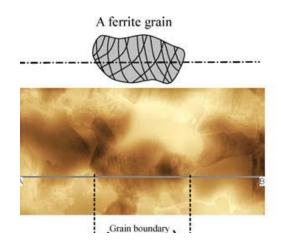
Fatigue: metal specimens subjected to varying stresses develop cracks and eventually break --- the major cause ofmechanical failure

Fatigue limit: if stresses are lower than this limit, cracks stop growing and the specimen doesn't break

Murakami's theory: fatigue limit is determined by the square root of area of the largest inclusion, measured on the projection perpendicular to the direction of stress

measurements: on polished planar sections, size of square root of area of sections of cut inclusions,

- Peaks over Thresholds measurements
- Area Maxima measurements,



choice depends mainly on experimental convenience and habit

**model:** inclusions are spheres, centers 3-d Poisson process in the specimen, 2-d sectional sizes (=diameters) exponential (PoT) or Gumbel (AM)

aim: distribution of maximal diameters of 3-d spheres, in bigger volumes, streamlined methods for engineering use