# Spot shape modelling and data transformations for microarrays

Claus Thorn Ekstrøm*,	Dept.	of Mathematics	and Physics,	The R	Royal Veterinary	and Agricultural	University,
Thorvaldsensvej 40, I	OK-1871	l Frederiksberg C	., Denmark				

- Søren Bak, Plant Biochemistry Laboratory, Dept. of Plant Biology, and Center of Molecular Plant Physiology (PlaCe), Royal Veterinary and Agricultural University, Thorvaldsensvej 40, DK-1871 Frederiksberg C., Denmark
- Charlotte Kristensen†, Plant Biochemistry Laboratory, Dept. of Plant Biology, and Center of Molecular Plant Physiology (PlaCe), Royal Veterinary and Agricultural University, Thorvaldsensvej 40, DK-1871 Frederiksberg C., Denmark

Mats Rudemo, Dept. of Mathematics and Physics, The Royal Veterinary and Agricultural University, Thorvald-sensvej 40, DK-1871 Frederiksberg C., Denmark

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<sup>\*</sup> To whom correspondence should be addressed

<sup>†</sup> Current address: Poalis A/S, Bülowsvej 25, 1870 Frederiksberg C, Denmark

#### Abstract

Motivation: To study lowly expressed genes in microarray experiments it is useful to increase the photometric gain in the scanning. However, a large gain may cause some pixels for highly expressed genes to become saturated. Spatial statistical models that model spot shapes on the pixel level may be used to infer information about the saturated pixel intensities. Other possible applications for spot shape models include data quality control and accurate determination of spot centres and spot diameters.

Results: Spatial statistical models for spotted microarrays are studied including pixel level transformations and spot shape models. The models are applied to a dataset from 50-mer oligonucleotide microarrays with 452 selected Arabidopsis genes. Logarithmic, Box-Cox and inverse hyperbolic sine transformations are compared and it is found that the Box-Cox transformation performs best. For spot shapes we compare a cylindric plateau shape, an isotropic Gaussian distribution and a difference of two scaled Gaussian distribution suggested in the literature. A substantial improvement is obtained for the dataset studied by a new polynomialhyperbolic spot shape model. The spatial statistical models are used to correct spot measurements with saturation by extrapolating the censored data.

**Availability:** Source code for R are available at http://www.matfys.kvl.dk/~ekstrom/spotshapes/

Contact: ekstrom@dina.kvl.dk

#### 1 Introduction

In order to study lowly expressed genes in microarray experiments it is useful to increase the photometric gain in the scanning. However, a large gain may cause some pixels for highly expressed genes to become saturated, that is the registered pixel values become censored at the upper limit, which with 16 bit precision is  $2^{16}-1=65535$ . Techniques for adjustment of highly expressed signal intensities are given in Wit and McClure (2003) based on a small set of available spot summaries such as spot mean, spot median and spot variance. As mentioned in Wit and McClure (2003) it should be possible to get more accurate adjustments when all pixel values are available. In the present paper we study spatial statistical models for pixel values which should enable such adjustments.

A convenient type of modelling is to transform data to become approximately Gaussian distributed with a mean value function determined by gene intensities and spot shapes and a corresponding covariance function. For such models censored pixel values can be optimally estimated. We investigate several types of transformations on the pixel level such as the logarithmic transformation, the Box-Cox family (Box and Cox, 1964) and the inverse hyperbolic sine transformation (Huber et al., 2002; Durbin et al., 2002), also called the generalized logarithm (Rocke and Durbin, 2003). The inverse hyperbolic sine transformation has proven useful for analyzing microarray spot intensities, but here we apply it at the pixel level. The Box-Cox transformation with exponent 0.5, i.e. a square root transformation optimal for Poisson distributed counts, has been used at pixel level analysis of microarray data by Glasbey and Ghazal (2003).

