## Differentiable $L^1$ -functional calculus for self-adjoint operators

Let T be a self-adjoint operator on the square-integrable functions on some measure space X. According to the spectral theorem, a bounded Borel function f induces a bounded operator f(T) on  $L^2(X)$ .

An interesting question is now, under which additional assumptions on f the operator f(T) extends to a bounded operator on  $L^1(X)$ .

The talk will treat some special situations, which are related to sub-lapacians on Lie groups with exponential volume growths.

(To follow the talk, deeper knowledge about Lie groups is not required.)