Formelblad

Trigonometriska formler

$$\sin(x+y) = \sin x \cos y + \cos x \sin y \qquad \sin^2 x = \frac{1-\cos 2x}{2}$$

$$\cos(x+y) = \cos x \cos y - \sin x \sin y \qquad \cos^2 x = \frac{1+\cos 2x}{2}$$

$$\tan(x+y) = \frac{\tan x + \tan y}{1 - \tan x \tan y}$$

Några integraler (integrationskonstanter är utelämnade)

$$\int \frac{1}{x^2+a}\,dx = \frac{1}{\sqrt{a}} \cdot \arctan \frac{x}{\sqrt{a}}\ , \quad a>0. \qquad \int \frac{1}{x^2-a}\,dx = \frac{1}{2\sqrt{a}} \cdot \ln\left|\frac{x-\sqrt{a}}{x+\sqrt{a}}\right|\ , \quad a>0.$$

$$\int \frac{1}{\sqrt{a-x^2}}\,dx = \arcsin \frac{x}{\sqrt{a}}\ , \quad a>0. \qquad \int \frac{1}{\sqrt{x^2+a}}\,dx = \ln\left|x+\sqrt{x^2+a}\right|\ , \quad a>0.$$

$$\int \sqrt{x^2+a}\,dx = \frac{1}{2}\left(x\sqrt{x^2+a} + a\ln\left|x+\sqrt{x^2+a}\right|\right)$$

Malaurinutvecklingar

$$e^x = 1 + x + \frac{x^2}{2} + \cdots + \frac{x^n}{n!} + \frac{x^{n+1}}{(n+1)!}e^{\theta x}$$

$$\ln(1+x) = x - \frac{x^2}{2} + \cdots + (-1)^{n-1}\frac{x^n}{n} + (-1)^n \frac{x^{n+1}}{(n+1)} \cdot \frac{1}{1+\theta x}$$

$$(1+x)^\alpha = 1 + \alpha x + \frac{\alpha(\alpha-1)}{2}x^2 + \cdots + \binom{\alpha}{n}x^n + \binom{\alpha}{n+1}x^{n+1} \cdot \frac{1}{(1+\theta x)^{n+1-\alpha}}$$

$$\sin x = x - \frac{x^3}{6} + \cdots + (-1)^{n-1}\frac{x^{2n-1}}{(2n-1)!} + (-1)^n \frac{x^{2n+1}}{(2n+1)!}\cos \theta x$$

$$\cos x = 1 - \frac{x^2}{2} + \cdots + (-1)^n \frac{x^{2n}}{(2n)!} + (-1)^{n+1}\frac{x^{2n+2}}{(2n+2)!}\cos \theta x$$

$$\arctan x = x - \frac{x^3}{3} + \cdots + (-1)^{n-1}\frac{x^{2n-1}}{2n-1} + (-1)^n \frac{x^{2n+1}}{(2n+1)} \cdot \frac{1}{1+(\theta x)^2}$$

Stirlings formel

$$n! = \left(\frac{n}{e}\right)^n \cdot \sqrt{2\pi n} \cdot (1+\epsilon_n)\ , \ \text{där} \quad \epsilon_n \to 0 \quad \text{då } n \to \infty.$$