The spot shapes studied include three types suggested by Wierling et al. (2002): (i) a cylindric plateau spot distribution, (ii) an isotropic 2D Gaussian distribution, and (iii) a crater spot distribution consisting of a difference between two scaled isotropic 2D Gaussian distributions. These models do not seem to give a satisfactory description for the dataset considered, and we introduce a new class of models with polynomial-hyperbolic spot shape. With a second degree polynomial we get a considerably improved performance. This spot shape may be regarded as a generalization of the cylindric plateau spot shape (i).

The models are applied to a dataset obtained with a specially designed spotted 50-mer oligonucleotide microarray. Here the expression of 452 selected genes in transgenic Arabidopsis plants are compared to the corresponding genes in wild-type plants. Data include scans with different photometric gains ranging from no saturation to heavy saturation.

[Figure 1 about here.]

## 2 Data, transformations and exploratory analysis

#### 2.1 Materials

The data used for shape modelling and data transformation are based on a transcriptome analysis (to be described in detail in a future publication, Kristensen and Bak) of metabolically altered Arabidopsis plants (Tattersall et al., 2000). The array is a custom designed 50-mer oligonucleotide array,  $9 \times 18$  mm, 350  $\mu m$  dot spacing, spotted by MWG Biotech using a single pin on epoxy coated glass slides. array contains probes for 452 selected Arabidopsis genes designed to cover the cytochromes P450 (Paguette et al., 2000; Werck-Reichhart et al., 2002) (see http://www.biobase.dk/P450/) and glycosyltransferase (UGT) (Paquette et al., 2003) multigene families as well as genes that relate to aromatic amino acid biosynthesis, secondary metabolism and stress. The 50-mer oligonucleotides were designed by MWG Biotech, essentially as described by Kane et al. (2000). mRNA was isolated from 30 days old Arabidopsis rosette leaves using MicroPoly(A)Pure  $^{TM}$  small scale mRNA purification kit (Ambion). 3-3.5  $\mu g$  mRNA was used for direct incorporation of cy3- and cy5-fluorescent dyes (Amersham Pharmacia Biotech) using Superscript II kit (Invitrogen). Hybridizations and washings were performed essentially according to the manufacturers instructions and subsequently scanned using a GMS 418 Array Scanner (Affymetrix) using four different photomultiplier gains: 30, 40, 50, 60 while keeping the laser power at 30.

The resulting 16 bit gray scale tif-images are available for two varieties: wildtype wt, transgenic line 3x.8, four photomultiplier gains: 30, 40, 50, 60, and two dye swap experiments: cy3, cy5, for a total of 16 images.

#### 2.2 Transformations

Let Z = Z(x) denote the intensity of a pixel x. Here Z is a 16-bit integer, i.e.,  $0 \le Z \le 2^{16} - 1 = 65535$ . Let Y(x) denote a transformation of Z(x),

$$Y(x) = f(Z(x), \lambda), \tag{1}$$

where  $f(\cdot, \lambda)$  is a family of transformation depending on the parameter vector  $\lambda$ .

In the following, we shall consider three transformations: A  $logarithmic\ transformation$ 

$$Y = k \log(Z + \lambda_1),\tag{2}$$

where  $\lambda_1$  is a positive offset parameter. A Box-Cox transformation

$$Y = \begin{cases} k \left( (Z + \lambda_1)^{\lambda_2} - 1 \right) / \lambda_2 & \text{if } \lambda_2 \neq 0 \\ k \log(Z + \lambda_1) & \text{if } \lambda_2 = 0 \end{cases}$$
 (3)

where  $\lambda_1 > 0$ , and an inverse hyperbolic sine transformation

$$Y = k \operatorname{arsinh}(\frac{Z + \lambda_1}{\lambda_2}), \ \lambda_2 > 0.$$
 (4)

The constant k is used in all three transformations to scale the transformed pixel intensities such that a saturated pixel (i.e., a pixel with intensity  $Z = 2^{16} - 1 = 65535$ ) corresponds to a value of Y = 1.

