

HOME TO THE LARGEST MULTI-BILLION DOLLAR CORPORATE ACCOUNTING FRAUD IN THE HISTORY OF OUR NATION

CLINTON, MISSISSIPPI -- FORMER CORPORATE WORLD HEADQUARTERS FOR WORLDCOM

my cube was approximately there

Kevin's office was right there

As the WORLDCOM turns.

CORPORATE CRIME. FBI INVESTIGATIONS. MASS LAYOFFS. LOSSES. MERGERS AND MORE...

MY JOB DESCRIPTION:
I started working at WorldCom in September of 1999. While I was there, I was the designer for their Corporate Intranet, which happened to be the busiest intranet site in the world. I also did graphics for the internet site as well. I quit my job soon after Quinn was born in February of 2002.

BITTER: Well, we lost it all! Kevin got laid off after working there for over 8 years!!! We had just bought a house, and had a baby!!! Not to mention I had just quit my job (at WorldCom) to be a stay-at-home mom! We both lost our ENTIRE 401k's and Kevin also lost hundreds of thousands of dollars in vested stock options. Times were tough!

SWEET: This is where we MET!!! This is where we worked when we got married and had our first child! This is where our life together began. So even though we lost all of our money, we gained ALL of those things that money just CANNOT BUY!! Like true love, a best friend, and family! I wouldn't trade this WorldCom experience for anything!!!!

KEVIN'S JOB DESCRIPTION:
Kevin started working at WorldCom when it was actually still LDDS. It's hard to just sum up ALL of what he did for them. He was there through over 60 mergers and acquisitions and played a major part in integrating the systems of all of the new companies. He was also over all of their Corporate Internet and Intranet Systems. Kevin was laid off from WorldCom in April of 2002, which was 2 months after I quit.

WORLDCOM
KIMBERLY SMITH
12/17/2008

WORLDCOM
Corporate
KEVIN CROTHERS

Financial Risk
4-rd quarter 2016/17
Tuesdays 13.15 – 115.00 and
Thursdays 15.15 – 17.00 in Euler

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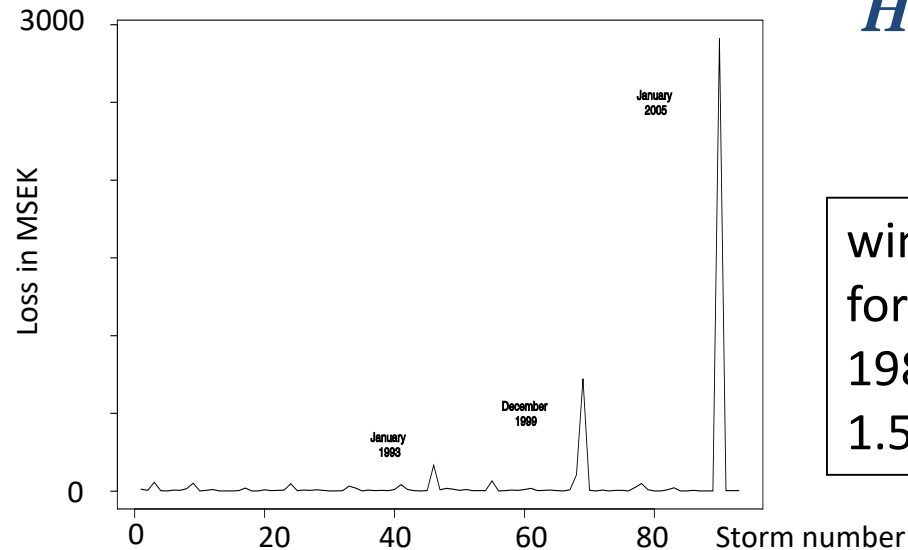


“As an alternative to the traditional 30-year mortgage, we also offer an interest-only mortgage, balloon mortgage, reverse mortgage, upside down mortgage, inside out mortgage, loop-de-loop mortgage, and the spinning double axel mortgage with a triple lutz.”



