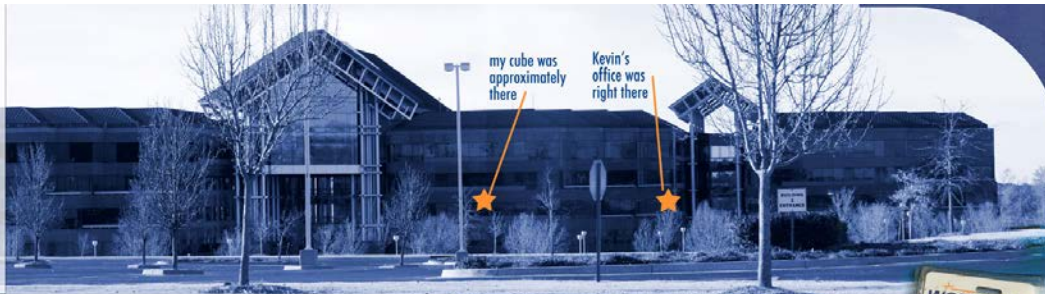


HOME TO THE
LARGEST
MULTI-BILLION
DOLLAR
CORPORATE
ACCOUNTING
FRAUD IN
THE HISTORY
OF OUR NATION



CLINTON, MISSISSIPPI -- FORMER CORPORATE WORLD HEADQUARTERS FOR WORLDCOM

As the **WORLDCOM** turns.

CORPORATE CRIME. FBI INVESTIGATIONS. MASS LAYOFFS. LOSSES. MERGERS AND MORE...

MY JOB DESCRIPTION:

I started working at WorldCom in September of 1999. While I was there, I was the designer for their Corporate Intranet, which happened to be the busiest intranet site in the world. I also did graphics for the internet site as well. I quit my job soon after Quinn was born in February of 2002.



BITTER:

Well, we lost it all! Kevin got laid off after working there for over 8 years!!! We had just bought a house, and had a baby!! Not to mention I had just quit my job (at WorldCom) to be a stay-at-home mom! We both lost our ENTIRE 401k's and Kevin also lost hundreds of thousands of dollars in vested stock options. Times were tough!

SWEET:

This is where we MET!!! This is where we worked when we got married and had our first child! This is where our life together began. So even though we lost all of our money, we gained ALL of those things that money just CANNOT BUY!! Like true love, a best friend, and family! I wouldn't trade this WorldCom experience for anything!!!!

KEVIN'S JOB DESCRIPTION:

Kevin started working at WorldCom when it was actually still LDDS. It's hard to just sum up ALL of what he did for them. He was there through over 60 mergers and acquisitions and played a major part in integrating the systems of all of the new companies. He was also over all of their Corporate Internet and Intranet Systems. Kevin was laid off from WorldCom in April of 2002, which was 2 months after I quit.



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“As an alternative to the traditional 30-year mortgage, we also offer an interest-only mortgage, balloon mortgage, reverse mortgage, upside down mortgage, inside out mortgage, loop-de-loop mortgage, and the spinning double axel mortgage with a triple lutz.”



Gudrun January 2005

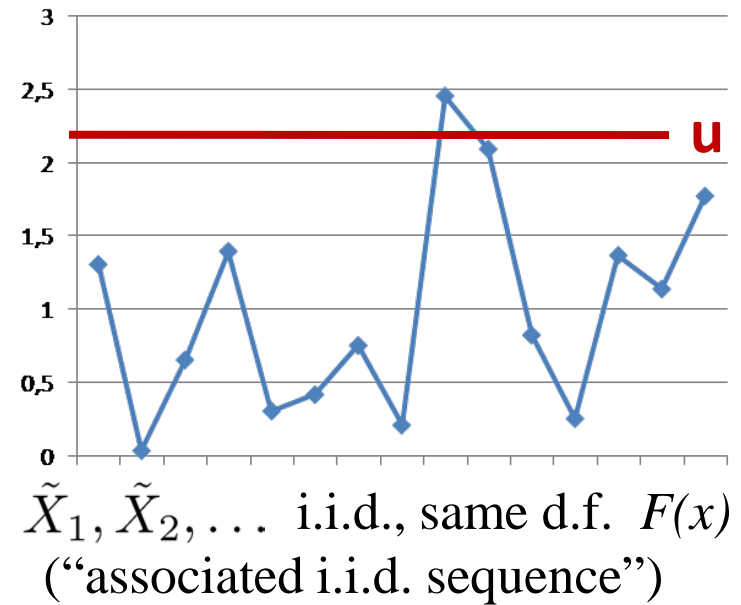
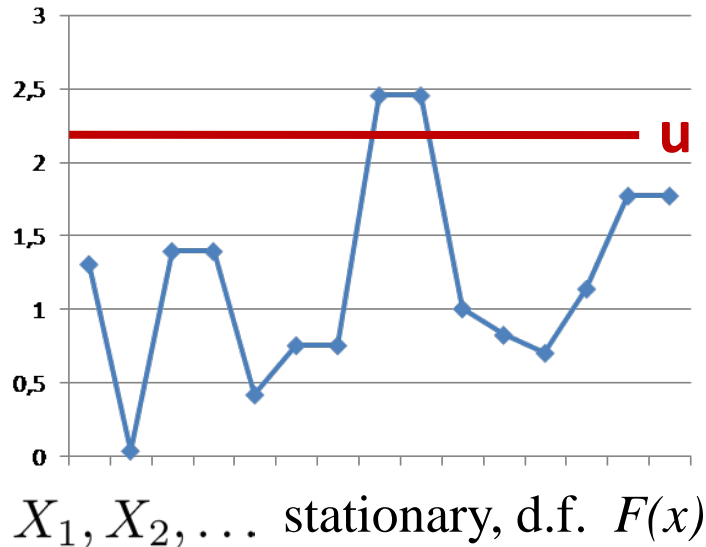
326 MEuro loss

