
Optimization of maintenance planning at Volvo Aero Corporation (VAC)



Fraunhofer

CHALMERS

Research Centre

Industrial Mathematics

Ann-Brith Strömberg

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Background

Maintenance of aircraft engines is expensive:

- *spare parts* cost up to 2 Mkr
- *total cost* for maintenance of a jet engine: 15-30 Mkr
- *rent* for a spare engine: 15 kkr/day

Opportunistic maintenance:

At each maintenance occasion, possible to *replace more components than* what is absolutely *necessary*

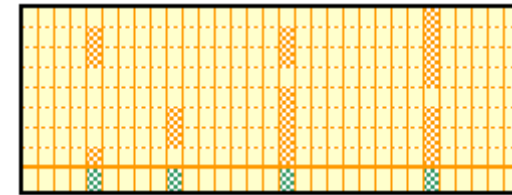
⇒ totally fewer maintenance occasions

⇒ totally lower cost



The purpose of the project

- Create a *methodology* that generates good *replacement schedules* for components in aircraft engines
- Consider:
 - *Life time restricted* and "*on condition*"-components
 - *Fixed cost* when an engine/module is taken to the workshop
 - *Work costs* to set free engine modules and components
 - Utilize a *store* of used components
- *Minimize total flight hour cost* during the contract period



An optimization model for the whole contract period

- For each component i in the module:
 - *Cost* for a new component: c_i
 - *Life* of a new component: T_i
 - *Remaining life* of current component: τ_i
- *Contract period* divided into T *time periods* $t = 1, \dots, T$
(a' 50 flight hours)
- Maintenance possible at start of each time period (*discrete time steps*)
- A *fixed cost* per maintenance occasion: d

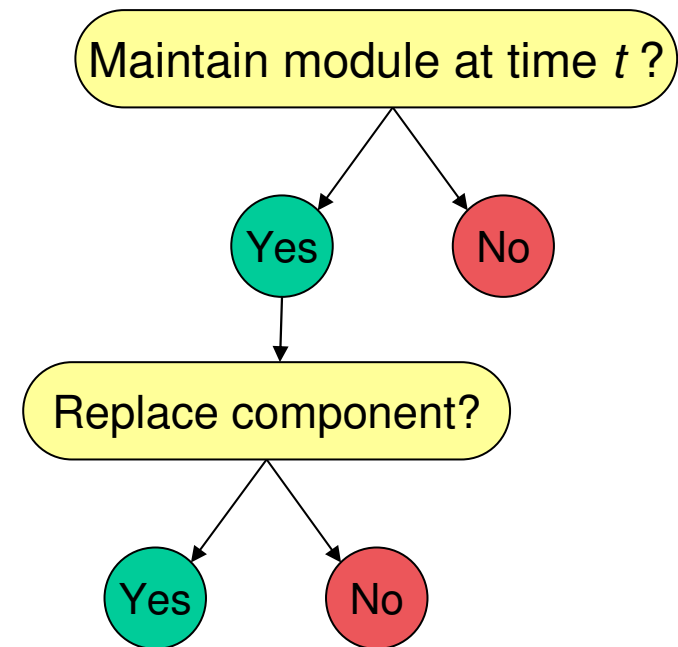


A mathematical optimization model for maintenance planning of a module

Definition of variables

$$z_t = \begin{cases} 1 & \text{if the module is maintained at time } t \\ 0 & \text{otherwise} \end{cases}$$

$$x_{it} = \begin{cases} 1 & \text{if component } i \text{ is replaced at time } t \\ 0 & \text{otherwise} \end{cases}$$