Gudrun January 2005
326 MEuro loss
72 % due to forest losses
4 times larger than second largest

The Peaks over Thresholds (PoT) method (*Coles p. 74-91, H&L p. 256-259*)



windstorm losses
for Länsförsäkringar
1982 – 2005: excesses of
1.5 MSEK

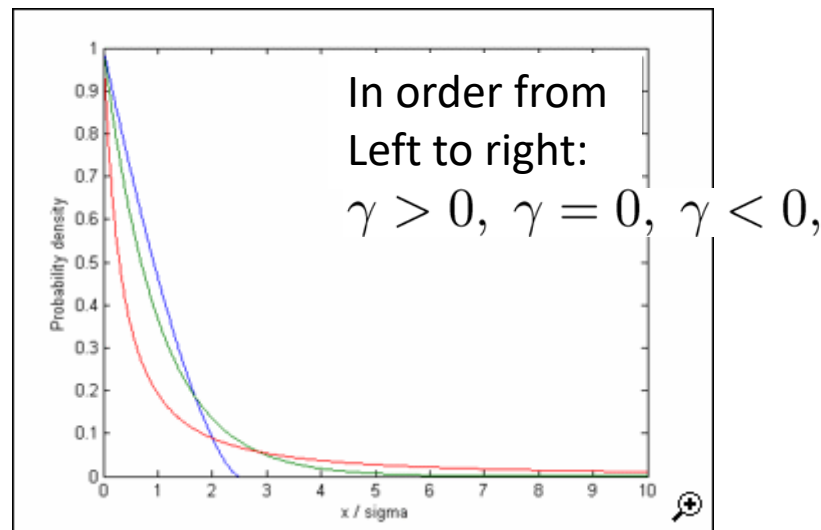
exceedance times Poisson process, excess losses have a Generalized Pareto (GP) distribution with distribution function

$$H(x) = 1 - \left(1 + \frac{\gamma}{\sigma}x\right)_+^{-1/\gamma} \quad (= 1 - e^{-x/\sigma} \text{ if } \gamma = 0),$$

and the times and sizes are all mutually independent

The choice of threshold an “art”, aided by graphics: parameter stability; median excess; goodness of fit; plots

The Generalized Pareto distribution



density function of Generalized Pareto distribution

$$h(x) = \frac{d}{dx} H(x) = \frac{1}{\sigma} \left(1 + \frac{\gamma}{\sigma} x\right)_+^{-1/\gamma - 1} \quad (= \frac{1}{\sigma} e^{-x/\sigma} \text{ if } \gamma = 0)$$

$\gamma \geq 0$ the distribution has left endpoint 0 and right endpoint ∞

$\gamma < 0$ the distribution has left endpoint 0 and right endpoint $\sigma/|\gamma|$

the distribution is “heavytailed” for $\gamma > 0$: then, moments of order greater than $1/\gamma$ are infinite/don't exist, exactly as for the Extreme Value distribution

The Generalized Pareto distribution

Assume the random variable X has d.f. F and let u be a (high) level. The distribution of exceedances then is the conditional distribution of $X-u$ given that X is larger than u , *i.e.* it has d.f.

$$F_u(x) = P(X - u \leq x | X > u) = \frac{P(X - u \leq x \text{ and } X > u)}{P(X > u)} = \frac{F(x+u) - F(u)}{1 - F(u)}$$

(and hence $\bar{F}_u(x) = 1 - F_u(x) = \frac{\bar{F}(x+u)}{\bar{F}(u)}$).

Mathematics similar to the one which motivated the Block Maxima Method shows that if $F_u(x)$ has a limit as the level $u \rightarrow \infty$ then this limit must be a GP distribution, *and* that the GP distribution is the only family of distributions which is stable under a change of levels (as specified in the next exercise).

Exercise: Show that if $F(x)$ is a GP distribution, then also $F_u(x)$ is a GP distribution, and express the parameters of $F_u(x)$ in terms of the parameters of $F(x)$. h

The Poisson process

Model for times of occurrence of events which occur “randomly” in time, with a constant “intensity”, e.g. radioactive decay, times when calls arrive to a telephone exchange, times when traffic accidents occur ... (all during periods of stationarity)