72 % due to forest losses

4 times larger than second largest

Dependence: Extreme Value Statistics for stationary time series

(Coles p. 92-104)



Dependence \rightarrow extremes typically come in small “clusters”

θ = “**Extremal index**” = 1/”asymptotic mean cluster length”

- typically $P(M_n \leq x) \approx F(x)^{\theta n}$ for n large
- typically clusters asymptotically i.i.d., dependence within clusters
- typically tail of cluster maxima asymptotically same as $\bar{F}(x)$!!
- typically the EV distributions the only possible limit distributions

The block maxima method for stationary time series

If blocks are sufficiently long, then block maxima (typically) are approximately independent, and one can use Extreme Value Statistics in precisely the same way as for i.i.d. sequences

The PoT method for stationary time series

- 1. Decluster:** identify approximately i.i.d clusters of large values by
 - a) Block method:* divide observations up into blocks of a fixed length r , all values in a block which exceed the level u is a cluster
 - b) Blocks-runs method:* the first cluster starts at first exceedance of u and contains all excesses of u within a fixed length r thereafter. The second cluster starts at the next exceedance of u and contains all excesses of u within r thereafter, and so on. . .
 - c) Runs method:* the first cluster starts with the first exceedance of u and stops as soon as there is a value below u , the second cluster starts with the next exceedance of u , and so on . . .
- 2.** $\hat{\theta} = \frac{\text{no. of clusters}}{\text{no. of exceedances}}$ estimate of the *extremal index*
- 3. PoT:** Use standard i.i.d. PoT model, but with excesses replaced by cluster maxima, and exceedance times replaced by the times when cluster maxima occur.
- 4.** Use $P(M_n \leq x) \approx F(x)^{\theta n}$ to switch between block maxima and PoT

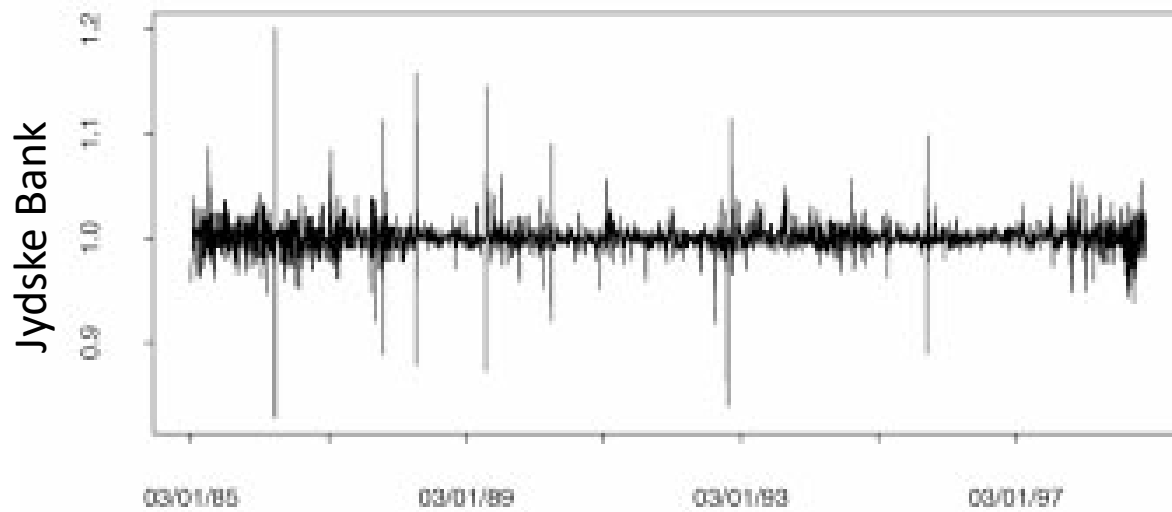
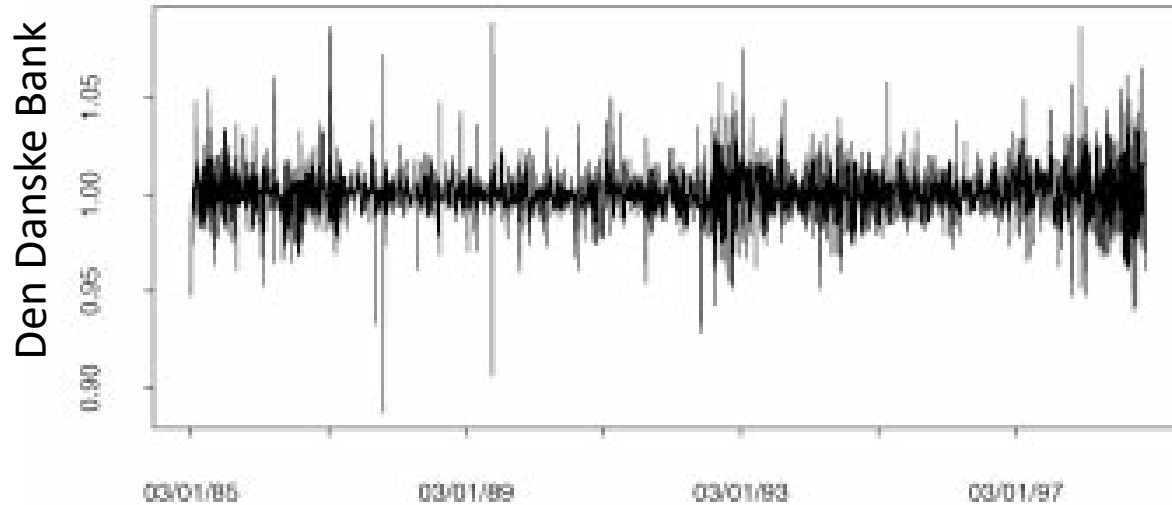
Estimating value at risk by extreme value methods;