Basic mathematical model: one module, N parts, T time steps

$$\text{minimize } \sum_{t=0}^{T-1} \left(\sum_{i \in N} c_i x_{it} + dz_t \right)$$

$$\text{subject to } \sum_{t=0}^{\tau_i} x_{it} \geq 1, \quad i \in N, \quad \text{replace part before its remaining life is over}$$

$$\sum_{t=l}^{T_i+l-1} x_{it} \geq 1, \quad l = 1, \dots, T - T_i, \quad i \in N, \quad \text{replace part at least once in a lifetime}$$

$$x_{it} \leq z_t, \quad t = 0, \dots, T - 1, \quad i \in N, \quad \text{replace part only at maintenance occasion}$$

$$x_{it} \in \{0, 1\}, \quad t = 0, \dots, T - 1, \quad i \in N,$$

$$z_t \in \{0, 1\}, \quad t = 0, \dots, T - 1.$$

- $x_{it} \in \{0, 1\}$ can be relaxed to $x_{it} \geq 0$

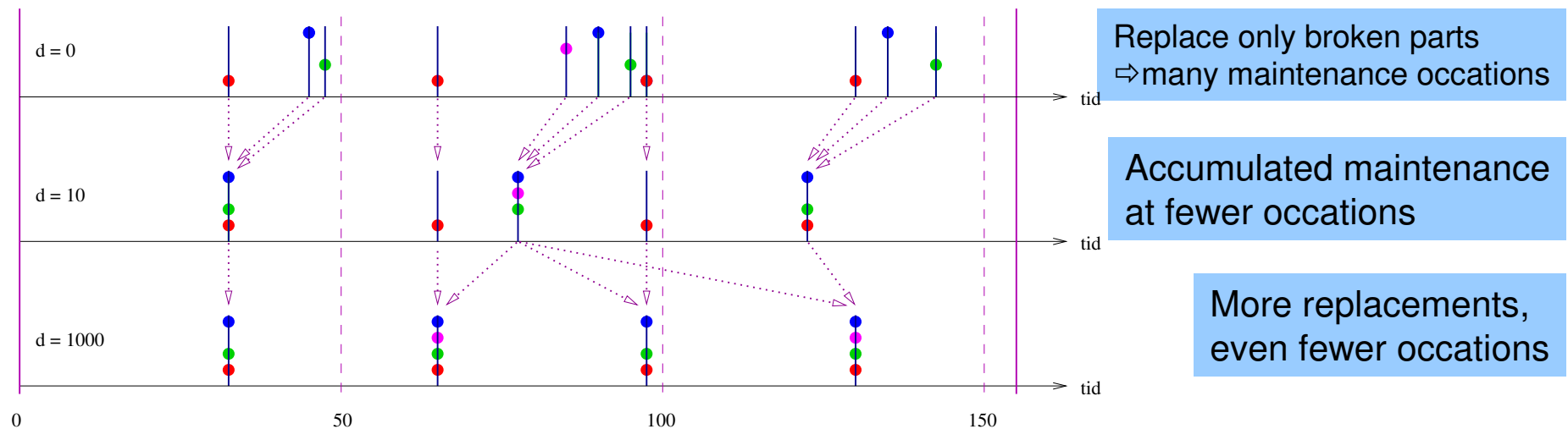
Integrality property (TU)!



Costs for spare parts vs. fixed maintenance costs

d = fixed cost per maintenance occasion (inspection, transport, admin, ...)

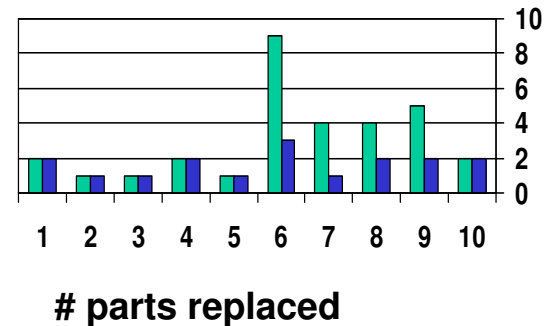
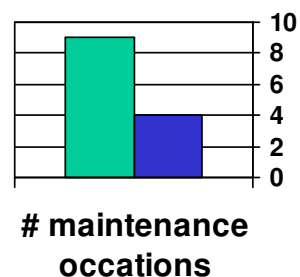
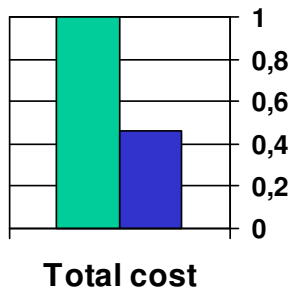
Optimal maintenance plans for 3 levels of the fixed cost



