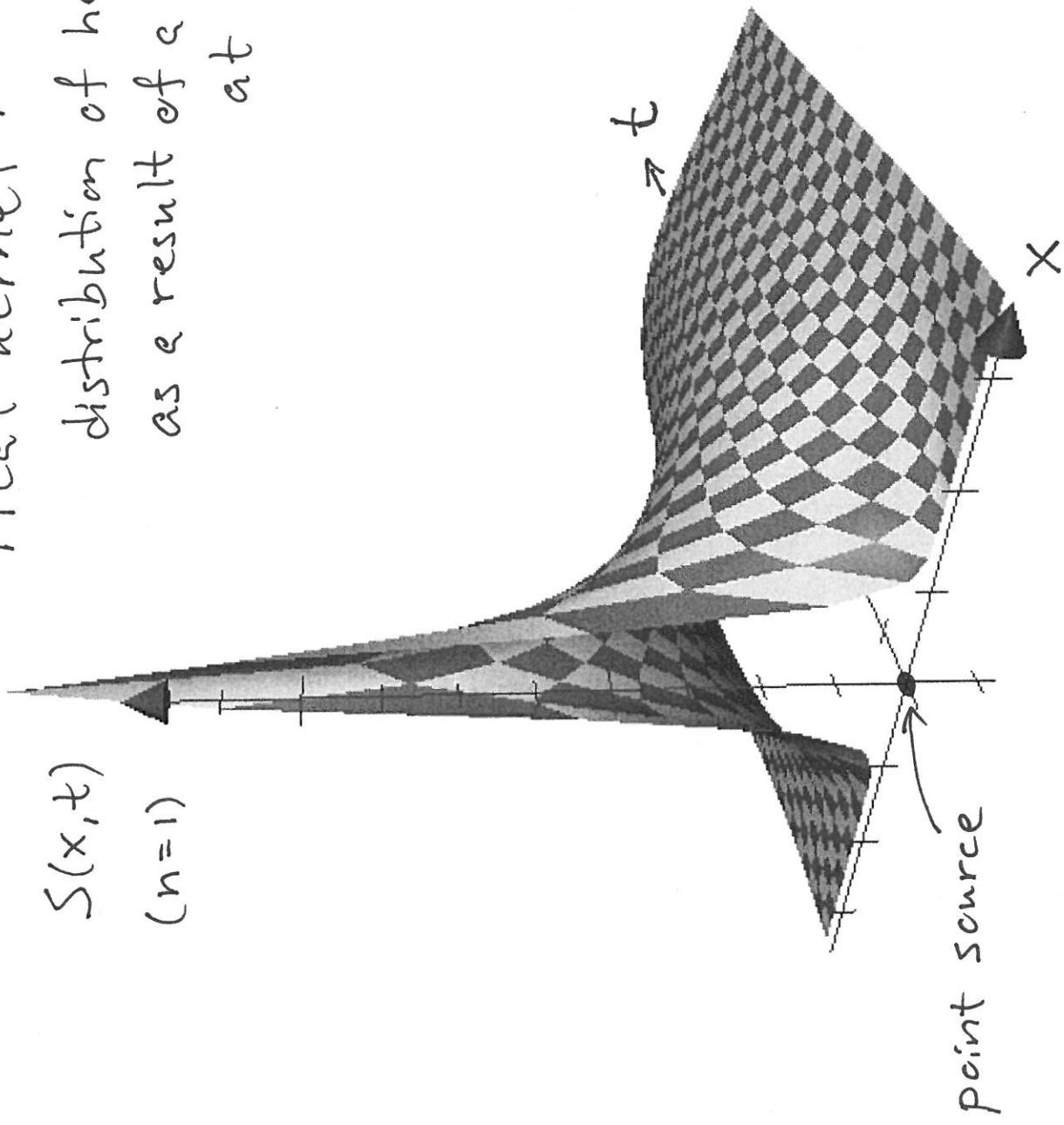


Heat kernel :

