

$$y'' + y = xE^x \sin(x).$$

$$y_p = (ax + b)e^x \sin(x) + (cx + d)e^x \cos(x)$$

$$\begin{aligned} y_p'' + y_p &= (ae^x \sin(x) + (ax + b)e^x \sin(x) + (ax + b)e^x \cos(x))' + (ce^x \cos(x) + \\ &(cx + d)e^x \cos(x) - (cx + d)e^x \sin(x))' + (ax + b)e^x \sin(x) + (cx + d)e^x \cos(x) = \\ &ae^x \sin(x) + ae^x \cos(x) + ae^x \sin(x) + (ax + b)e^x \sin(x) + (ax + b)e^x \cos(x) + \\ &ae^x \cos(x) + (ax + b)e^x \cos(x) - (ax + b)e^x \sin(x) + ce^x \cos(x) - ce^x \sin(x) + \\ &ce^x \cos(x) + (cx + d)e^x \cos(x) - (cx + d)e^x \sin(x) - ce^x \sin(x) - (cx + d)e^x \sin(x) - \\ &(cx + d)e^x \cos(x) + (ax + b)e^x \sin(x) + (cx + d)e^x \cos(x) = (2a + b - 2c - \\ &2d)e^x \sin(x) + (2a + 2b + 2c + d)e^x \cos(x) + (2a + c)xe^x \cos(x) + (a - 2c)xe^x \sin(x) = \\ &xe^x \sin(x), \end{aligned}$$

$$\begin{cases} 2a + b - 2c - 2d = 0 \\ 2a + 2b + 2c + d = 0 \\ 2a + c = 0 \\ a - 2c = 1 \end{cases}$$

$$\begin{cases} a = 1/5 \\ c = -2/5 \\ 6/5 + b - 2d = 0 \\ -2/5 + 2b + d = 0 \end{cases}$$

$$\begin{cases} a = 1/5 \\ c = -2/5 \\ b = -2/25 \\ d = 14/25 \end{cases}$$

$$\text{Svar: } y_p = (1/5x - 2/25)e^x \sin(x) - (2/5x - 14/25)e^x \cos(x).$$