

$$C_n = \sum_{m=1}^n C_{m-1} C_{n-m}$$

C_{m-1} possibilities

C_{n-m} possibilities