(Sarah Lauridsen, Extremes 3, 107-144, 2000)

VaR = high quantiles of the loss-profits distribution

- empirical quantiles
- unconditional Gaussian method
- conditional Gaussian method
- GEV + different extremal index estimators
- GP pretending independence
- GP with declustering
- GARCH + GP residuals, conditional
- GARCH + GP residuals, unconditional

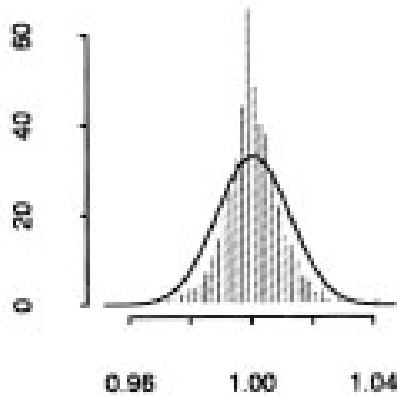
Compared, and evaluated via backtesting



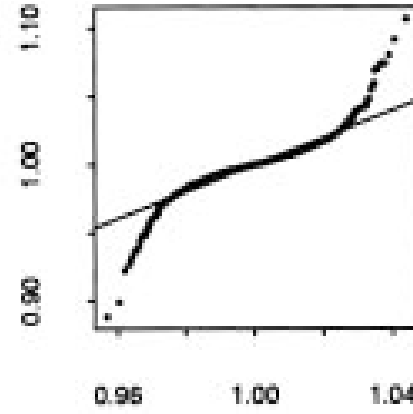
Daily returns from Jan. 1, 1985 to Nov. 27, 1998

Synthetic portfolio of 50 MDKK Danske Bank + 50 MDKK Jydske Bank

Empirical and Normal



histogram with estimated normal density
(13 left values and 10 right values not shown)



normal qq-plot

VaR in mDKr estimated by Gaussian and empirical method

1-day VaR	95%	96%	97%	98%	99%	99.9%	99.99%
Gaussian method	- 1.93	- 2.05	- 2.21	- 2.42	- 2.75	- 3.67	- 4.42
Empirical method	- 1.66	- 1.85	- 2.07	- 2.43	- 3.10	- 7.55	—

To assume returns normally distributed and i.i.d. gives easy calculations, also for complex portfolios consisting of many financial instruments.

-- but, distribution doesn't fit at all in the tails, and independence not OK

-- the empirical method gives no estimates for extreme quantiles

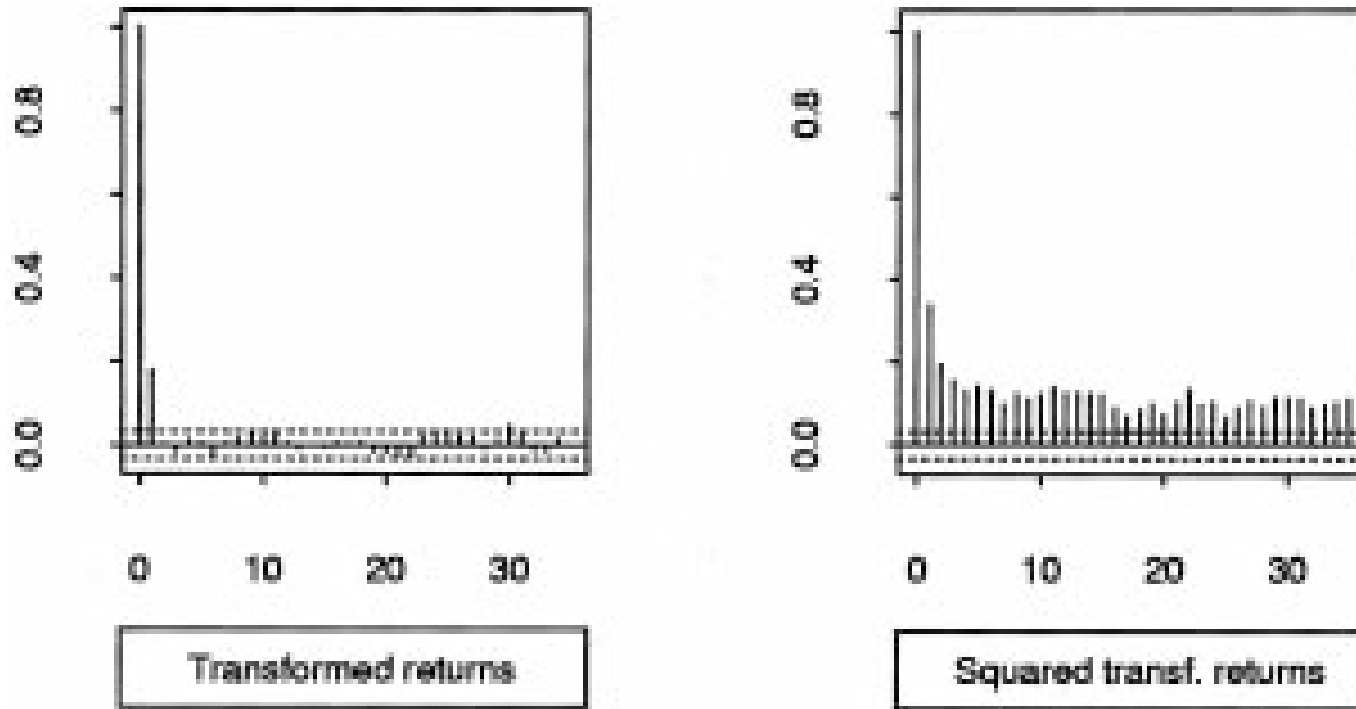
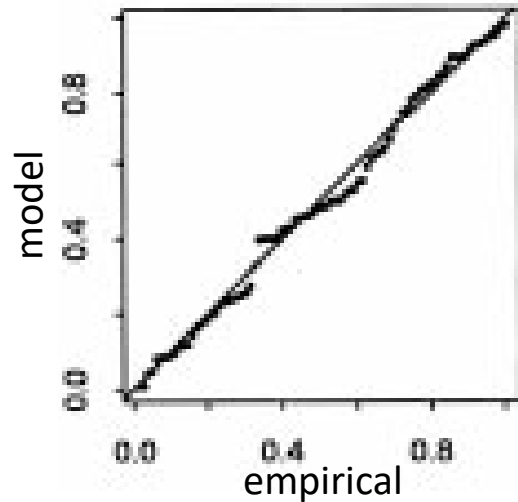