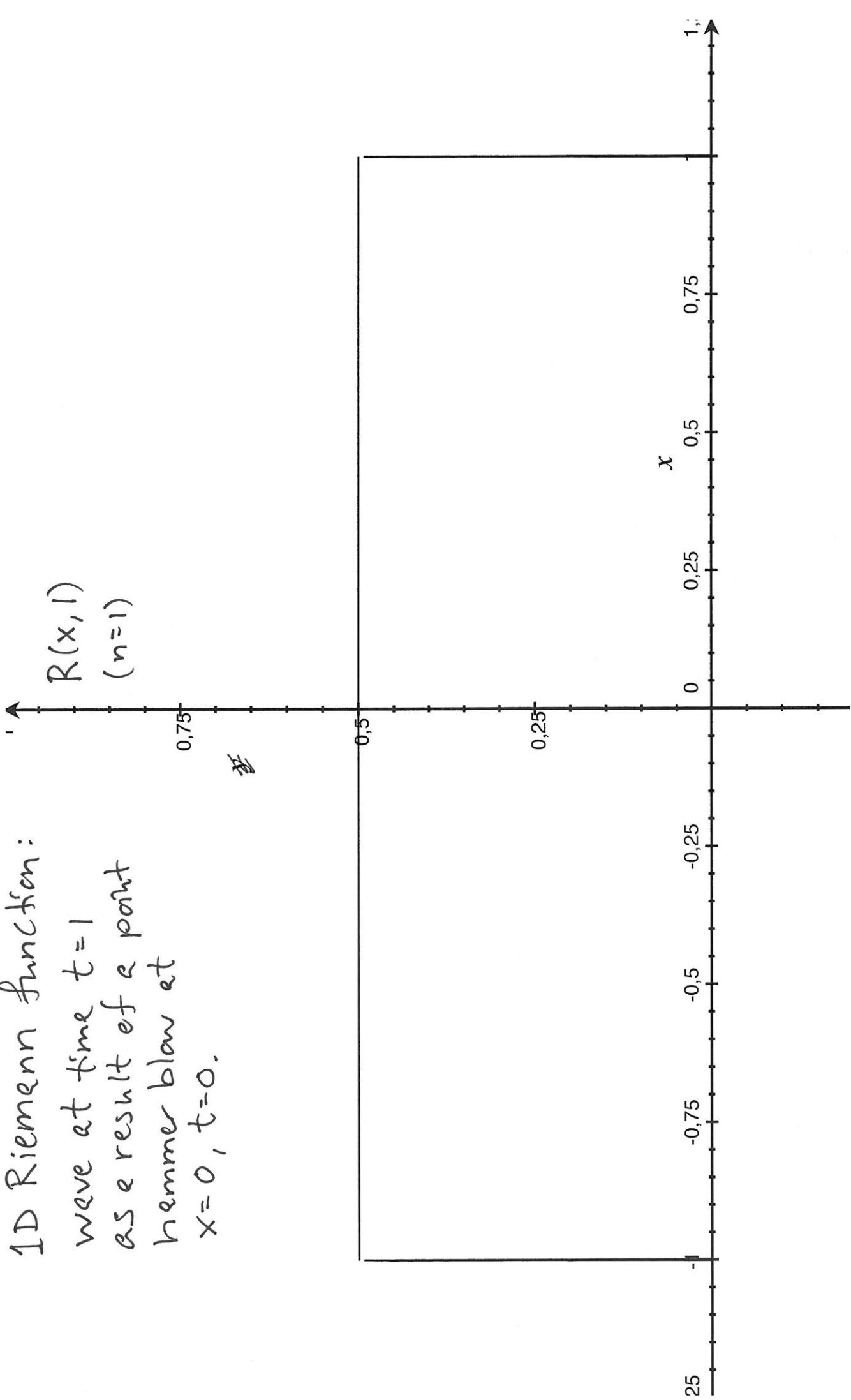
$$S(x, t) \\ (n=1)$$

distribution of heat / mass
as a result of a point source
at $x = 0, t = 0$.