Comparison of the methods

- An engine module with 10 components
- Only life time restricted components

- Value policy
- Optimization



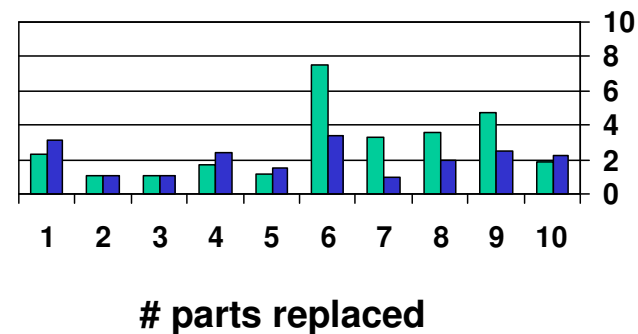
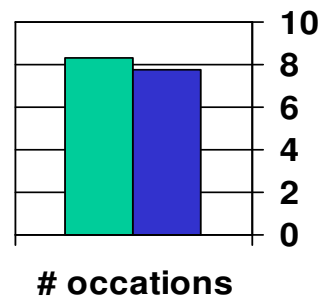
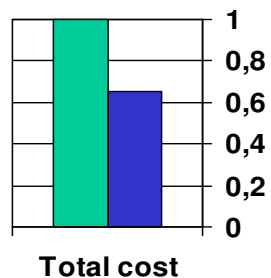
Comparison of the methods using stochastic simulations

- An engine module with 10 components
- Parts 1, 4, 5, 6, 9, 10 are OC (Weibull)

Part no	1	4	5	6	9	10
β	2	2	4	4	6	6

- Value policy
- Optimization

- Average values from 200 scenarios



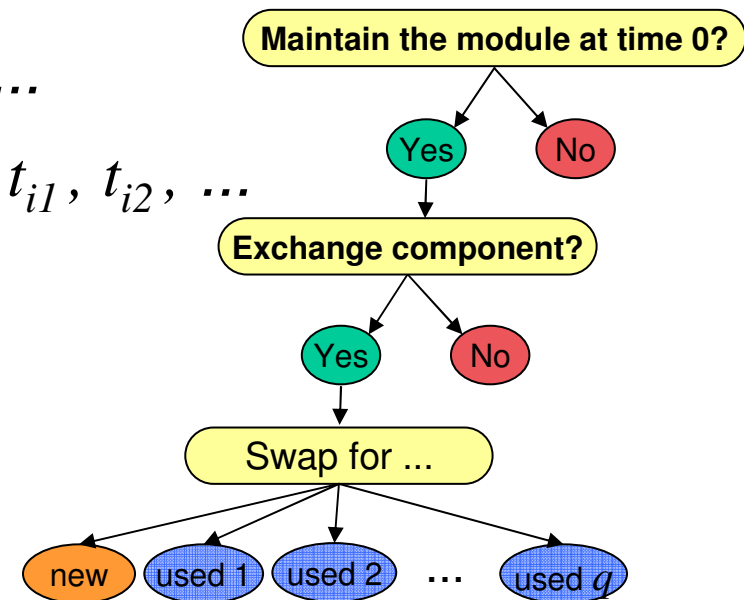
Conclusions from the simulations

- + Optimization \Rightarrow *always best plan w.r.t. cost (10-30% savings)*
- + Solution time typically a few CPU-seconds (one module)
- Compared also with
 - *"age policy"* (replace part older than a certain age limit, optimize age limits)
 - *"no method"* (replace only broken parts, not opportunistic)
 - + The optimization model is *best* also here
- + Optimization \Rightarrow *fewer maintenance occasions*