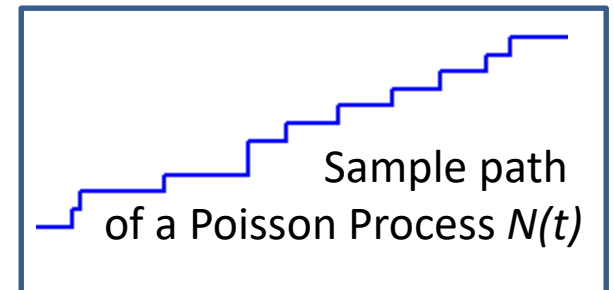
Can be mathematically described as a counting process $N(t) = \#events\ in\ [0, t]$

Mathematically, the counting process $N(t)$ is a Poisson process if

- a) The numbers of events which occur in disjoint time intervals are mutually independent
- b) $N(s+t) - N(s)$ has a Poisson distribution for any $s, t \geq 0$, i.e.

$$P(N(s+t) - N(s) = k) = \frac{(\lambda t)^k}{k!} e^{-\lambda t}, \text{ for any } s, t \geq 0, k = 1, 2, \dots$$

λ is the “intensity” parameter. One interpretation of it is that λ is the expected number of events in any time interval of length 1 .



A connection between the PoT and Block Maxima methods

Suppose the PoT model holds. Thus values larger than u occur according to a Poisson process with intensity λ , where this process is independent of the sizes of the exceedances, and these sizes are i.i.d. and have a GP distribution

$$H(x) = 1 - \left(1 + \frac{\gamma}{\sigma}x\right)_+^{-1/\gamma}. \text{ Then}$$

$$\begin{aligned} P(M_T \leq u + x) &= \sum_{k=0}^{\infty} P(M_T \leq u + x, \text{ there are } k \text{ exceedances in } [0, T]) \\ &= \sum_{k=0}^{\infty} H(x)^k \frac{(\lambda T)^k}{k!} \exp\{-\lambda T\} \\ &= \sum_{k=0}^{\infty} \left(1 - \left(1 + \frac{\gamma}{\sigma}x\right)_+^{-1/\gamma}\right)^k \frac{(\lambda T)^k}{k!} \exp\{-\lambda T\} \\ &= \exp\left\{\left(1 - \left(1 + \frac{\gamma}{\sigma}x\right)_+^{-1/\gamma}\right)\lambda T\right\} \exp\{-\lambda T\} \\ &= \exp\left\{-\left(1 + \frac{\gamma}{\sigma}x\right)_+^{-1/\gamma}\lambda T\right\} \\ &= \exp\left\{-\left(1 + \gamma \frac{x - ((\lambda T)^\gamma - 1)\sigma/\gamma}{\sigma(\lambda T)^\gamma}\right)_+^{-1/\gamma}\right\} \end{aligned}$$

Tail and quantile estimation when underlying variables (e.g. daily wind damage claims) and not just big values (e.g. total loss in big windstorm) are the data

Suppose we have observed the (random) number $N(u)$ of excesses of the level u by X_1, \dots, X_n . Writing $\bar{F}(x) = 1 - F(x)$ for the probability that an observation is larger than x , the ratio $N(u)/n$ is a natural estimator of $\bar{F}(u)$. Assume further that we have computed estimators $\hat{\sigma}, \hat{\gamma}$ of the parameters in the GP distribution from these σ, γ exceedances. Since

$$\bar{F}(x) = \bar{F}(u) \frac{\bar{F}(x)}{\bar{F}(u)} = \bar{F}(u) \bar{F}_u(x - u),$$

a natural estimator of the “tail function” $\bar{F}(x)$, for $x > u$, then is

$$\hat{\bar{F}}(x) = \frac{N(u)}{n} \left(1 + \hat{\gamma} \frac{x-u}{\hat{\sigma}}\right)^{-1/\hat{\gamma}}.$$

Solving $\hat{\bar{F}}(x_p) = p$ for x_p we get an estimator of the p -th quantile of X :

$$\hat{x}_p = u + \frac{\hat{\sigma}}{\hat{\gamma}} \left(\left(\frac{n}{N(u)} p \right)^{-\hat{\gamma}} - 1 \right).$$

(Why all this trouble? Why not just estimate $\bar{F}(x)$ by $N(x)/n$? Because if x is a very high level then $N(x)$ is very small or zero, and then this estimator is useless, and it is such very large x -es we are interested in.)