Figure 3. Auto correlograms for the series of daily returns on the bank portfolio. The returns have been transformed to have Gaussian marginals.

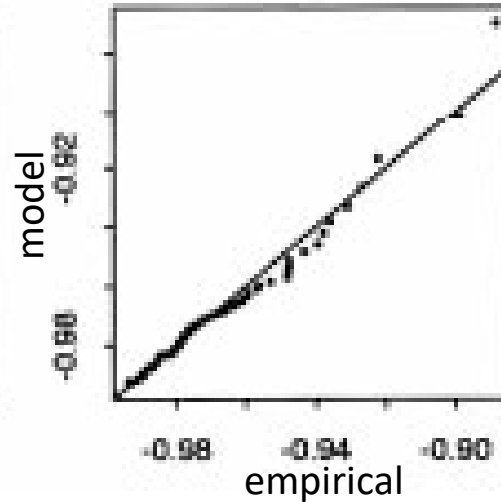
checked dependence by transforming to normal marginal distribution and computing correlations → clear and strong dependence

Block Maxima for 42 days approximately independent (figure not shown)

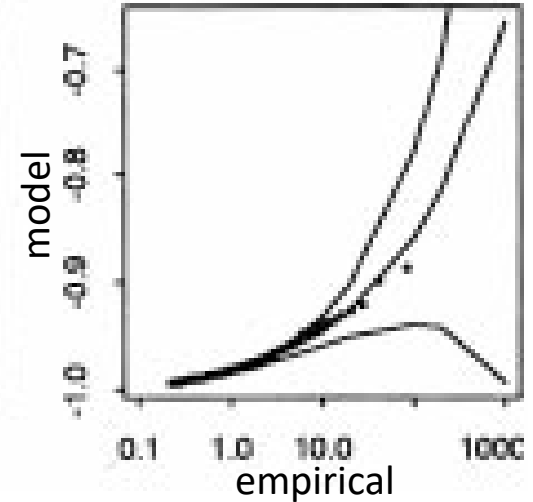
Block Maxima



pp-plot against EV,
42 day Block Maxima



qq-plot against EV,
42 day Block Maxima



return level plot assuming EV,
42 day Block Maxima

EV distribution fits the data well, and 42 days maxima interesting for firm survival, but how can one get from there to overnight VaR?