1D Riemann function:

wave at time $t=1$
as a result of a point
hammer blow at
 $x=0, t=0.$



2D Riemann function:

wave at time $t=1$

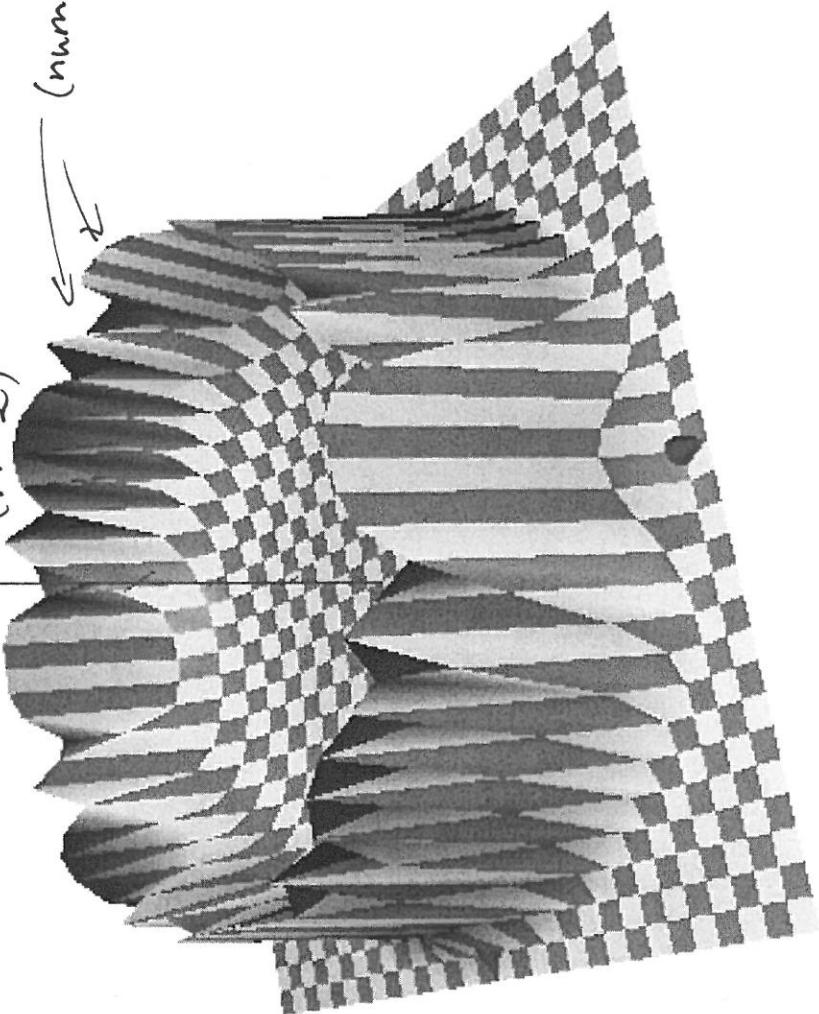
