

EQUILIBRIUM EQUATIONS

We give some hints on how to set up mathematical equations for chemical equilibrium problems.

0.1. **Chemical equilibrium.** Consider an elementary reaction of the form



Chemical equilibrium means that the rates of formation of the substances are zero:

$$0 = \frac{d}{dt}[\text{AB}] = -\frac{d}{dt}[\text{A}] = -\frac{d}{dt}[\text{B}] = -k_{11}[\text{AB}] + k_{12}[\text{A}][\text{B}],$$

so that

$$(2) \quad \frac{[\text{A}][\text{B}]}{[\text{AB}]} = K,$$

where the equilibrium constant is $K = \frac{k_{11}}{k_{12}}$, measured in the unit M = molar = mol/L. In order to use Newton's method we write the equation in the form

$$Kx_1 - x_2x_3 = 0,$$

or

$$x_1 - x_2x_3/K = 0,$$

where $x_1 = [\text{AB}]$, $x_2 = [\text{A}]$, $x_3 = [\text{B}]$.

0.2. **Solubility product.**



Here we cannot speak of the concentration of the solid AB and instead of (2) we have

$$[\text{A}][\text{B}] = K_{\text{sp}},$$

where K_{sp} is the solubility product with unit M². This leads to the equation

$$K_{\text{sp}} - x_2x_3 = 0,$$

or

$$1 - x_2x_3/K_{\text{sp}} = 0.$$

0.3. **Mass balance.** We need more equations. One possibility is to note that in (1) or (3) we must have

$$V([\text{AB}] + [\text{A}]) = A_{\text{tot}}$$

where V is the volume and A_{tot} is the total amount of A (mol) which may be known from the preparation of the experiment. If there are more reactions, and A appears in other forms, then the corresponding terms must be added into the mass balance.

0.4. **Charge balance.** Further equations may be obtained by counting the charges of the ions. For example, if AB is neutral and A positive and B negative, then

$$[\text{A}] - [\text{B}] = 0,$$

means that the solution is electrically neutral. If there are more reactions and other ions then more terms must be added in the charge balance equation.

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