A store of used components

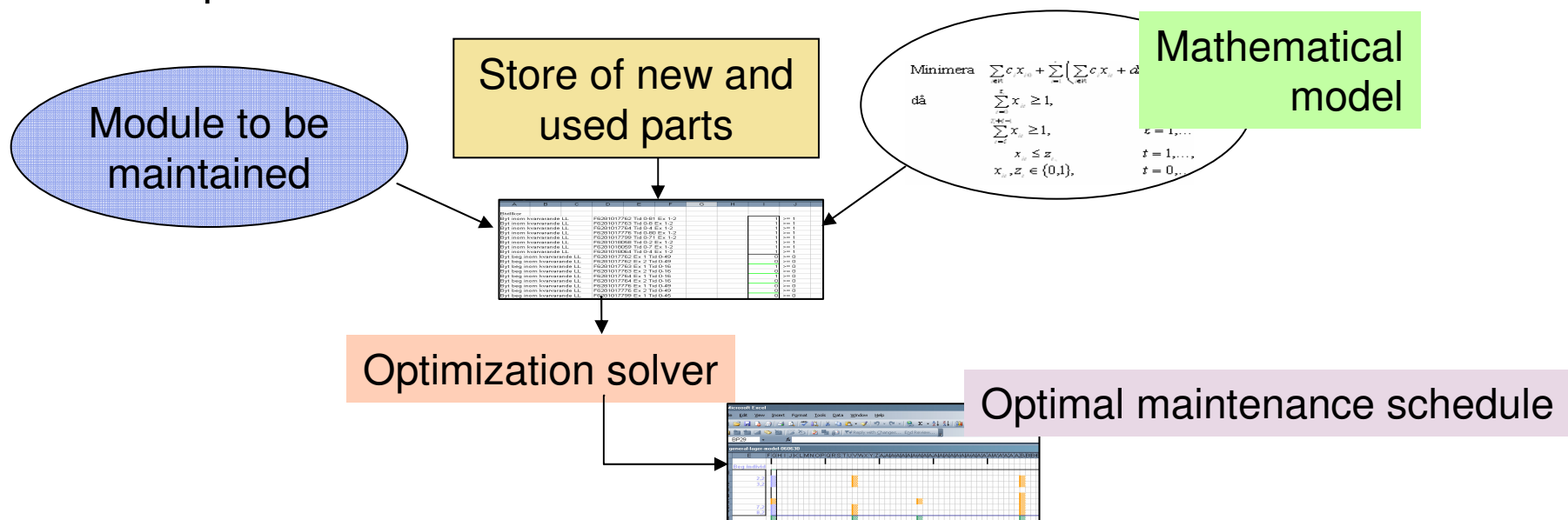
- For each part i in the module there is a *store of used components* at time 0 (at present maintenance occasion):
 - Costs* for used components: k_{i1}, k_{i2}, \dots
 - Remaining lives* of used components: t_{i1}, t_{i2}, \dots
- Additional variables:

$$s_{ij} = \begin{cases} 1 & \text{if used individual } j \text{ of component } i \\ & \text{from the store is used at time 0} \\ 0 & \text{otherwise} \end{cases}$$