as a result of a point
hammer blow at

$$(x, y) = (0, 0), \quad t=0.$$

$$R(x, y, t)$$

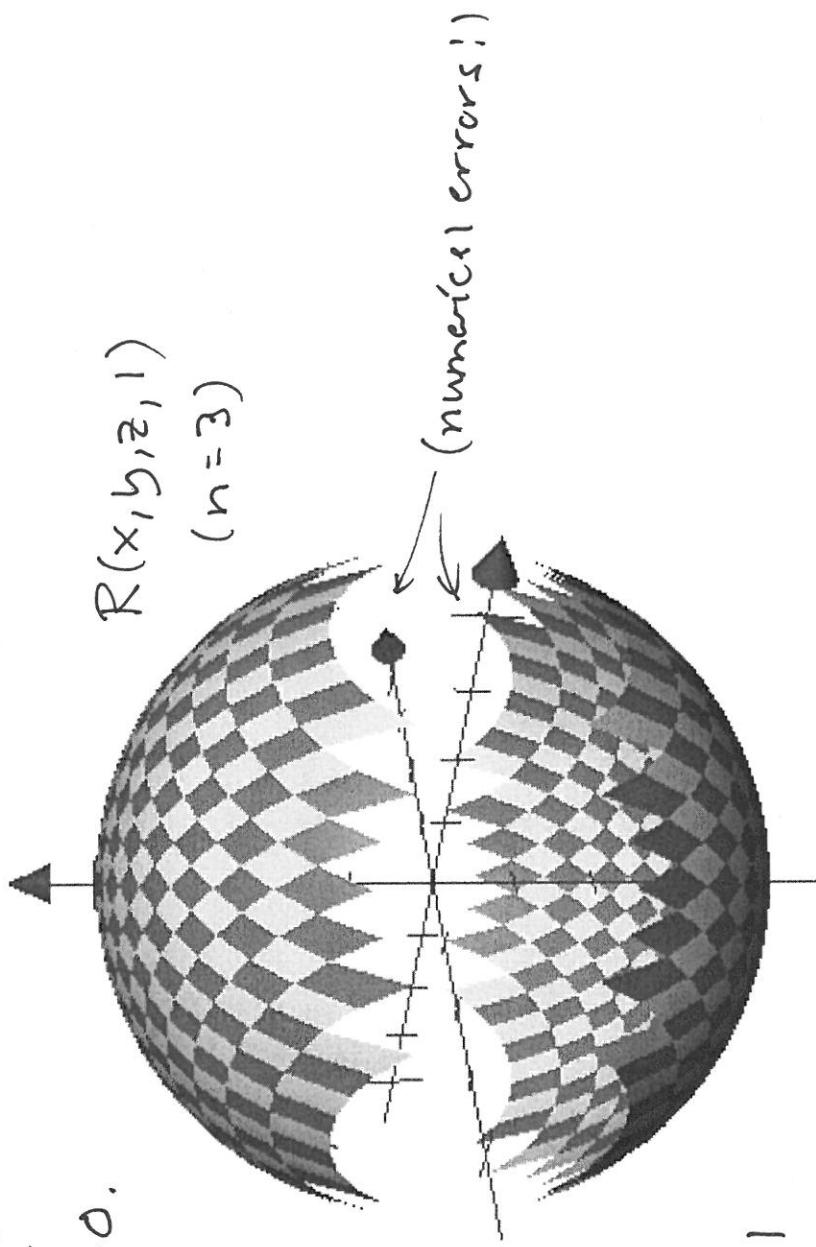
($n=2$)

← (numerical errors!)