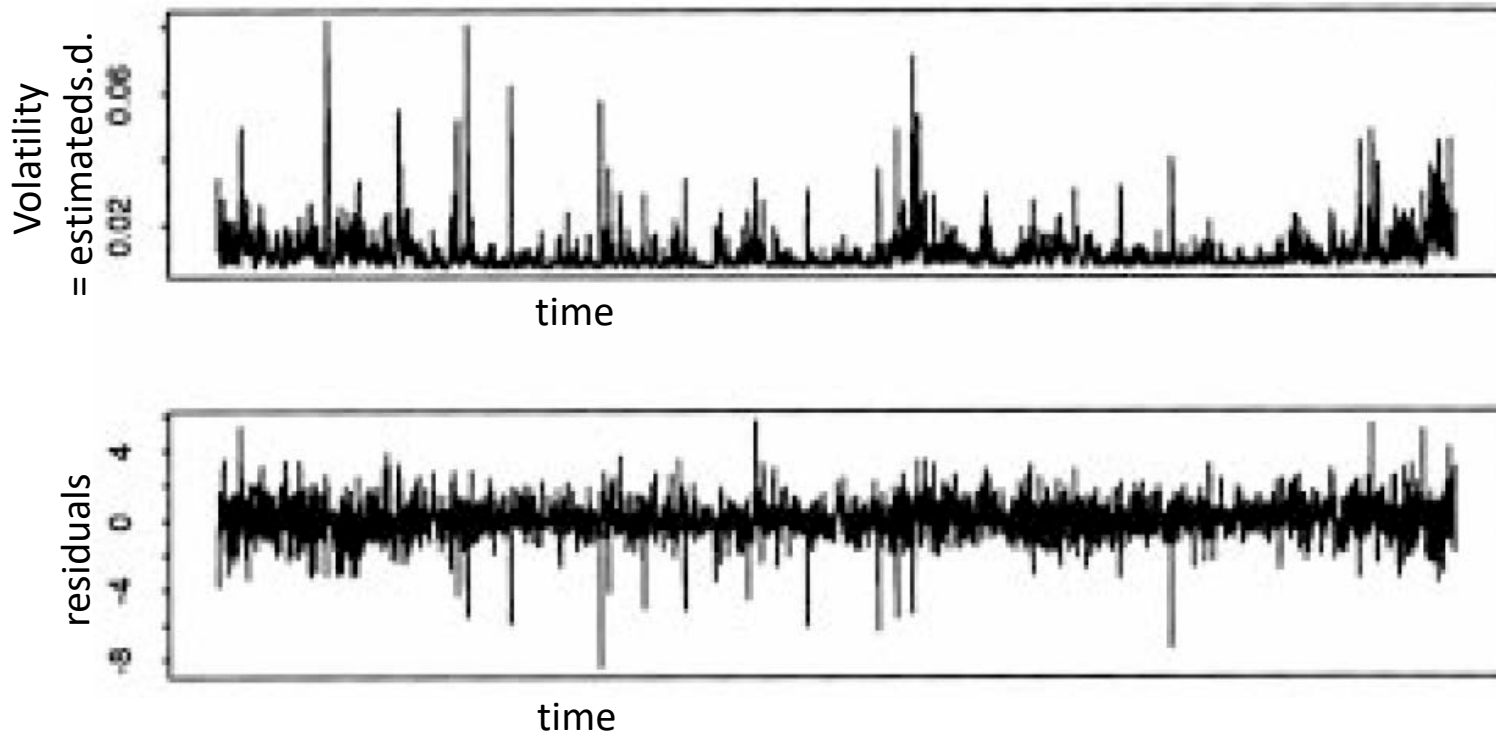
$\alpha^n \theta$ - quantile of overnight P&L-distribution may be roughly estimated by
 α - quantile of n-day maxima

- but difficult to estimate θ

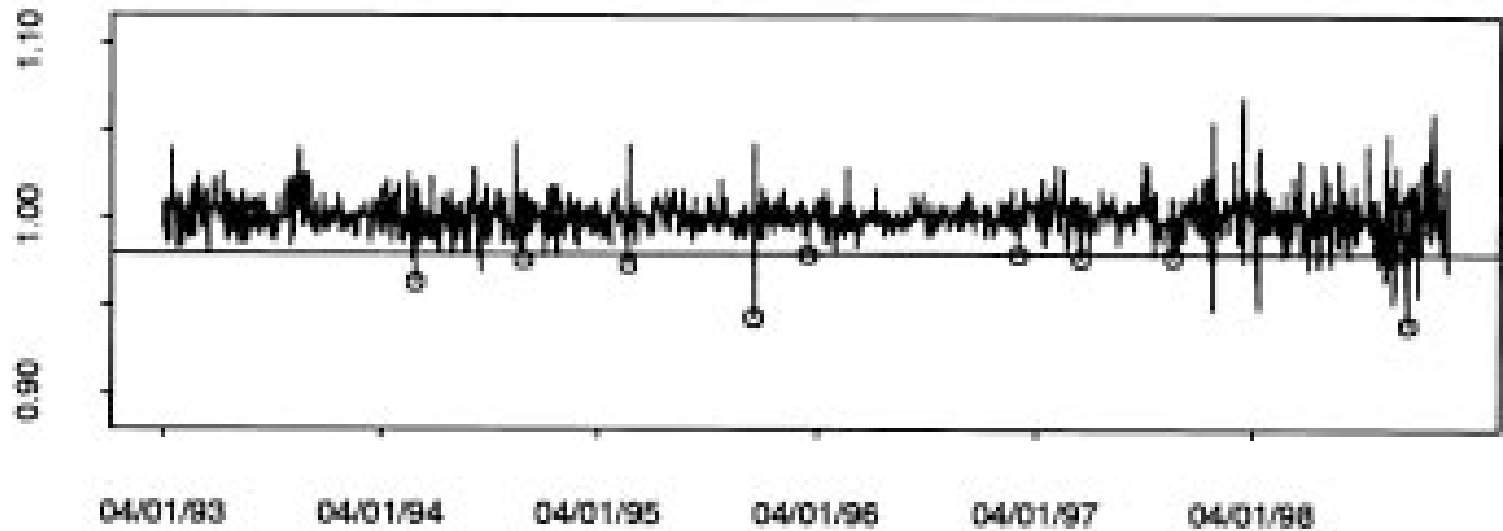
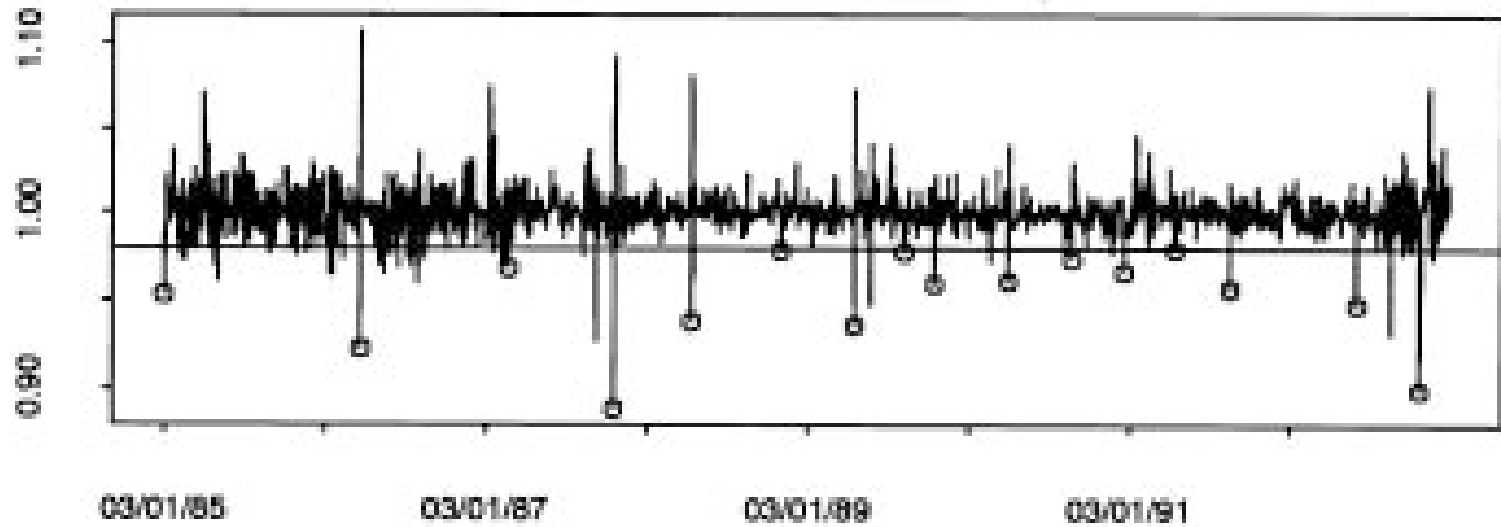
Garch