#### [Figure 2 about here.]

Note that  $\arcsin h(z) = \log(z + \sqrt{z^2 + 1})$  for z > 0, so for large z we have  $\arcsin h(z) \approx \log(2z)$ . As a result, the logarithmic transformation is essentially (at least for large values of z) a special case of both the Box-Cox transformation (with  $\lambda_2 = 0$ ) and the inverse hyperbolic sine transformation (with  $\lambda_2 = 2$ ).

Figure 1 shows the inverted grey scale image of the Y-intensities for the logarithmic transformation (2) with  $\lambda_1=20$  and  $k=1/\log(2^{16}+20-1)$  for the wildtype

green (cy3) channel with photometric gain 60. Pixels with Y-values close to 1 are shown in black and pixels with Y-values close to 0 are light grey. The middle panel of Figure 1 shows the corresponding saturated pixels where Y=1. In the right panel we show the intensities for three spots with photometric gains 30, 40, 50 and 60, respectively, along horisontal lines through the spot centres. Each of the intensity curves are given for 25 pixels, the centre pixel and 12 pixels on each side. The spots are the sixth, tenth and twelfth spots in the 9th row in the left panel; these three spots have numbers 102, 106, and 108, and show medium, high and low spot intensity, respectively, and the intensity curves are overlayed for all four gains. Spots 102, 106 and 108 are marked with boxes in the left panel of Figure 1.

#### 3 Spot shape models

Based on empirical observations of spot intensity profiles as seen in Figure 1, we desire a spatial spot shape model to have the following three properties: (i) isotropic, i.e., that the average intensity at a pixel x only depends on the distance from x to the spot centre and not on the direction from the centre, (ii) should allow for spot-shapes resembling both "volcanos/craters/donuts" and "plateaus". Spot intensities are often highest near the edge of the spot and smaller near the spot centre making the resulting spot shape resemble a volcano (see middle panel of Figure 1), and (iii) allow for spatial correlation, i.e., pixels close together and with the same distance from the spot centre should be more correlated than pixels further apart.

Let S denote the set of spots. With each spot  $s, s \in S$ , we associate a set  $A_s$  of pixels. We assume that no pixel belongs to more than one such set, and some pixels may not be associated with any spot. Let Y = Y(x) denote the (possibly transformed) intensity at a pixel, x, with pixel centre coordinates  $x = (x_1, x_2)$ . We assume that Y(x) and Y(x') are independent if x and x' are associated with different spots.

Consider now a spot s and pixels  $x \in A_s$ . Let  $c_s = (c_{s1}, c_{s2})$  be the spot centre of spot s, and let  $r_s(x) = ||x - c_s||$  be the distance from pixel x to the spot centre. Assume that

$$Y(x) = B_s h_s(r_s(x)) + b_s + \epsilon(x), \quad x \in A_s$$
 (5)

where  $B_s$  measures the intensity of spot s,  $b_s$  is a constant representing the background,  $h_s(r)$  is a spot shape function and  $\epsilon(x)$  corresponds to zero-mean noise at x. We assume that  $(Y(x), x \in A_s)$  has a multivariate normal distribution with mean vector  $\mu_s$  and covariance matrix  $C_s$ . Thus

$$\mu_s(x) = B_s h_s(r_s(x)) + b_s,$$

and the spot shape function  $h_s(r)$  may depend on parameters. Some spot shape parameters may be common

for all spots but some may be spot-specific.

In the present paper we only consider the simplest covariance model where each pixel intensity is assumed independent, i.e.,  $\epsilon(x) \sim N(0, \sigma^2 \mathbf{I})$ , where  $\mathbf{I}$  is the identity matrix. More complicated spatial correlation structures will be investigated further in a later publication.

We consider the following four spot shape models:

#### The cylindrical shape model. Let

$$h_s(r) = \frac{1}{\pi \sigma_s^2} 1(r \le \sigma_s), \tag{6}$$

where 1(P) = 1 if P is true and 1(P) = 0 otherwise. The parameter  $\sigma_s > 0$  is the radius of the spot.