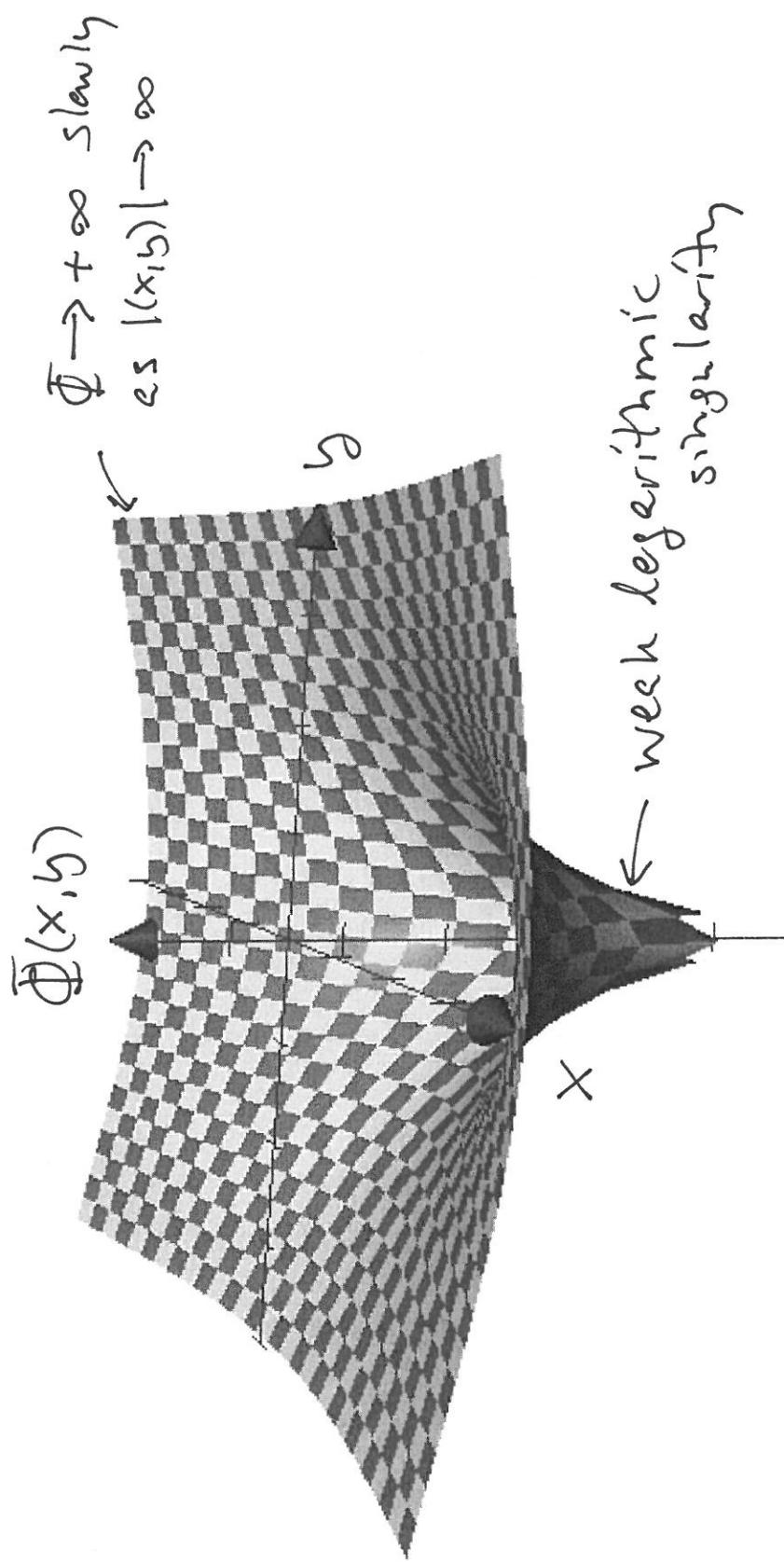


3D Riemann function:

wave at time $t=1$
as a result of a point
hammer blow at
 $(x,y,z) = (c,0,0)$, $t=0$.



