

Formelblad för TMV036c och MVE350, 14/15

Trigonometri.

$$\cos(x+y) = \cos(x)\cos(y) - \sin(x)\sin(y)$$

$$\sin(x)\cos(y) = \frac{1}{2}(\sin(x-y) + \sin(x+y))$$

$$\sin(x+y) = \sin(x)\cos(y) + \cos(x)\sin(y)$$

$$\tan(x+y) = \frac{\tan(x) + \tan(y)}{1 - \tan(x)\tan(y)}$$

$$\cos(x)\cos(y) = \frac{1}{2}(\cos(x-y) + \cos(x+y))$$

$$\cos(2x) = \cos^2(x) - \sin^2(x)$$

$$\sin(x)\sin(y) = \frac{1}{2}(\cos(x-y) - \cos(x+y))$$

$$\sin(2x) = 2\sin(x)\cos(x)$$

Integralkatalog

$$\int x^a dx = \frac{x^{a+1}}{a+1} + C, \quad a \neq -1$$

$$\int \frac{1}{x} dx = \ln|x| + C$$

$$\int \sin x dx = -\cos x + C$$

$$\int \cos x dx = \sin x + C$$

$$\int \frac{1}{\cos^2 x} dx = \tan x + C$$

$$\int \frac{1}{\sin^2 x} dx = -\cot x + C$$

$$\int e^x dx = e^x + C$$

$$\int a^x dx = \frac{a^x}{\ln a} + C, \quad 0 < a \neq 1$$

$$\int \frac{1}{x^2 + a^2} dx = \frac{1}{a} \arctan \frac{x}{a} + C, \quad a \neq 0$$

$$\int \frac{f'(x)}{f(x)} dx = \ln|f(x)| + C$$

$$\int \frac{1}{\sqrt{a-x^2}} dx = \arcsin \frac{x}{\sqrt{a}} + C, \quad a > 0$$

$$\int \sqrt{a-x^2} dx = \frac{1}{2}x\sqrt{a-x^2} + \frac{a}{2} \arcsin \frac{x}{\sqrt{a}} + C, \quad a > 0$$

$$\int \frac{1}{\sqrt{x^2+a}} dx = \ln|x + \sqrt{x^2+a}| + C, \quad a \neq 0$$

$$\int \sqrt{x^2+a} dx = \frac{1}{2}(x\sqrt{x^2+a} + a \ln|x + \sqrt{x^2+a}|) + C$$