#### The Gaussian shape model. Put

$$h_s(r) = \frac{1}{\sqrt{2\pi}\sigma_s^2}\phi(\frac{r}{\sigma_s}),\tag{7}$$

where  $\sigma_s > 0$  and  $\phi$  is the standardized onedimensional normal density

$$\phi(r) = \frac{1}{\sqrt{2\pi}} \exp(-\frac{1}{2}r^2).$$

#### The Gaussian difference shape model. Let

$$h_s(r) = \frac{1 + \alpha_s}{\sqrt{2\pi}\sigma_s^2}\phi(\frac{r}{\sigma_s}) - \frac{\alpha_s}{\sqrt{2\pi}(\beta_s\sigma_s)^2}\phi(\frac{r}{\beta_s\sigma_s}), \quad (8)$$

where  $\sigma_s > 0$ ,  $\alpha_s > 0$  and  $0 < \beta_s < 1$ .

#### A polynomial-hyperbolic spot shape family. Put

$$g_s(r) = \sum_{i=1}^{I} b_{si} r^i - \frac{a_s}{\gamma_s - r}, \quad 0 \le r < \gamma_s,$$

where  $I \geq 2$ ,  $a_s > 0$  and  $\gamma_s > 1$ . Put further

$$h_s(r) = \begin{cases} \frac{K_s}{\sigma_s^2} \exp(g_s(r/\sigma_s)) & \text{if } 0 \le r < \gamma_s \sigma_s \\ 0 & \text{if } r \ge \gamma_s \sigma_s, \end{cases}$$
(9)

where  $\sigma_s$  represents the radius of the spot and  $\sigma_s \gamma_s$  is the distance from the spot centre where there are no more signal from the spot. The constant  $K_s$  is a function of the parameters  $b_{s1}, \ldots, b_{sI}, a_s, \gamma_s$  such that

$$\int_0^\infty \int_0^{2\pi} h_s(r) r dr d\theta = 1,$$

a condition that is also satisfied by the spot shapes (6), (7), and (8). The parameters  $a_s$  and  $\gamma_s$  determine the steepness of the spot edge. It may be noted that the spot function (9) is zero outside a circle around the centre for  $r > \gamma_s \sigma_s$ , similar to the cylindric spot function (6), which is zero

for  $r > \sigma_s$ . While the cylindric spot shape function is discontinuous, the function (9) is continuous and infinitely differentiable. However, the cylindric spot shape may be obtained as a limiting case of the polynomial-hyperbolic spot shape, see below.

We require the boundary condition

$$g_s'(0) = 0, (10)$$

i.e., that the spot intensities are flat near the centre of the spot. Most often, we would also require that

$$g_s'(1) = 0, (11)$$

such that the spot intensity starts to decrease at value 1 (i.e., when the pixel is at distance  $\sigma_s$  away from the spot centre).

For I=2 the boundary conditions (10) and (11) result in the following constraints on the parameters in the polynomial:

$$b_{s1} = a_s/\gamma_s^2 b_{s2} = \frac{a_s}{2} \left\{ \frac{1}{(\gamma_s - 1)^2} - \frac{1}{\gamma_s^2} \right\}.$$

If we here let  $a_s$  tend to zero and  $\gamma_s$  tend to one we get the the cylindric spot shape as a limiting case.

We will use the condition (11) in the sequel but it may be noted that if we specify  $g'_s(1)$  as a positive constant we may obtain spot shapes with a dome shape, and if we specify  $g'_s(1)$  as a negative constant we may obtain more pronounced crater shapes.

Data and estimated spot shape for the polynomial-hyperbolic spot shape model are shown in 3D in Figure 3 for spot 102 at gain 60, corresponding to the upper curve in the right panel of Figure 1.

#### [Figure 3 about here.]

Fitted cylindrical, Gaussian, Gaussian difference, and polynomial-hyperbolic shape functions corresponding to the spots in the right panel of Figure 1 are shown in Figure 4. It is clearly seen that the polynomial-hyperbolic spot shape model fits the data better than the three other models.