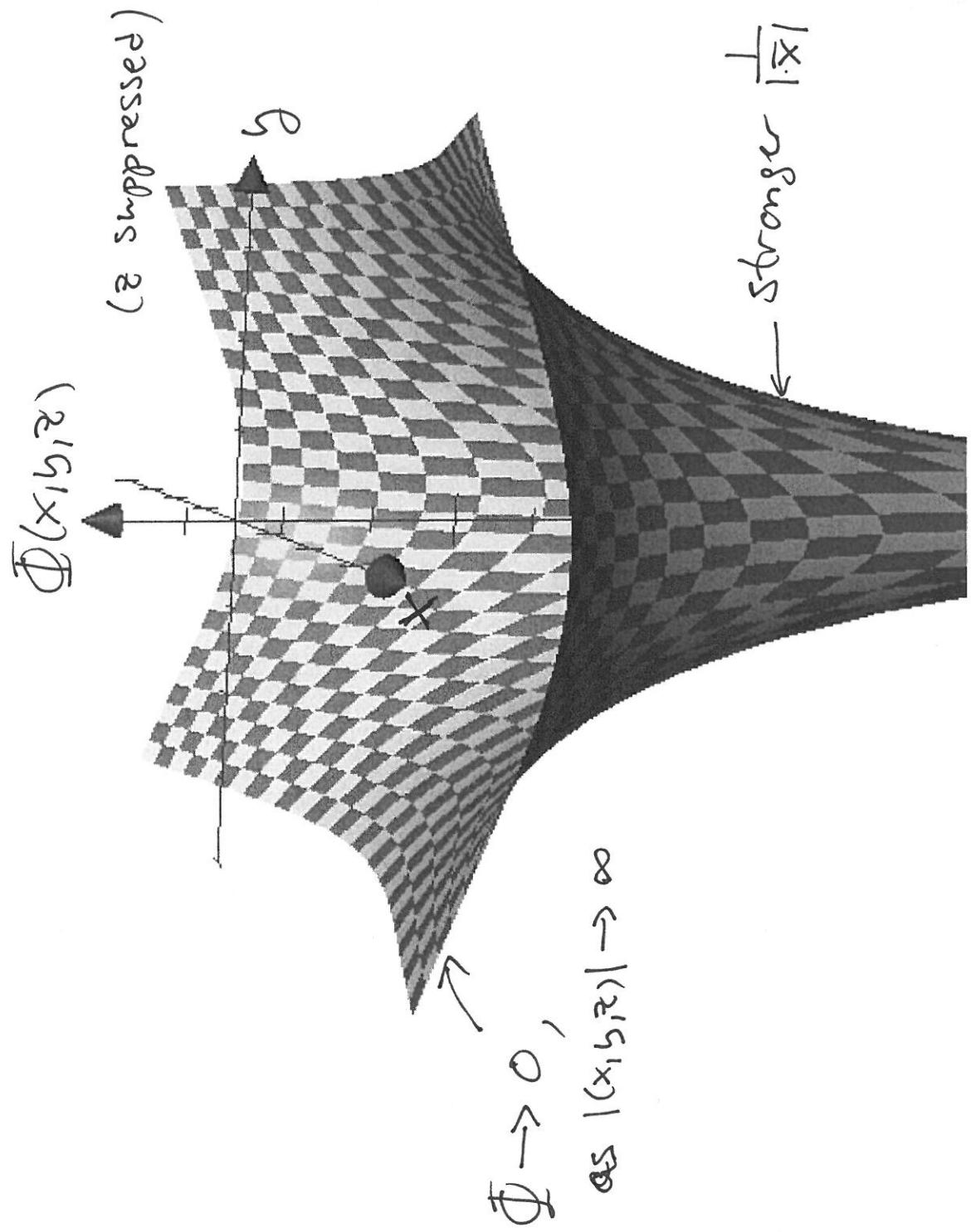
$$R = \begin{cases} \infty & ; x^2 + y^2 + z^2 = 1 \\ 0 & ; x^2 + y^2 + z^2 \neq 1 \end{cases}$$