fit Garch model to data, compute residuals, fit GP distribution to residuals, and compute quantiles of the resulting estimated distribution of returns (computation done by simulation).

- this can be done *conditionally*, using the present estimate of the volatility -- for what happens with the portfolio tomorrow
- or *unconditionally* – for longtime behavior of portfolio



PoT



Cluster minima: level $u = 0.98$, separation length $r = 40$

Backtesting

Backtesting results, violations of 1-day VaR							
Empirical method							
	95%	96%	97%	98%	99%	99.9%	99.99%
Portfolio	119 (99.3)	100 (79.4)	74 (59.6)	56 (39.7)	30 (19.9)	1 (2.0)	– (0.2)
S&P 500	101 (159.9)	77 (127.9)	55 (95.9)	35 (64.0)	20 (32.0)	3 (3.2)	– (0.3)
B&O	90 (99.3)	72 (79.4)	53 (59.6)	35 (39.7)	19 (19.9)	0 (2.0)	– (0.2)
Carlsberg	81 (99.3)	68 (79.4)	56 (59.6)	39 (39.7)	17 (19.9)	0 (2.0)	– (0.2)
DS 1912	117 (99.3)	93 (79.4)	73 (59.6)	52 (39.7)	27 (19.9)	3 (2.0)	– (0.2)
ISS	148 (99.3)	126 (79.4)	93 (59.6)	63 (39.7)	23 (19.9)	1 (2.0)	– (0.2)
Novo B	113 (99.3)	90 (79.4)	70 (59.6)	49 (39.7)	26 (19.9)	2 (2.0)	– (0.2)
Svendborg	122 (99.3)	96 (79.4)	77 (59.6)	55 (39.7)	30 (19.9)	4 (2.0)	– (0.2)
Unconditional Gaussian method							
	95%	96%	97%	98%	99%	99.9%	99.99%
Portfolio	76 (99.3)	66 (79.4)	62 (59.6)	47 (39.7)	30 (19.9)	16 (2.0)	10 (0.2)
S&P 500	101 (159.9)	79 (127.9)	59 (95.9)	36 (64.0)	22 (32.0)	5 (3.2)	3 (0.3)
B&O	61 (99.3)	56 (79.4)	49 (59.6)	40 (39.7)	28 (19.9)	13 (2.0)	9 (0.2)
Carlsberg	63 (99.3)	55 (79.4)	48 (59.6)	39 (39.7)	27 (19.9)	11 (2.0)	5 (0.2)
DS 1912	105 (99.3)	95 (79.4)	85 (59.6)	67 (39.7)	48 (19.9)	19 (2.0)	8 (0.2)
ISS	81 (99.3)	67 (79.4)	57 (59.6)	41 (39.7)	29 (19.9)	19 (2.0)	11 (0.2)
Novo B	88 (99.3)	72 (79.4)	61 (59.6)	54 (39.7)	41 (19.9)	16 (2.0)	7 (0.2)
Svendborg	108 (99.3)	98 (79.4)	84 (59.6)	73 (39.7)	57 (19.9)	22 (2.0)	9 (0.2)
Conditional Gaussian							
	95%	96%	97%	98%	99%	99.9%	99.99%
Portfolio	77 (99.3)	64 (79.4)	51 (59.6)	41 (39.7)	27 (19.9)	10 (2.0)	6 (0.2)
S&P 500	151 (159.9)	127 (127.9)	88 (95.9)	61 (64.0)	33 (32.0)	7 (3.2)	4 (0.3)
B&O	71 (99.3)	61 (79.4)	53 (59.6)	42 (39.7)	27 (19.9)	11 (2.0)	7 (0.2)
Carlsberg	60 (99.3)	53 (79.4)	44 (59.6)	36 (39.7)	26 (19.9)	11 (2.0)	5 (0.2)
DS 1912	90 (99.3)	71 (79.4)	57 (59.6)	45 (39.7)	23 (19.9)	9 (2.0)	4 (0.2)
ISS	90 (98.2)	80 (78.6)	70 (58.9)	53 (39.3)	37 (19.6)	18 (2.0)	14 (0.2)
Novo B	72 (99.3)	61 (79.4)	46 (59.6)	37 (39.7)	24 (19.9)	8 (2.0)	3 (0.2)
Svendborg	97 (99.3)	87 (79.4)	72 (59.6)	52 (39.7)	31 (19.9)	10 (2.0)	4 (0.2)
GEV and simple blocks estimator (95% threshold)							
	95%	96%	97%	98%	99%	99.9%	99.99%
Portfolio	71 (99.3)	57 (79.4)	36 (59.6)	19 (39.7)	11 (19.9)	0 (2.0)	0 (0.2)
S&P	43 (159.9)	37 (127.9)	25 (95.9)	15 (64.0)	8 (32.0)	2 (3.2)	1 (0.3)
B&O	54 (99.3)	46 (79.4)	34 (59.6)	23 (39.7)	8 (19.9)	0 (2.0)	0 (0.2)
Carlsberg	40 (99.3)	33 (79.4)	24 (59.6)	16 (39.7)	7 (19.9)	0 (2.0)	0 (0.2)
DS 1912	66 (99.3)	55 (79.4)	44 (59.6)	28 (39.7)	14 (19.9)	1 (2.0)	0 (0.2)
ISS	79 (99.1)	60 (79.3)	36 (59.5)	20 (39.6)	11 (19.8)	0 (2.0)	0 (0.2)
Novo B	62 (99.3)	54 (79.4)	40 (59.6)	26 (39.7)	11 (19.9)	1 (2.0)	0 (0.2)
Svendborg	77 (99.3)	67 (79.4)	54 (59.6)	34 (39.7)	12 (19.9)	1 (2.0)	0 (0.2)