#### [Figure 4 about here.]

### 4 Estimation of parameters and saturated (censored) values

#### 4.1 Parameter estimation

Let  $A_s' = \{x \in A_s : Y(x) < \ell_c\}$  and  $A_s'' = \{x \in A_s : Y(x) \ge \ell_c\}$  denote the set of pixels in  $A_s$  that are uncensored and censored, respectively, at the level  $\ell_c$ . Spot shape parameters may be estimated by maximizing the log likelihood function

$$L_Y = L_1 + L_2, (12)$$

where

$$L_1 = \sum_{x \in A_s'} \log \left\{ \frac{1}{\sigma_e} \phi\left(\frac{Y(x) - B_s h_s(r_s(x)) - b_s}{\sigma_e}\right) \right\}$$

and

$$L_2 = \sum_{x \in A''} \log\{1 - \Phi(\frac{\ell_c - B_s h_s(r_s(x)) - b_s}{\sigma_e})\},\,$$

where  $\phi$  and  $\Phi$  are the standardized normal density function and distribution function, respectively. The log likelihood (12) can be maximized by standard iterative maximization techniques, e.g., quasi-Newton or Nelder-Mead.

We note that if the spot shape parameters are varied individually for spots we get six parameters for the spot shape models (6) and (7):  $B_s$ ,  $c_{s1}$ ,  $c_{s2}$ ,  $b_s$ ,  $\sigma_e$  and  $\sigma_s$ , and eight parameters for the models (8) and (9). The additional parameters are  $\alpha_s$  and  $\beta_s$  for model (8) and  $a_s$  and  $\gamma_s$  for model (9).

To estimate also parameters in the transformation (1), we maximize

$$L_Z = L_Y + \sum_x \log\left(\frac{\partial Y(x)}{\partial Z}\right),$$
 (13)

### 4.2 Prediction of saturated (censored)

For  $x \in A_s''$  we denote the transformed estimated (predicted) intensity by

$$\hat{Y}(x) = \hat{B}_s \hat{h}_s(r_s(x)) + \hat{b}_s,$$

where  $\hat{B}_s$  and  $\hat{b}_s$  denote estimated parameters and  $\hat{h}_s$  denotes the spot shape function with estimated parameters. If f is the transformation employed, e.g., (2), (3) or (4), then the corresponding estimated intensity is

$$\hat{Z}(x) = f^{-1}(\hat{Y}(x)).$$

Once the predicted values for the saturated pixels are obtained, we can plug-in these values and analyze the spot as if all pixels were completely observed.

#### 5 Results

#### 5.1 Choice of transformation

The Box-Cox (3) and the inverse hyperbolic sine transformation (4) both contain the logarithmic transformation (2) as a special case. Thus we can use log likelihoods to tests if either of them gives a significant improvement relative to the logarithmic transformation.

The results shown in Table 1 are based on analysis of 25 spots and for each of them four gains, which gives 100 datasets. The choice of spots was made such that both low, median and high intensity levels were represented but with a slight over-representation of high intensities as one of our main objective was to study reconstruction of spots with saturated pixels.

As the polynomial-hyperbolic spot shape model turned out to clearly superior to the other spot shape models studied here, it was used in the comparison of the three transformations.

Table 1 shows that the Box-Cox transformation provides the best fit when we use the log likelihood as criterion, and that even the Box-Cox transformation with fixed values of  $\lambda_1$  and  $\lambda_2$  provides a better median fit than does the logarithmic and inverse hyperbolic transformations with variable  $\lambda$ 's. The inverse hyperbolic transformation gives a small improvement relative to the logarithmic transformation.

The logarithmic transformation with variable offset parameter  $\lambda_1$  turned out to be considerably better than the logarithmic transformation with fixed  $\lambda_1 = 1$ . (We use  $\lambda_1 = 1$  as fixed value rather than  $\lambda_1 = 0$  as some pixel values were zero.)

A priori, we can not formally test the Box-Cox and the inverse hyperbolic sine transformations against each other as the statistical models are not nested. However, it turned out that in most of the 100 datasets the logarithmic and inverse hyperbolic sines were close, while the Box-Cox transformation gave a considerable improvement relative to the logarithmic transformation. Therefore, we conclude that the Box-Cox transformation was also superior to the inverse hyperbolic sine in this study.