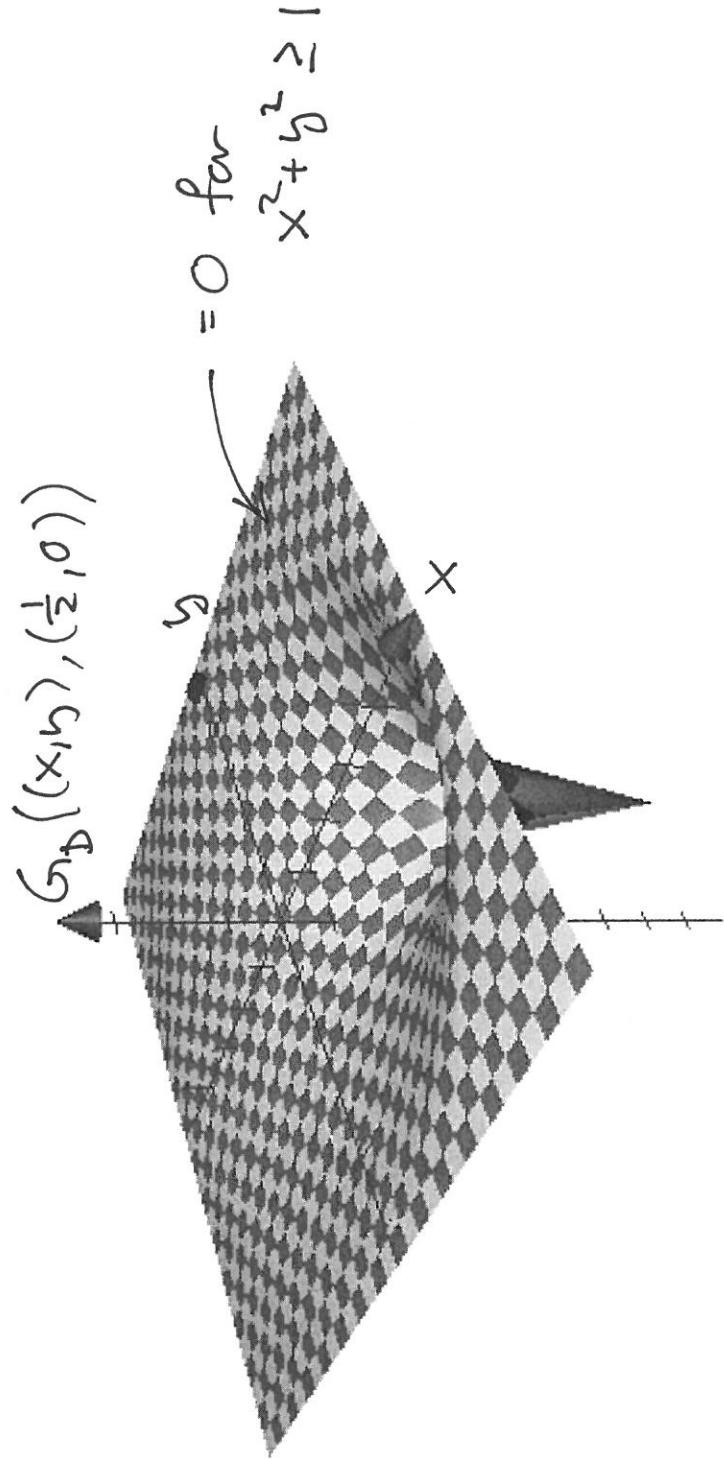


2D fundamental solution for Δ :
 potential from point source at $(x,y) = (0,d)$

3D fundamental solution for Δ :

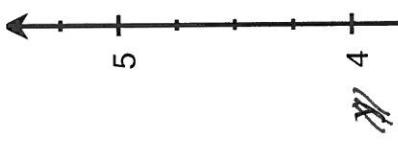
potential from point source at $(x_1, y_1, z_1) = (0, 0, 0)$.





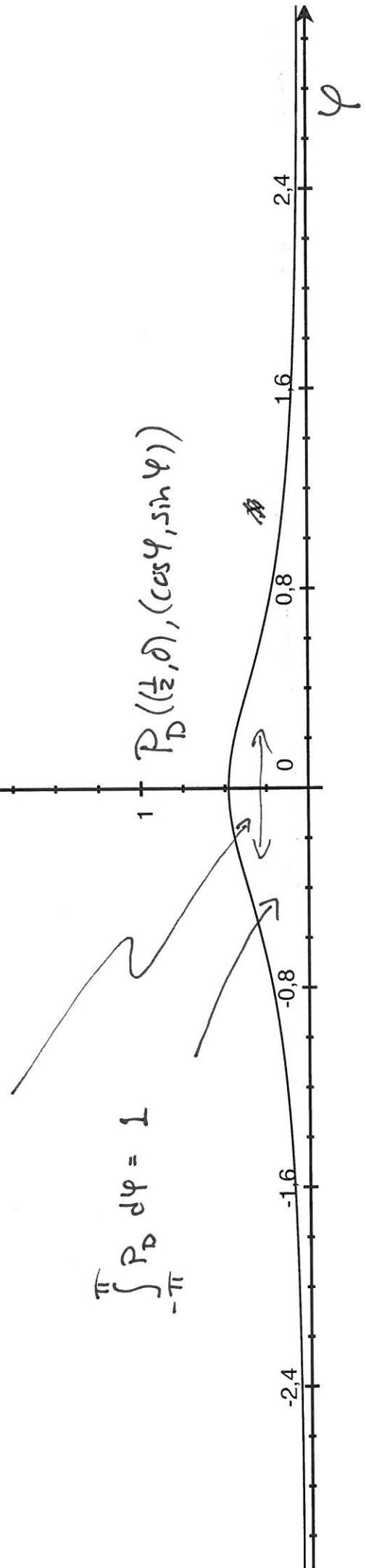
Green's function for the unit disk with pole at $(\frac{1}{2}, 0)$:
 potential from point source at $(\frac{1}{2}, 0)$, with the
 unit circle conducting and grounded.

Poisson kernel for the unit disk with pole at $(\frac{1}{2}, 0)$:
 the normal derivative of the Green's function at the boundary.