- compute VaR from the first six years of data, see if it “is violated”, i.e. if next days return is lower than VaR, repeat again using six years of data but starting one day later, two days later, ... count number of violations
- expected no. of violations in parentheses

Backtesting

Backtesting results, violations of 1-day VaR
GEV and simple blocks estimator (99% threshold)

	95%	96%	97%	98%	99%	99.9%	99.99%
Portfolio	140 (99.3)	106 (79.4)	78 (59.6)	56 (39.7)	17 (19.9)	1 (2.0)	0 (0.2)
S&P500	79 (159.9)	56 (127.9)	36 (95.9)	25 (64.0)	13 (32.0)	2 (3.2)	2 (0.3)
B&O	80 (99.3)	63 (79.4)	51 (59.6)	38 (39.7)	15 (19.9)	0 (2.0)	0 (0.2)
Carlsberg	80 (99.3)	70 (79.4)	51 (59.6)	33 (39.7)	16 (19.9)	0 (2.0)	0 (0.2)
DS 1912	108 (99.3)	94 (79.4)	75 (59.6)	48 (39.7)	23 (19.9)	4 (2.0)	0 (0.2)
ISS	157 (99.1)	129 (79.3)	97 (59.5)	61 (39.6)	23 (19.8)	2 (2.0)	0 (0.2)
Novo B	115 (99.3)	93 (79.4)	71 (59.6)	49 (39.7)	25 (19.9)	2 (2.0)	0 (0.2)
Svendborg	125 (99.3)	106 (79.4)	82 (59.6)	60 (39.7)	26 (19.9)	3 (2.0)	0 (0.2)

GEV and blocks estimator (95% threshold)

	95%	96%	97%	98%	99%	99.9%	99.99%
Portfolio	139 (99.3)	107 (79.4)	78 (59.6)	54 (39.7)	18 (19.9)	1 (2.0)	0 (0.2)
S&P500	97 (159.9)	75 (127.9)	57 (95.9)	34 (64.0)	15 (32.0)	3 (3.2)	2 (0.3)
B&O	89 (99.3)	73 (79.4)	58 (59.6)	44 (39.7)	17 (19.9)	1 (2.0)	0 (0.2)
Carlsberg	77 (99.3)	65 (79.4)	46 (59.6)	33 (39.7)	14 (19.9)	0 (2.0)	0 (0.2)
DS 1912	112 (99.3)	90 (79.4)	70 (59.6)	49 (39.7)	21 (19.9)	3 (2.0)	0 (0.2)
ISS	147 (99.1)	129 (79.3)	94 (59.5)	46 (39.6)	20 (19.8)	1 (2.0)	0 (0.2)
Novo B	109 (99.3)	88 (79.4)	65 (59.6)	45 (39.7)	21 (19.9)	2 (2.0)	0 (0.2)
Svendborg	118 (99.3)	100 (79.4)	80 (59.6)	58 (39.7)	29 (19.9)	2 (2.0)	0 (0.2)

GEV and blocks estimator (99% threshold)