[Table 1 about here.]

#### 5.2 Choice of spot shape model

Using the Box-Cox transformation the four spot shape models are compared in Table 2 for the same spots that were used in Table 1. As was also indicated in Figure 4 the polynomial-hyperbolic shape gives a considerably better fit than the other three spot shape models, and the differences are here much larger than in the comparison of the transformations.

Interestingly, the second best fit is provided by the simple cylindrical model while the two Gaussian models give the worst fit. This was also suggested by Figure 4 where the Gaussian models — in contrast to the cylindrical and the polynomial hyperbolic shape models — fit equally bad on the spot boundary and at the spot centres.

[Table 2 about here.]

#### 5.3 Reconstruction of saturated values

Figure 5 shows the estimated spot profiles for the polynomial-hyperbolic spot shape model when the pixels for spots 242, 352 and 787 are artificially censored at different intensities. These three spots were chosen as those with the highest level not exceeding the upper limit. Thus the the leftmost diagrams show for each of these spots the estimate without censoring, while the other diagrams show reconstruction for varying degrees of censoring. In these diagrams the Box-Cox transformation was used with fixed  $\lambda$ -values,  $\lambda_1=3.35$  and  $\lambda_2=.13$ . The parameters  $a_s$  and  $\gamma_s$ , were also fixed and chosen empirically to mimic the results shown in Table 1,  $a_s=0.65$  and  $\gamma_s=1.75$ .

The conclusion from Figure 5 is that with a small degree of censoring corresponding to the second column in Figure 5 the reconstruction is satisfactory. For a higher degree of censoring corresponding to the third column in Figure 5 we get some overshoot. With increasing degree of censoring an improvement is in fact seen in the fourth column, while the rightmost column corresponding to censoring at level 0.6 gives a clear undershot. This undershot is even more pronounced for censoring at level 0.5 (data not shown).

[Figure 5 about here.]

#### 6 Discussion

In this paper we consider models for spot intensities on the pixel scale and different transformations to approximate normality and variance constance.

An empirical observation is that a logarithmic transformation with no offset is found to result in non-homogeneous variation: low-range pixel intensities show larger variation than mid-range or high-range pixels. The results from Table 1 show that inclusion of an offset  $\lambda_1$  improves the logarithmic transformation and that a further improvement is obtained with the Box-Cox transformation. The results from Table 1 also indicate, that a value of  $\lambda_2$  near 0.13 (i.e., the 8th root) is optimal for the Box-Cox transformation.

The proposed polynomial-hyperbolic spot shape model (9) is more flexible than both the cylindrical,

Gaussian and Gaussian difference models and is found to provide by far the best fit in (Table 2).

The results seen in Figure 5 indicate that with a small percentage of censoring (less than 30%, say) it should be possible to estimate parameters and predict pixel intensities for the censored pixels in a satisfactory way. An obvious consequence of this is, that the photometric laser gain in some situations may be increased such that a some pixels are saturated in order to improve the pixel intensities of the low intensity spots without any serious loss of information for the spot with highest pixels intensities.

Figure 5 also suggests that the some pixels from the spot centre need to be observed in order to estimate censored pixel values well. When only the edge and the background pixels of the spot is observed (corresponding to the last column with artificial censoring at level 0.6 and even more pronounced at level 0.5, not shown), the polynomial-hyperbolic spot shape models has difficulties in reconstructing the non-observed saturated pixel values.

It should also be possible to combine several runs with varying gains, compare the right panel in Figure 1. For spots with saturated pixels, pixel values may be reconstructed as shown in this paper. But if the censoring is too hard the corresponding estimate should be downweighted when combined with signal intensities for runs with lower gains. To find optimal weights further study is necessary.

