Tentamen i MVE041 och MMGL32 Flervariabelmatematik

Den 30 May 2015, kl. 830-1230

Hjälpmedel: Formelblad (bifogat), inga räknare.

Telefon: Gustav Kettil, 0703-088304

Totalpoäng 50. För godkänt påtentan krävs antingen 25 utav 32 poäng pågodkäntdelen, inklusive eventuella bonuspoäng. För godkänt påkursen skall också Matlabmomentet vara godkänt. För betyg 4 eller 5 krävs dessutom 33 resp. 42 poäng sammanlagt påtentamens alla delar.

Lösningar läggs ut påkursens webbsida första vardagen efter tentamensdagen. Tentan rättas och bedöms anonymt. Resultat meddelas via Ladok ca. tre veckor efter tentamenstillfället. Första granskningstillfälle meddelas påkurswebbsidan, efter detta sker granskning alla vardagar 9-13, MV:s exp.

Godkäntdel

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Överbetygsdel

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Exam for MVE041 och MMGL32 Flervariabelmatematik

The 30 May 2015, kl. 830-1230

Help materials: Attached formula sheet. No calculators.

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Total points are 50. Passing this course requires a) 25 points of 32 points on the *Passing Part*, and b) a pass on all six Matlab labs. Your bonus points from this course apply to the passing part of the exam. The maximum score on the passing part is 32. A grade of 4 or 5 is obtained with scores of 33, and 42 respectivley. Bonus points do not apply to the mastery part of the exam.

Solutions will be posted on the course website on the first weekday following the exam. The exam is graded anonymously. Results are available on Ladok starting three weeks after the exam day. The first day on which you may contest your grade will be posted on the course website, and after that you may file a contest with the MV exp any week day 9-13.

Passing Part

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Mastery Part

...

Equations and Formulas MVE041, 14/15

Geometri

Circle radius a: $Area = \pi a^2$.
Sphere of radius a: $Vol. = \frac{4}{3}\pi a^3$, $Area = 4\pi a^2$

Cylinder radius a, height h: $Vol. = \pi a^2 h$, $Area = 2\pi a h$.
Circular cone rad. a, height h. $Vol. = 1/3\pi a^2 h$

Trigonometri

$\sin(2x) = 2\sin(x)\cos(x)$
$\cos(2x) = 1 - 2\sin^2(x)$
$\cos(x+y) = \cos(x)\cos(y) - \sin(x)\sin(y)$
$\sin(x+y) = \sin(x)\cos(y) + \cos(x)\sin(y)$

$\cos(x)\cos(y) = \frac{1}{2}(\cos(x-y) + \cos(x+y))$
$\sin(x)\sin(y) = \frac{1}{2}(\cos(x-y) - \cos(x+y))$
$\sin(x)\cos(y) = \frac{1}{2}(\sin(x-y) + \sin(x+y))$
$\cos^2(x) + \sin^2(x) = 1$

Derivater

$\frac{d}{dx}x^a = ax^{a-1}$,
$\frac{d}{dx}\sqrt{x} = \frac{1}{2}\sqrt{x}$

$\frac{d}{dx}e^x = e^x$
$\frac{d}{dx}\ln(x) = \frac{1}{x}, x > 0$

$\frac{d}{dx}\cos(x) = -\sin(x)$
$\frac{d}{dx}\sin(x) = \cos(x)$

$$\textbf{grad}\, f(x,y,z) = \bar{\nabla} f(x,y,z), \quad \textbf{div}\, \bar{\mathbf{F}}(x,y,z) = \bar{\nabla}\cdot\bar{\mathbf{F}}(x,y,z), \quad \textbf{curl}\, \bar{\mathbf{F}}(x,y,z) = \bar{\nabla}\times\bar{\mathbf{F}}(x,y,z)$$

Integrals

$$\int x^a dx = \frac{x^{a+1}}{a+1} + C \qquad \int \frac{1}{x}dx = \ln|x| + C,$$

$$\int \sin(x)dx = -\cos(x) + C, \qquad \int \cos(x)dx = \sin(x) + C$$

$$\int e^x dx = e^x + C, \qquad \int \ln(x)dx = x\ln(x) - x + C,$$

$$\int \sin^2(x)dx = \frac{x}{2} - \frac{1}{4}\sin(2x) + C, \qquad \int \cos^2(x)dx = \frac{x}{2} + \frac{1}{4}\sin(2x) + C,$$

$$\int \sin^3(x)dx = -\frac{1}{3}\sin^2(x)\cos(x) - \frac{2}{3}\cos(x) + C, \qquad \int \cos^3(x)dx = \frac{1}{3}\cos^2(x)\sin(x) + \frac{2}{3}\sin(x) + C,$$

$$\int \frac{dx}{\sqrt{a^2-x^2}} = -\sin^{-1}\left(\frac{x}{a}\right) + C, \quad (a > 0, |x| < a)$$

$$\int \frac{dx}{a^2+x^2} = \frac{1}{a}\tan^{-1}\left(\frac{x}{a}\right) + C, \quad (a > 0)$$

$$\int \frac{dx}{a^2-x^2} = \frac{1}{2a}\ln\left|\frac{x+a}{x-a}\right| + C, \quad (a > 0)$$

$$\int \frac{dx}{x\sqrt{a^2-x^2}} = \frac{1}{a}\sec^{-1}\left|\frac{x}{a}\right| + C, \quad (a > 0, |x| > a)$$

Maclaurinutvecklingar

$$e^x = \sum_{k=0}^{\infty} \frac{x^k}{k!} \qquad \ln(1+x) = \sum_{k=1}^{\infty}(-1)^{k+1}\frac{x^k}{k}$$

$$\sin x = \sum_{k=1}^{\infty}(-1)^{k-1}\frac{x^{2k-1}}{(2k-1)!} \qquad \cos x = \sum_{k=0}^{\infty}(-1)^k\frac{x^{2k}}{(2k)!}$$

$$(1+x)^\alpha = \sum_{k=0}^{\infty}\frac{\alpha!}{k!(\alpha-k)!}x^k \qquad \frac{1}{1-x} = \sum_{k=0}^{\infty}x^k$$