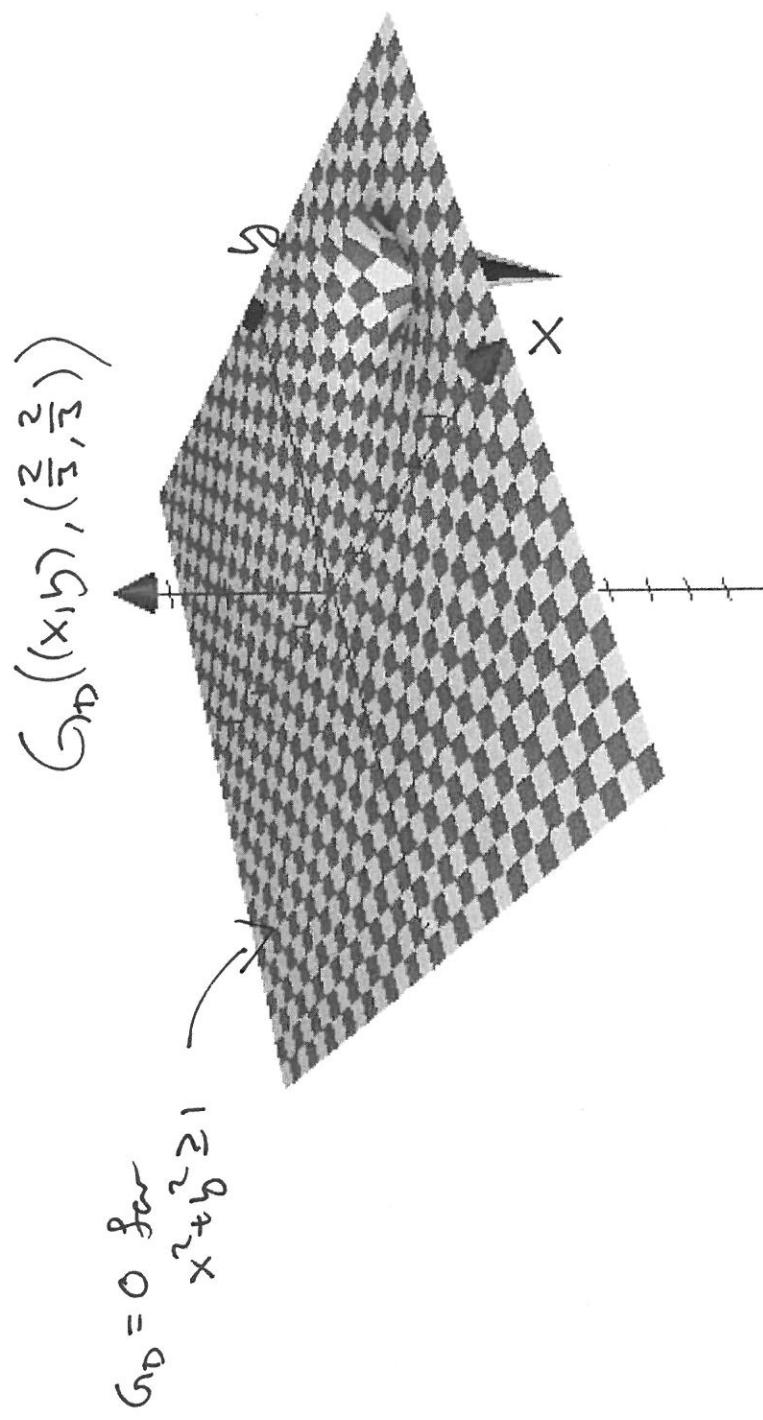


$$\text{width} \approx | -1 - (\frac{1}{2}, 0) |$$

$$\int_{-\pi}^{\pi} P_D(\frac{1}{2}, \theta), (\cos \varphi, \sin \varphi)) d\varphi = 1$$



Green's function for the unit disk with pole at $(\frac{2}{3}, \frac{2}{3})$:
potential from point source at $(\frac{2}{3}, \frac{2}{3})$, with the
unit circle conducting and grounded.



$P_D\left((\frac{2}{3}, \frac{2}{3}), (\cos\varphi, \sin\varphi)\right)$
 Poisson kernel for the
 unit disk with pole at $(\frac{2}{3}, \frac{2}{3})$:
 the normal derivative of
 the Green's function at
 the boundary.