We conclude by listing some additional items that may be studied by use of a good spot shape model:

- To find accurate estimates of the local background level. We note that the model (5) contains such a parameter  $b_s$  for the local background at spot s.
- To make a quality control by finding spots that deviate in some way as may be seen in left panel in Figure 1 (e.g., the second spot to the right of the middle circled spot and several spots in the upper part of the chip).
- To find improved estimates of spot centres and spot diameters. It is also possible that the estimate of the parameter  $B_s$  in (5) could used to estimate the total intensity of a spot, but we rather think that an average within an accurately determined circular disk would give a more robust intensity estimate for spots with all pixels uncensored.

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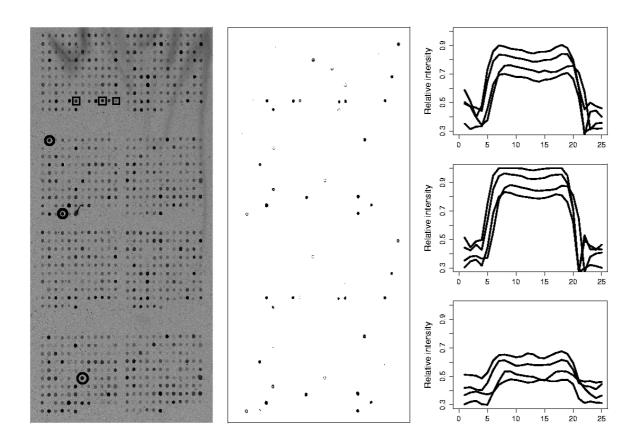


Figure 1: Inverted gray scale image of cy3 wildtype with photometric gain 60 (left panel) and the corresponding saturated pixels (middle panel). Horizontal intensity profiles through spot centres for wildtype cy3 images with gains 30, 40, 50 and 60 are shown for three spots (right panel). The three spots depicted in the right panel are the ones marked with boxes on the left panel. The three spots marked with circles are used in Figure 5.

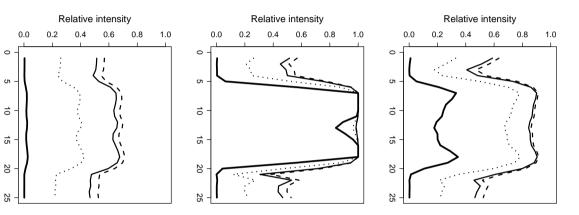


Figure 2: Examples of transformations of spots 102, 106 and 108 at gain 60. logarithmic transformation (—), inverse hyperbolic sine ( $\cdots$ ) and Box-Cox (- -). Original data (——),

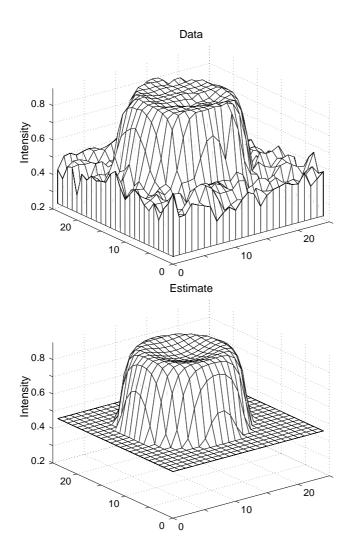


Figure 3: Three-dimensional plot of observed intensities for spot 102 at gain 60 (top surface) and estimated spot shape from the polynomial-hyperbolic shape model (bottom surface).