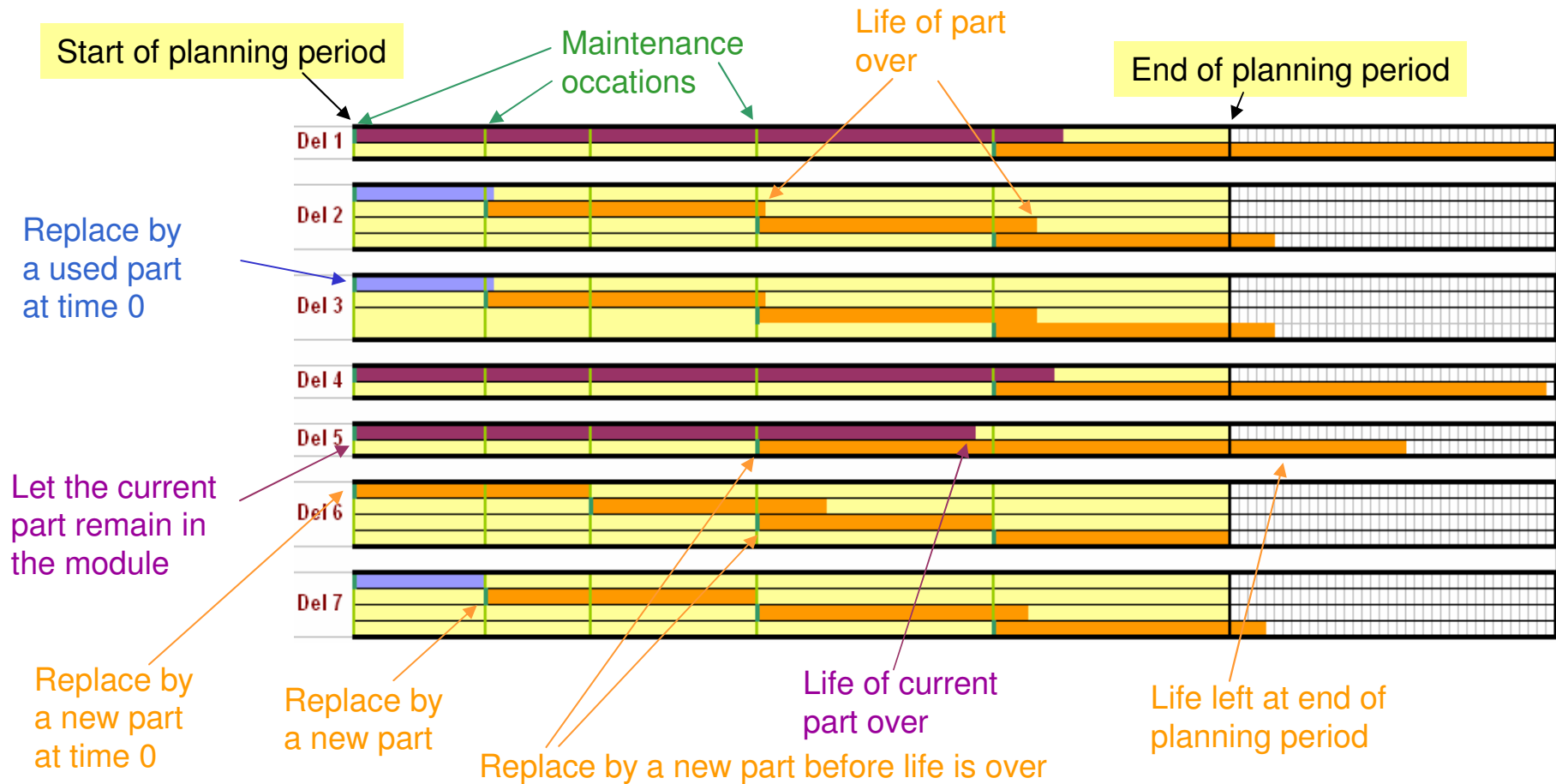


A tool for optimization and decision support at maintenance planning

- For one engine module and a store of new and used (at time 0) parts
- *Implemented in Excel* for input and presentation of results
- With Xpress-MP as IP solver