	95%	96%	97%	98%	99%	99.9%	99.99%
Portfolio	166 (99.3)	133 (79.4)	99 (59.6)	62 (39.7)	23 (19.9)	1 (2.0)	0 (0.2)
S&P500	88 (159.9)	66 (127.9)	45 (95.9)	31 (64.0)	14 (32.0)	3 (3.2)	2 (0.3)
B&O	86 (99.3)	75 (79.4)	59 (59.6)	45 (39.7)	18 (19.9)	1 (2.0)	0 (0.2)
Carlsberg	102 (99.3)	78 (79.4)	61 (59.6)	42 (39.7)	20 (19.9)	0 (2.0)	0 (0.2)
DS 1912	126 (99.3)	104 (79.4)	87 (59.6)	55 (39.7)	27 (19.9)	5 (2.0)	1 (0.2)
ISS	187 (99.1)	156 (79.3)	114 (59.5)	75 (39.6)	27 (19.8)	2 (2.0)	0 (0.2)
Novo B	133 (99.3)	109 (79.4)	81 (59.6)	58 (39.7)	30 (19.9)	4 (2.0)	0 (0.2)
Svendborg	144 (99.3)	121 (79.4)	99 (59.6)				

GPD

	95%	96%	97%	98%	99%	99.9%	99.99%
Portfolio	118 (99.3)	98 (79.4)	78 (59.6)	57 (39.7)	20 (19.9)	1 (2.0)	0 (0.2)
S&P500	26 (20.8)	26 (16.6)	21 (12.5)	16 (8.32)	5 (4.1)	2 (0.4)	1 (0.04)
B&O	89 (98.9)	74 (79.1)	54 (59.3)	38 (39.5)	16 (19.8)	2 (2.0)	0 (0.2)
Carlsberg	69 (95.6)	56 (76.8)	46 (57.6)	33 (38.4)	16 (19.2)	1 (2.0)	0 (0.2)
DS 1912	98 (74.3)	76 (59.4)	65 (44.6)	41 (29.7)	24 (14.9)	4 (1.5)	1 (0.1)
ISS	151 (99.3)	128 (79.4)	95 (59.6)	61 (39.7)	26 (19.9)	3 (2.0)	0 (0.2)
Novo B	116 (99.2)	89 (79.4)	70 (59.5)	50 (39.7)	27 (19.8)	4 (2.0)	1 (0.2)
Svendborg	110 (88.9)	96 (71.1)	68 (53.3)	52 (35.5)	25 (17.8)	4 (1.8)	0 (0.2)

- compute VaR from the first six years of data, see if it “is violated”, i.e. if next days return is lower than VaR, repeat again using six years of data but starting one day later, two days later, ... count number of violations

- expected no. of violations in parentheses

Backtesting

Backtesting results, violations of 1-day VaR GARCH based extreme value method, conditional							
	95%	96%	97%	98%	99%	99.9%	99.99%
Portfolio	109 (99.3)	91 (79.4)	64 (59.6)	44 (39.7)	18 (19.9)	1 (2.0)	0 (0.2)
S&P 500	145 (157.8)	123 (126.2)	88 (94.7)	60 (63.1)	34 (31.6)	6 (3.2)	2 (0.3)
B&O	95 (99.3)	73 (79.4)	53 (59.6)	33 (39.7)	12 (19.9)	2 (2.0)	0 (0.2)
Carlsberg	75 (99.3)	61 (79.4)	45 (59.6)	32 (39.7)	20 (19.9)	0 (2.0)	0 (0.2)
DS 1912	94 (98.3)	66 (78.6)	48 (59.0)	26 (39.3)	11 (19.6)	2 (2.0)	1 (0.2)
ISS	144 (98.2)	117 (78.5)	87 (58.9)	57 (39.3)	22 (19.6)	5 (2.0)	0 (0.2)
Novo B	93 (99.3)	75 (79.4)	52 (59.6)	36 (39.7)	18 (19.9)	2 (2.0)	0 (0.2)
Svendborg	102 (99.3)	87 (79.4)	60 (59.6)	34 (39.7)	14 (19.9)	3 (2.0)	1 (0.2)
GARCH based extreme value method, unconditional							
	95%	96%	97%	98%	99%	99.9%	99.99%
Portfolio	107 (98.1)	90 (78.4)	66 (58.8)	44 (39.2)	16 (19.6)	0 (2.0)	0 (0.2)
S&P500	98 (143.8)	77 (115.1)	55 (86.3)	30 (57.5)	14 (28.8.0)	2 (2.9)	0 (0.3)
B&O	82 (99.3)	65 (79.4)	52 (59.6)	34 (39.7)	14 (19.9)	0 (2.0)	0 (0.2)
Carlsberg	88 (98.8)	77 (79.0)	62 (59.3)	37 (39.5)	22 (19.8)	0 (2.0)	0 (0.2)
DS 1912	108 (94.8)	87 (75.8)	69 (56.9)	43 (37.9)	20 (19.0)	1 (2.0)	0 (0.2)
ISS	114 (81.7)	100 (65.3)	70 (49.0)	41 (32.7)	16 (16.3)	1 (1.6)	0 (0.2)
Novo B	106 (99.2)	87 (79.4)	62 (59.5)	49 (39.7)	25 (19.8)	2 (2.0)	0 (0.2)
Svendborg	115 (98.6)	100 (78.8)	76 (59.1)	56 (39.4)	27 (19.7)	2 (2.0)	0 (0.2)

- compute VaR from the first six years of data, see if it “is violated”, i.e. if next days return is lower than VaR, repeat again using six years of data but starting one day later, two days later, ... count number of violations

- expected no. of violations in parentheses