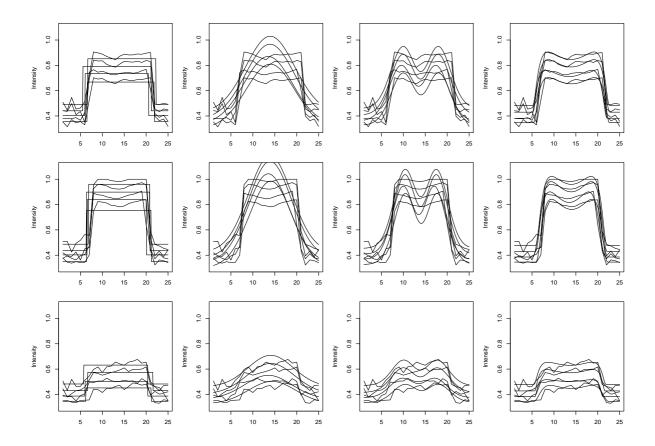


Figure 4: Horizontal intensity profiles through the centres of spots 102, 106 and 108 (each spot represented by a row) together with estimated spot shapes for each of the four spot shape models: cylindrical, Gaussian, Gaussian difference, polynomial-hyperbolic (corresponding to each column) for gains 30, 40 50 and 60. Estimates are, for each spot, based on pixels in  $25 \times 25$  area, but are here (as well as in Figure 5) displayed as profiles through the spot centre.

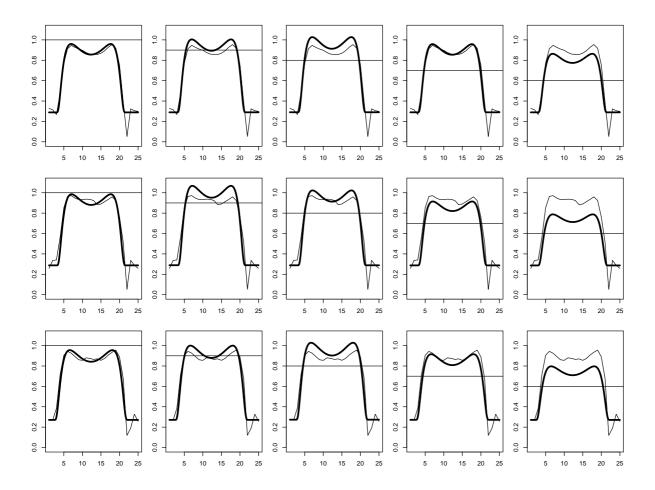


Figure 5: Horizontal intensity profiles through the centres of spots 242, 352 and 787 (each spot represented by a row) at photometric gain 60 for the polynomial-hyperbolic spot shape model for different levels of (artificial) censoring as indicated by a horizontal line. For each profile both data (thin lines) and the reconstruction are shown. The average fraction of pixels that were censored among the  $25 \times 25$  pixels regarded for each spot were (from the left) in the five columns: 0%, 17%, 29%, 30% and 32%, respectively.

Parameter estimate								
Transformation	$\sigma_s$	$a_s$	$\gamma_s$	$\lambda_{1s}$	$\lambda_{2s}$	logLikelihood incr.		
Logarithmic (fixed $\lambda_1$ )	4.83	0.66	1.87	$1^{\dagger}$		47.74		
Logarithmic	4.81	0.64	1.87	10.51		13.82		
Inv. hyperbolic sine	4.90	0.63	1.82	7.43	1.32	11.42		
Box-Cox (fixed $\lambda$ 's)	4.86	0.84	1.86	$3.35^{\dagger}$	$0.13^{\dagger}$	6.70		
Box-Cox	4.98	0.63	1.86	3.35	0.13	0		

† Values fixed.

Table 1: Comparison of transformations: Median values for selected estimated parameters from the three transformations for 25 spots and four gains. The log likelihood increase is the median increase of the log likelihood (13) for a given transformation relative to the log likelihood for the Box-Cox transformation.

Parameter estimate							
Spot shape model	$\sigma_s$	$a_s$	$\gamma_s$	$\lambda_{1s}$	$\lambda_{2s}$	logLikelihood incr.	
Cylindrical	7.61			1.98	0.04	178.248	
Gaussian	5.34			1.17	-0.05	283.46	
Gaussian difference	6.32			1.13	0.04	263.47	
Polynomial-hyperbolic	4.98	0.63	1.86	3.35	0.13	0	

Table 2: Comparison of spot shapes: Median values for selected estimated parameters from the four spot shape models for 25 spots and four gains. The log likelihood increase is the median increase of the log likelihood (13) for a given spot shape model relative to the log likelihood for the polynomial-hyperbolic spot shape.