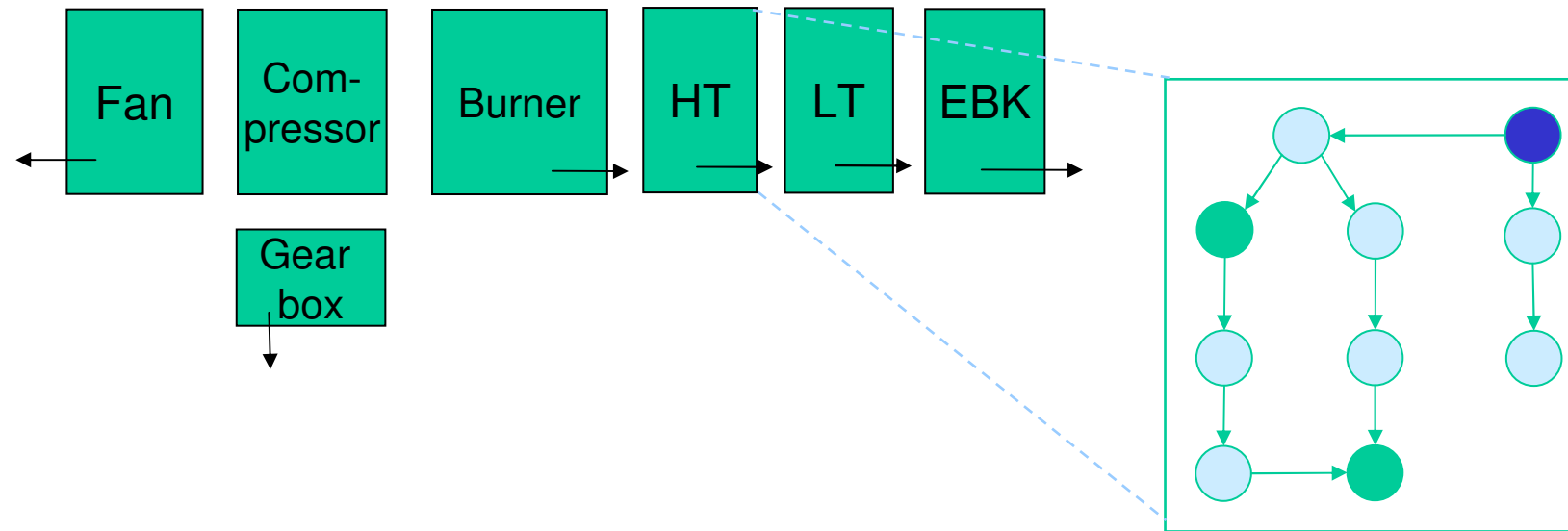


An optimal maintenance schedule for 7 components in an engine module



Several modules in an engine

- *Work costs* to *set modules free*
- *Work costs* to *set components free*



A model for a whole engine

Variable definition

$$x_{it}^m = \begin{cases} 1 & \text{if component } i \text{ in module } m \text{ is replaced at time } t \\ 0 & \text{otherwise} \end{cases}$$

$$y_{it}^m = \begin{cases} 1 & \text{if component } i \text{ in module } m \text{ is removed at time } t \\ 0 & \text{otherwise} \end{cases}$$

$$w_t = \begin{cases} 1 & \text{if the engine is maintained at time } t \\ 0 & \text{otherwise} \end{cases}$$

$$v_{nt} = \begin{cases} 1 & \text{if activity } n \text{ is done at time } t \\ 0 & \text{otherwise} \end{cases}$$

$$z_t^m = \begin{cases} 1 & \text{if module } m \text{ is maintained at time } t \\ 0 & \text{otherwise} \end{cases}$$



A model for a whole engine

Includes:

- *Costs* for several *work tasks*
- *Dependencies* between components – graph structure
- Possibility to *fix* certain *activities* in advance

$$\text{minimize } \sum_t \left(\sum_m \left(\sum_i \left(c_i^m \cdot x_{it}^m + a_i^m \cdot y_{it}^m \right) \right) + d_t \cdot w_t + \sum_n b_n \cdot v_{nt} \right)$$

$$\text{subject to } \sum_t z_t^m \leq T f_m \quad \forall M$$

$$\sum_{t=0}^{\tilde{T}_i^m} x_{it}^m \geq f_m \quad \text{if } (\tilde{T}_i^m \leq T-1), i \in N^m, \forall m$$

$$\sum_{t=l}^{T_i^m+l-1} x_{it}^m \geq f_m \quad l=1, \dots, T-T_i^m, i \in N^m, \forall m$$

$$\sum_{j \in \delta^m(i)} y_{jt}^m \geq y_{it}^m \quad i \in N^m, \forall m, \forall t$$

$$z_t^m \leq \sum_{n \in A^m} v_{nt} \quad \forall m, \forall t$$

$$v_{nt} \leq \sum_{n' \in A(n)} v_{n't} \quad \forall n, \forall t$$

$$x_{it}^m \leq y_{it}^m \leq z_t^m \leq w_t \quad i \in N^m, \forall m, \forall t$$

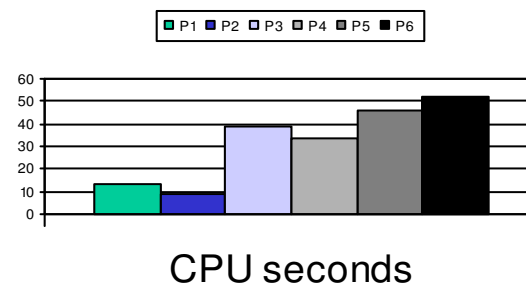
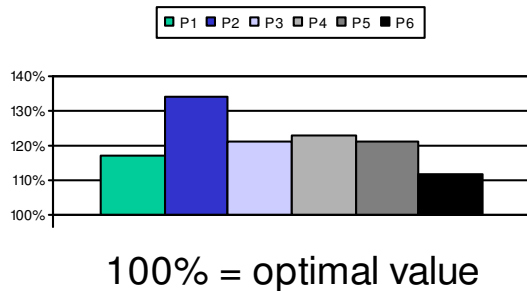
$$y_{it}^m, z_t^m, v_{nt} \in \{0,1\} \quad i \in N^m, \forall m, \forall n, \forall t$$

$$x_{it}^m, w_t \geq 0 \quad i \in N^m, \forall m, \forall t$$



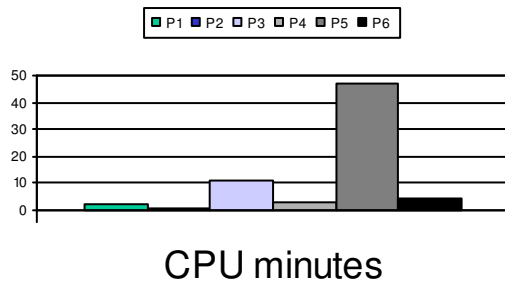
Results from initial tests for a whole engine

First maintenance plan

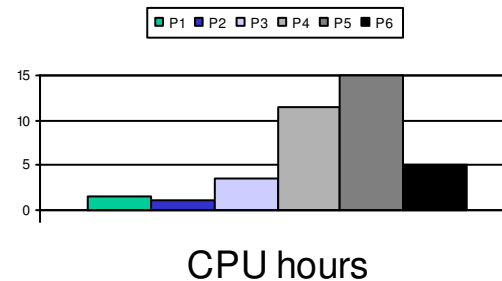


P1–P6: six models with different levels of inclusion of work costs

\leq optimal value + 10%



\leq optimal value + 5%



Model for a whole engine – several magnitudes harder than for one module



More ...

- Alternative *solution approaches*, decomposition methods:
- Solve the basic model very many times
 - Benefit from solving it efficiently
- Study the *structure* of the basic mathematical *model*
 - New formulations \Rightarrow significant *reduction of execution time*
- Tests are going on
 - Vary fixed costs and # time steps
 - Vary age of existing engine
 - How good is the first feasible solution found (for time 0)?

